EPFL

Modern PV-Technologies
3.3: Junctions

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Current-voltage characteristic

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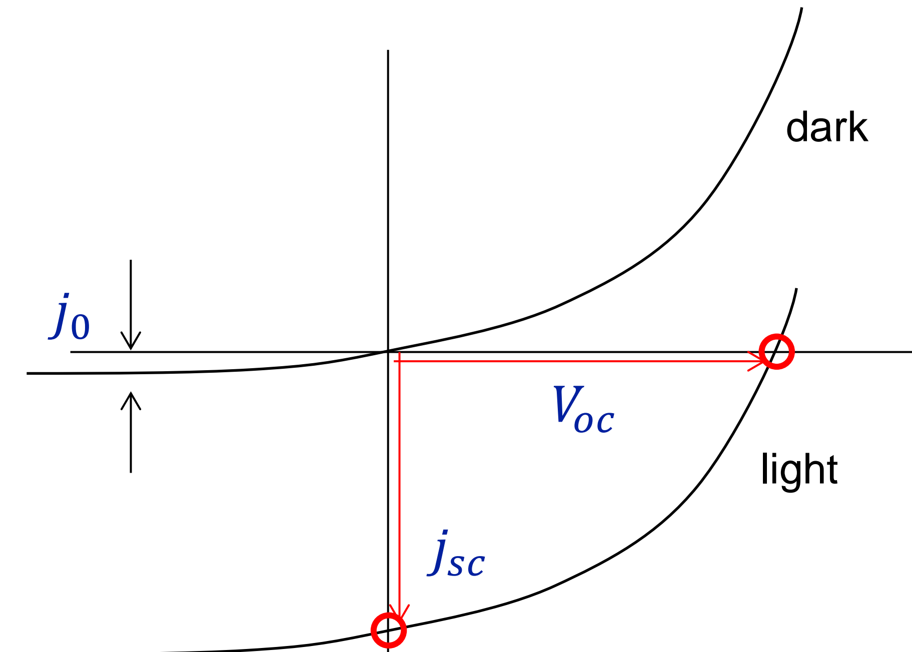
Simple form of j-V characteristics

Dark:

$$j = j_0\left(e^{qV/kT} - 1\right)$$

Illuminated (superposition principle):

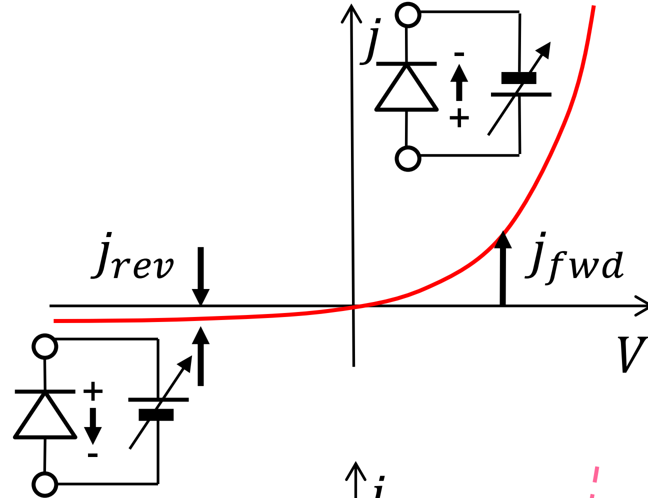
$$j = j_0\left(e^{qV/kT} - 1\right) - j_{ph}$$

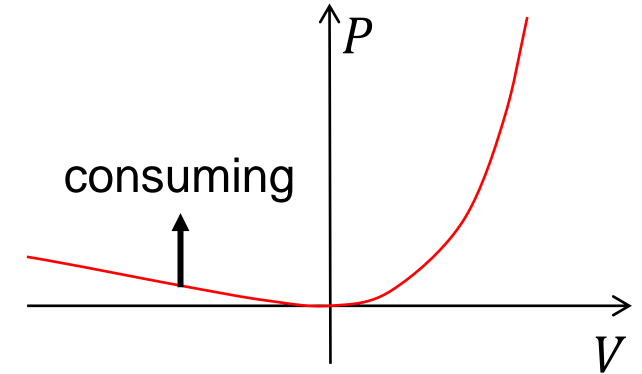


Sign convention

dark

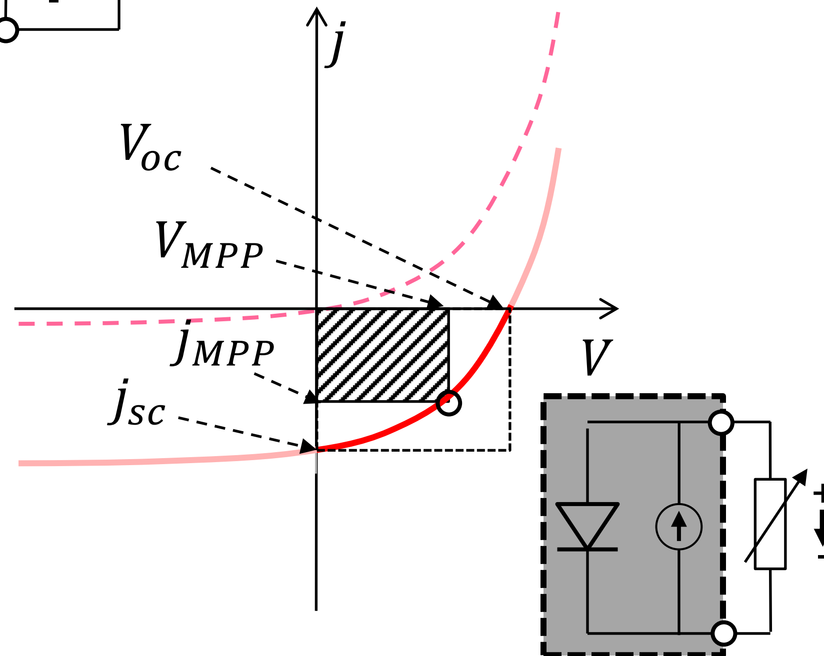
$$j = j_0 \left[\exp\left(\frac{qV}{kT}\right) - 1 \right]$$

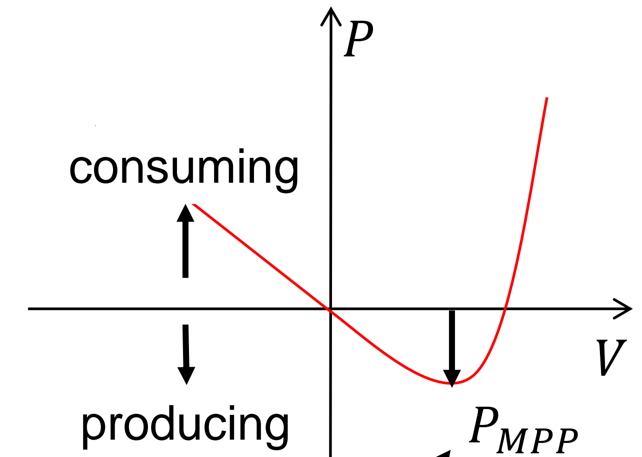




light

$$j = j_0 \left[\exp\left(\frac{qV}{kT}\right) - 1 \right] - j_L$$





Power can be delivered to a load !

Special points of the characteristic

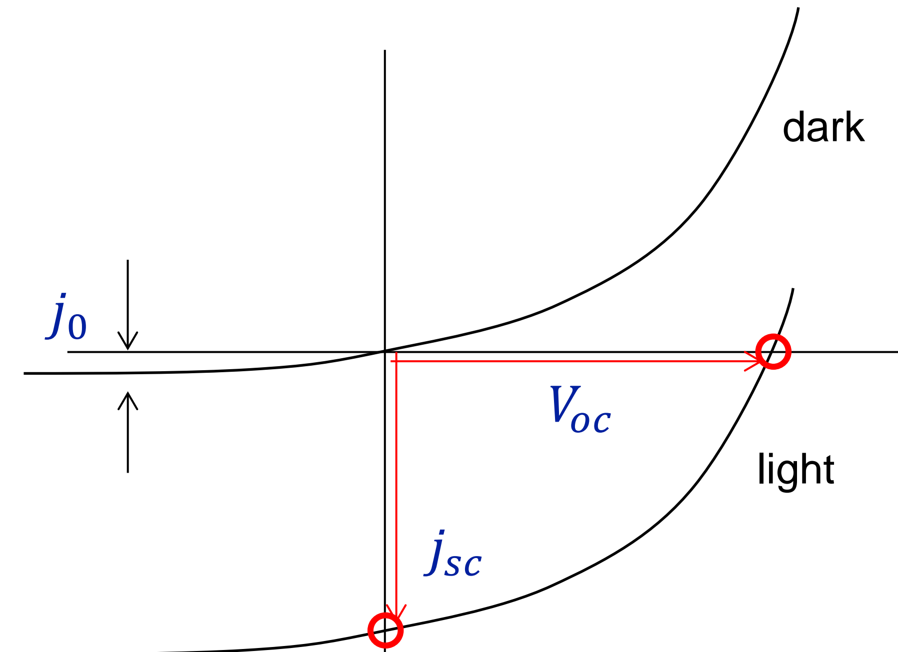
Simple form of j-V characteristics

$$j = j_0\left(e^{qV/kT} - 1\right) - j_{ph}$$

Short circuit current ($V = 0$):
$j_{sc} = j_{ph}$

Open circuit voltage ($j = 0$):

$$V_{oc} = \frac{kT}{q}\ln\left(\frac{j_{ph}}{j_0} + 1\right)$$



Knobs to turn for high V_{oc}:

kT/q is fixed by operating conditions (ambient to approx. +70°C)
j_{sc} is fixed by solar irradiation; slight control via absorption enhancement
j_0 should be as small as possible

Saturation current

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Ideal j_0 for diffusion transport in infinite cell (almost valid for silicon):

$$j_0 = \left(\frac{q D_n n_i^2}{L_n N_A} + \frac{q D_p n_i^2}{L_p N_D} \right)$$

contribution of p-type absorber:

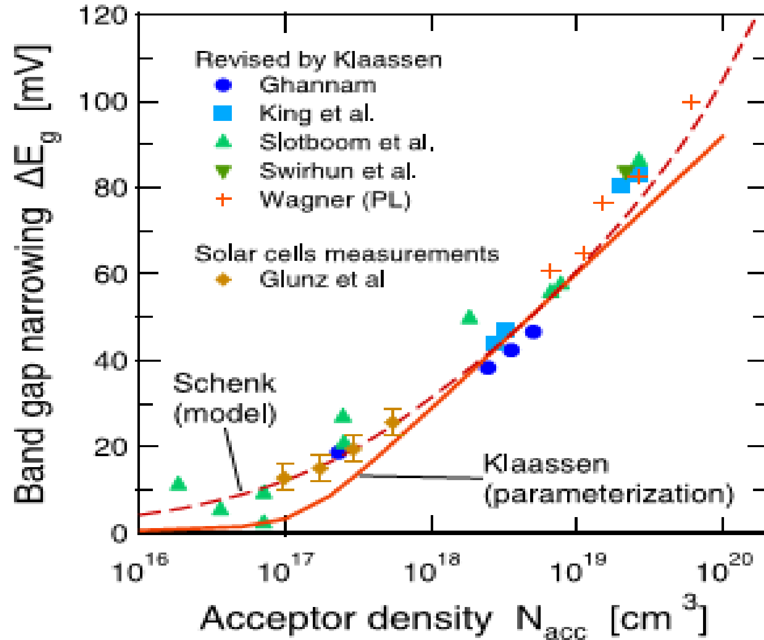
$$j_0 = \frac{q D_n n_i^2}{L_n N_A} = \frac{q n_i^2}{N_A} \cdot \sqrt{\frac{D_n}{\tau_n}}$$

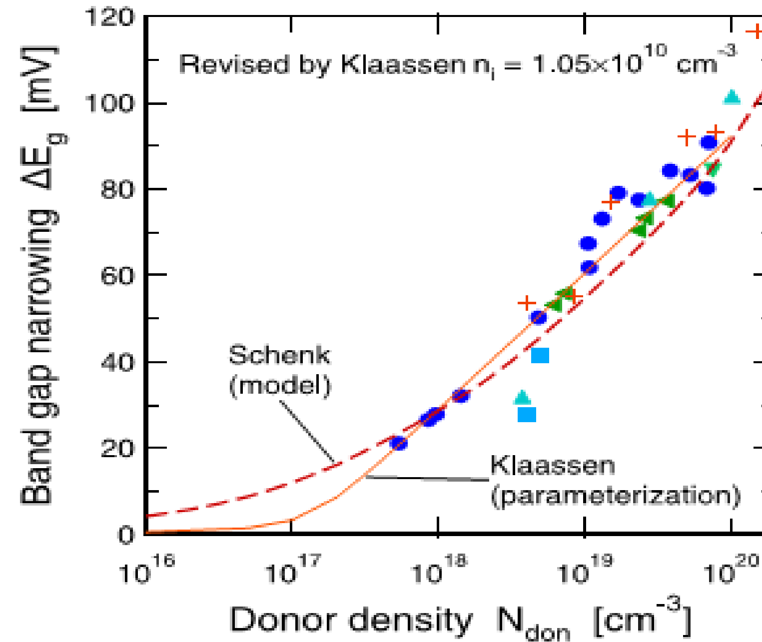
Knobs to turn for small j_0:

increase N_A (but…)

Intrinsic carrier density

Band gap narrowing (BGN)





Remember: $n_i^2 \sim e^{-\frac{E_g}{kT}} = e^{-\frac{E_{g,0}-\Delta E_g}{kT}}$

On BGN models: e.g. Altermatt, J. Comput. Electron. (2011)

Diffusion coefficient

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Einstein relation: $D = \mu \cdot \frac{kT}{q}$

phonon scattering | ionized impurity scattering (non degenerate) | ionized imp. scattering (degenerate)

Boron
p-type c-Si
holes
electrons
Mobility (cm^2/Vs)
Acceptor concentration (cm^{-3})

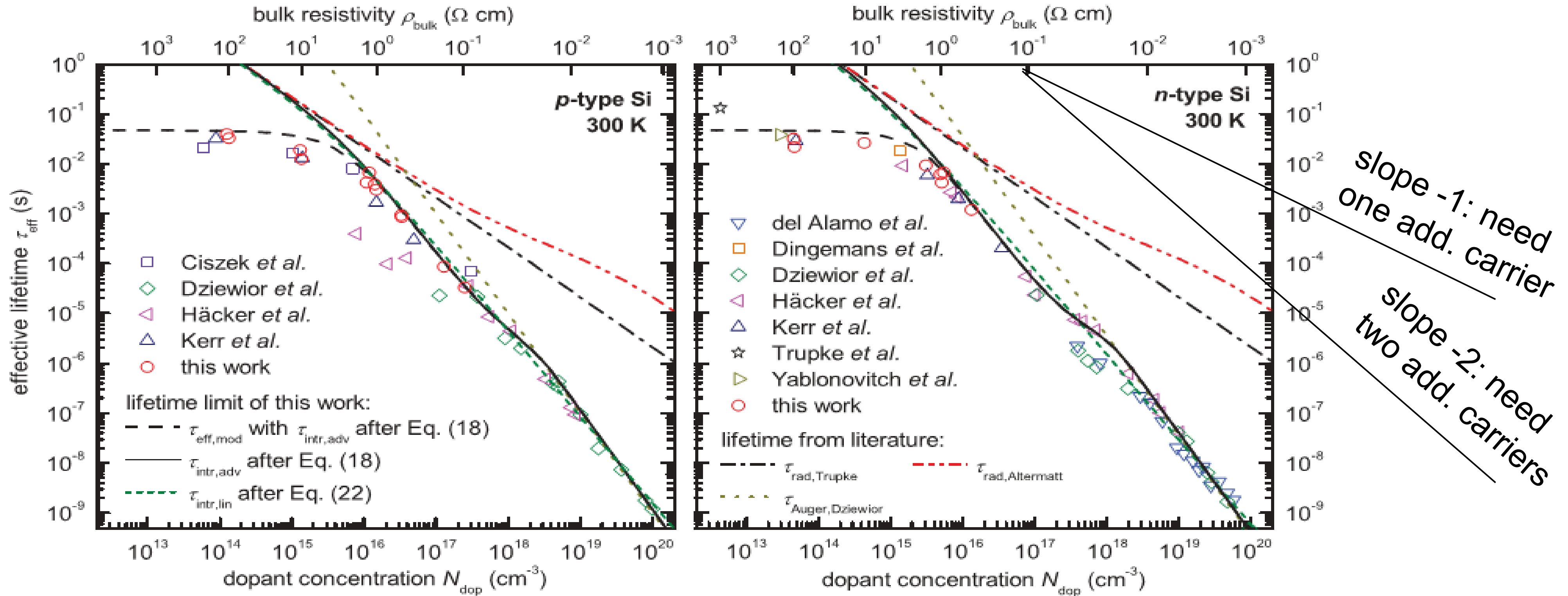
Phosphorus
n-type c-Si
electrons
holes
Mobility (cm^2/Vs)
Donor concentration (cm^{-3})

High doping will decrease D (both majority and minority, but slightly differently)

Majority mobility: Thurber, JECS (1980, 1981)
Minority mobility: Swirhun, TED (1986)

Minority carrier lifetime

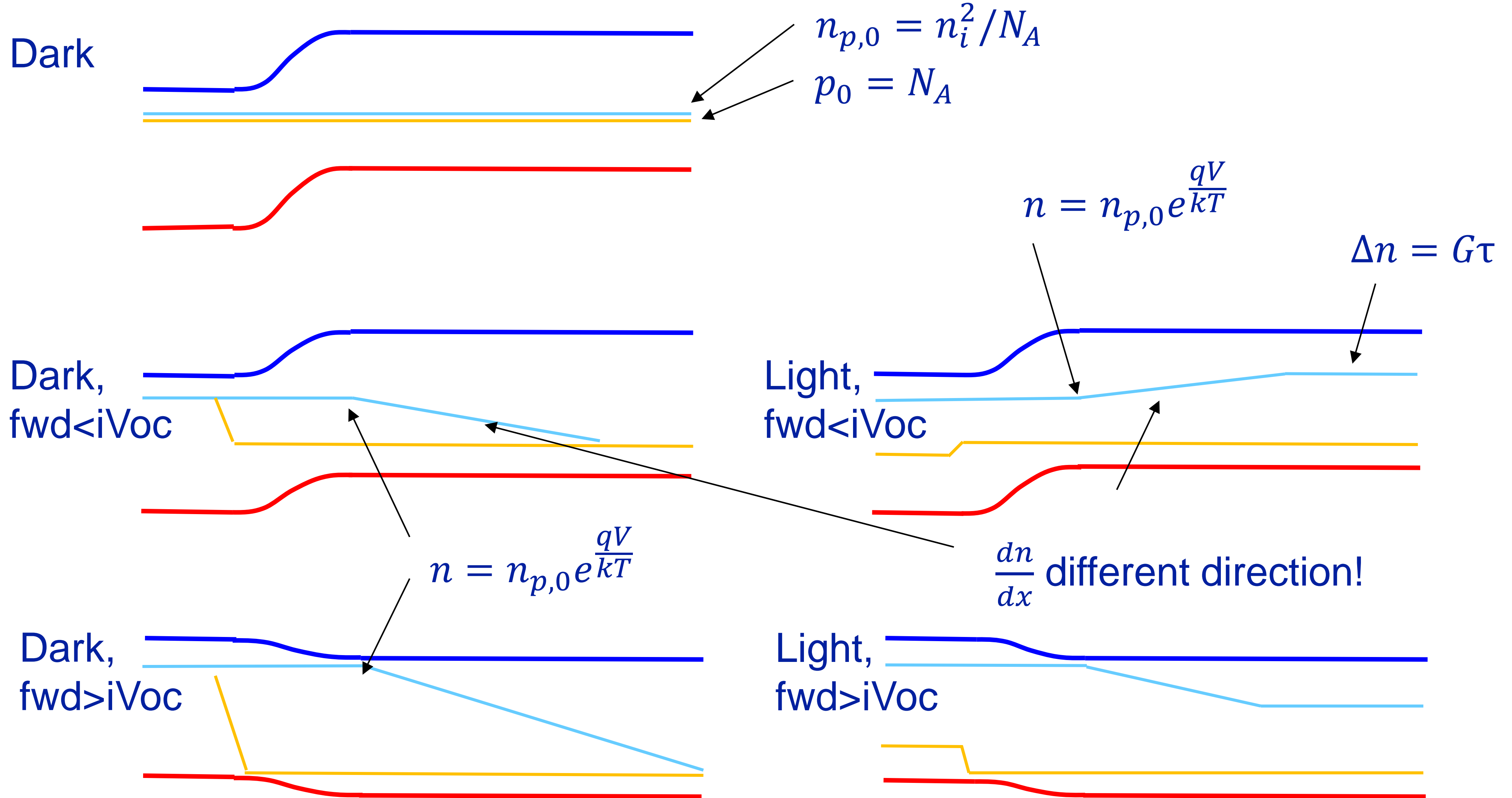
$$\tau^{-1} = \tau_{Auger}^{-1} + \tau_{rad}^{-1} + \tau_{bulk}^{-1}$$



High doping will also decrease τ!

reviews on Auger-limited lifetimes: Kerr, PPV (2003)
Richter, PRB (2012)
Niewelt, SEM (2022)

QFL splitting and minority carrier lifetime (infinite cell)



Steady state minority carrier density – QFL splitting

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Recombination rate: $R = \Delta n / \tau$

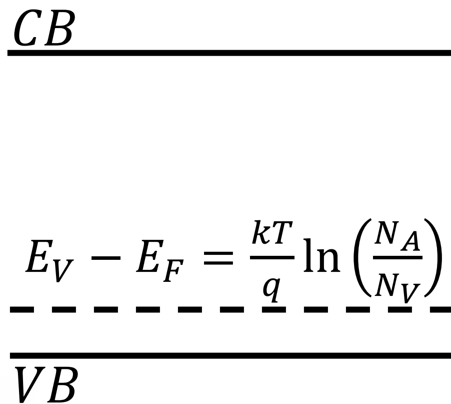
When no carriers are extracted (e.g. semiconductor w/o contacts or solar cell at Voc):
=> Recombination rate R = Optical generation rate G

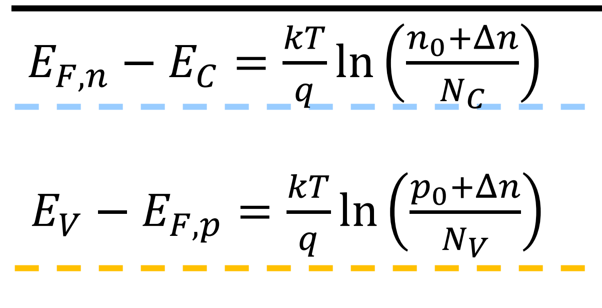
$\Delta n = G\tau$ (excess minority carrier density in steady state)

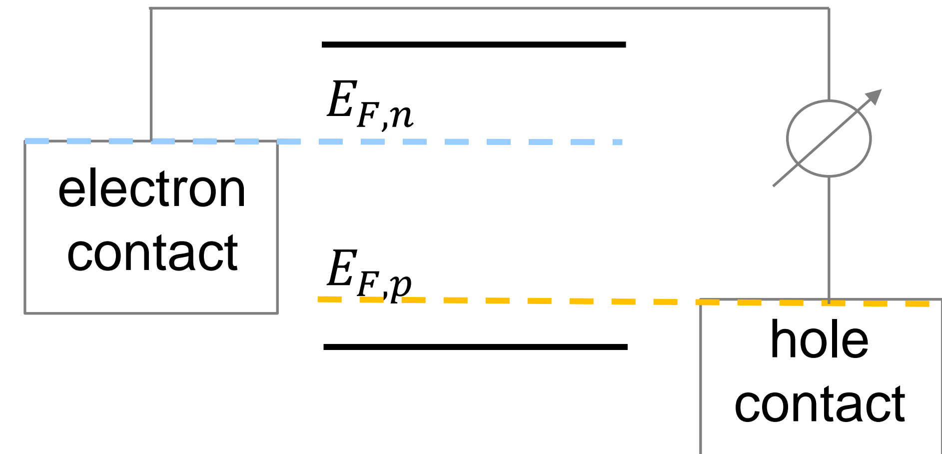
Dark:
thermal equilibrium,
unique Fermi level

Illuminated:
Define independent
quasi Fermi levels (QFLs)

With idealized contacts:
QFL splitting equal to
achievable voltage







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Implied open circuit voltage (iVoc)

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For ideal contacts: QFL splitting equal to external voltage

Assume

- $N_A = 10^{16}$ cm^{-3} (= p_0)
- $G \approx 10^{19}$ cm^{-3}s^{-3}
- $\tau \approx 1$ ms (minority carrier lifetime)

$$\Delta n = G\tau \approx 10^{16} \text{ cm}^{-3}$$

$$iV_{oc} = \frac{kT}{q} \ln \frac{np}{n_i^2} \approx 720 \text{ mV}$$

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Limiting efficiency

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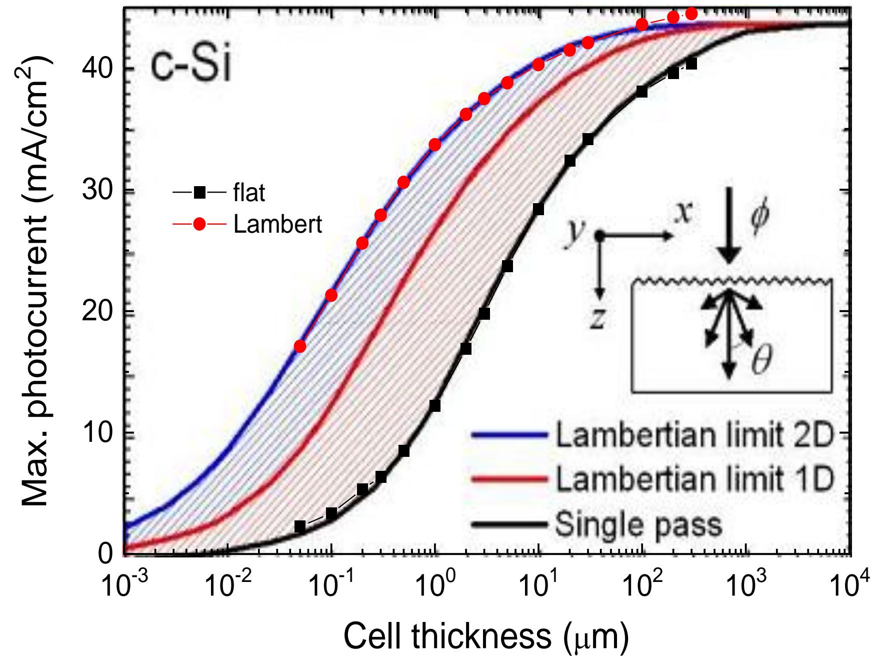
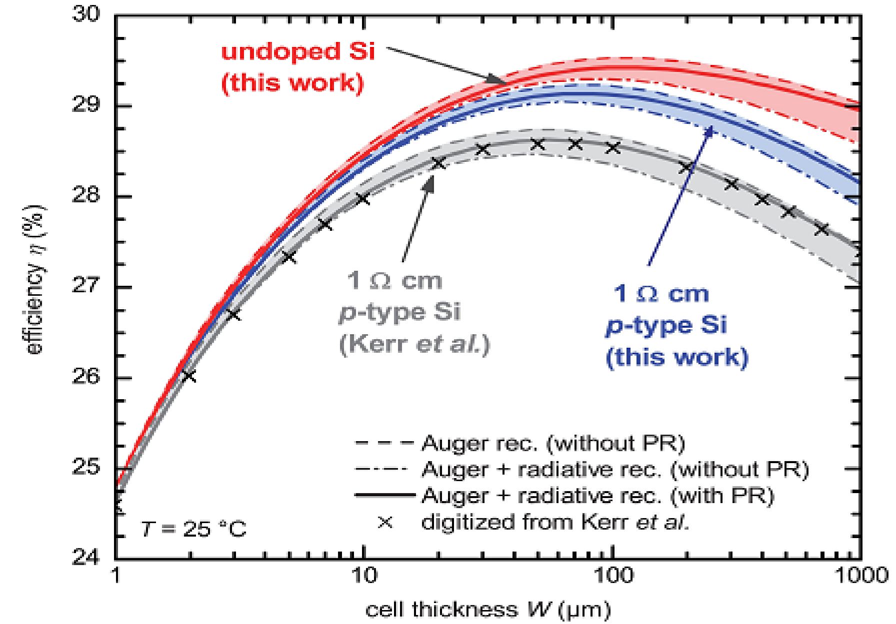
Photocurrent



Efficiency



Conclusion:

- dope as little as possible and reduce recombination volume (thin cells) !
- maximize j_{sc}

Then: η_{max}= 29.4-29.5%

On limiting jsc: e.g. Bozzola, EU-PVSEC (2011)
On limiting efficiency: Richter, JPV (2013),
Schäfer SEM (2018)
Niewelt, SEM (2022)

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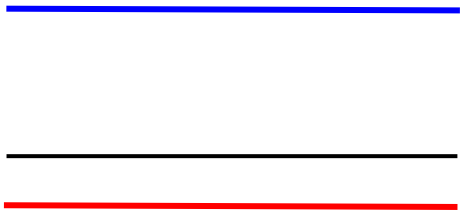
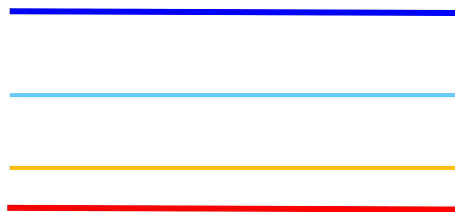
Impact of surfaces

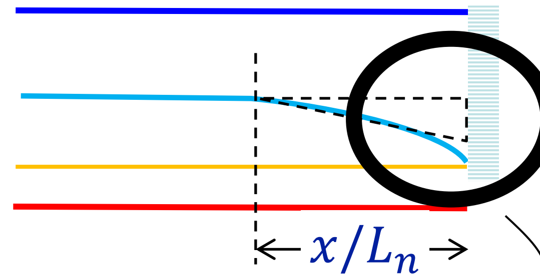
Equilibrium (p-type)



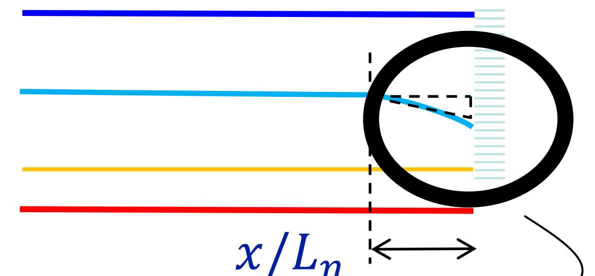
with illumination:
$p \approx p_0 \, , n \approx n_0 + \Delta n$



with $S \approx 10^5$ cm/s
(metal contact)



with $S \approx 10..100$ cm/s
(oxide passivation)

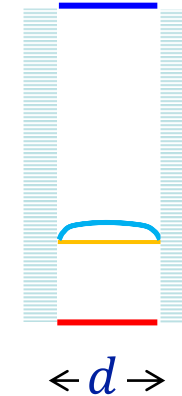


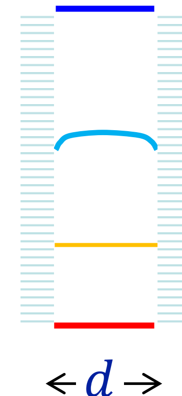
exponential decay from bulk to surface with $L_n = \sqrt{D_n \tau_n}$
in c-Si (τ_n = 1…10 ms): $L_n \approx$ 5 mm but $d \approx$ 150 µm

But: wafer thickness $d \approx$ 150 µm

$$\frac{1}{\tau_{eff}} = \frac{1}{\tau_n} + \frac{S}{2d}$$

=> surface recombination limits Δn and thus V_{oc}
=> for large L_n of c-Si, surface passivation is imperative

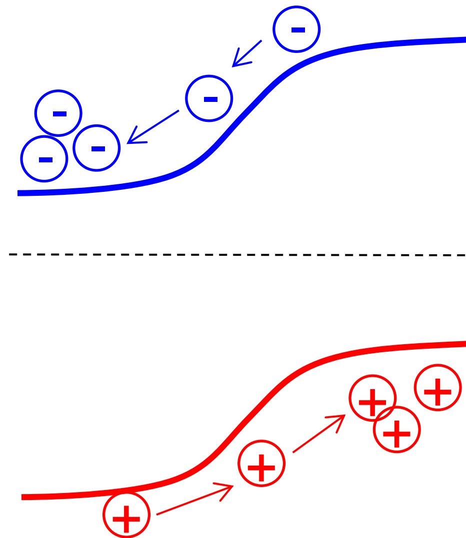




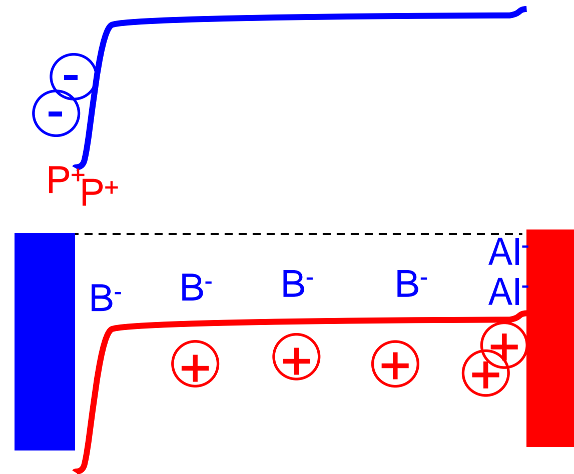
Sproul, JAP (1994)

How to get current out of the cell

What you often see…

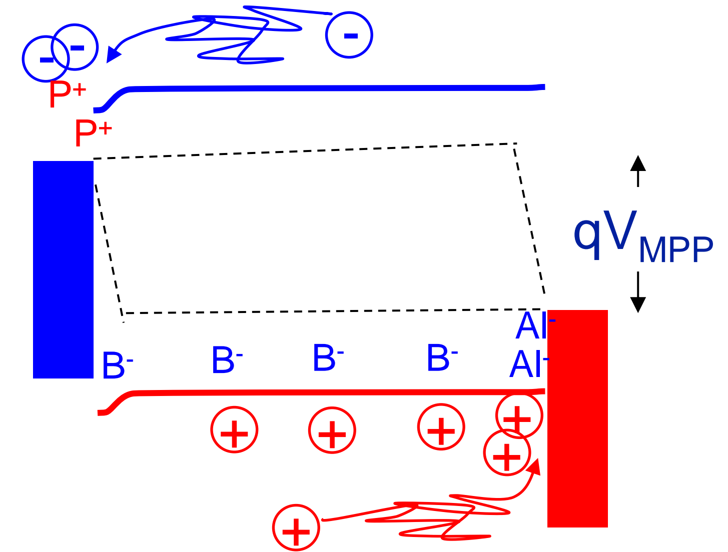


how it actually looks in dark



the field extends over <1µm, most of the 200 µm wafer is neutral

…and how it really works



charges diffuse randomly until they "see" a contact region (may be doped, but need not!)

Working principle of metallic contact, e.g. Al-Si:B

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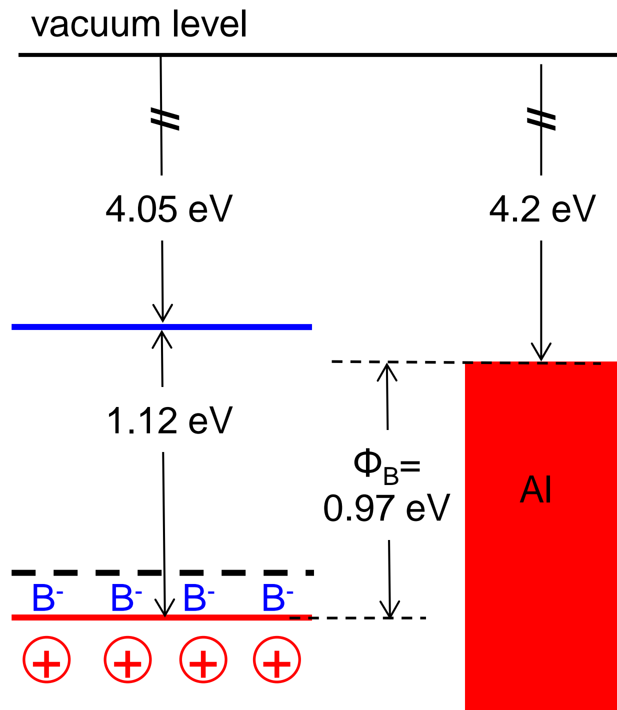
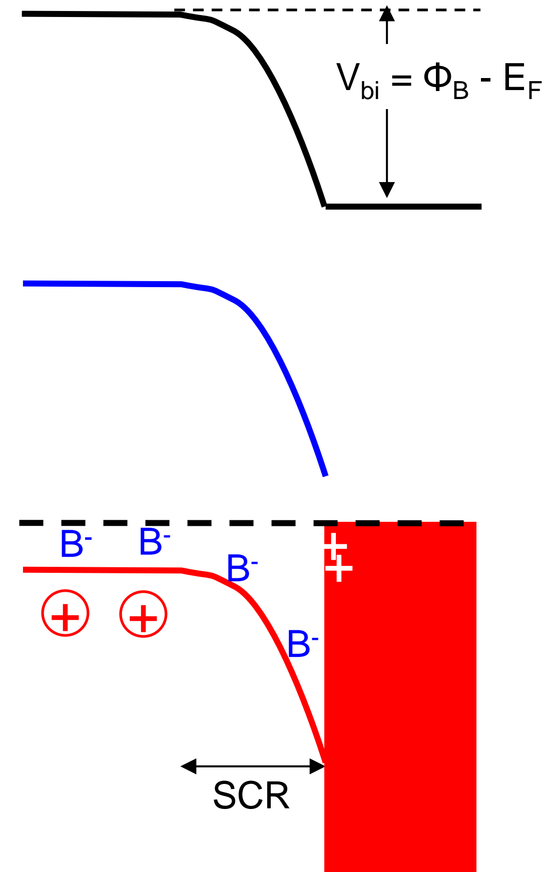
Before contact



Ideal Schottky contact



p-type contact with Fermi-level pinning

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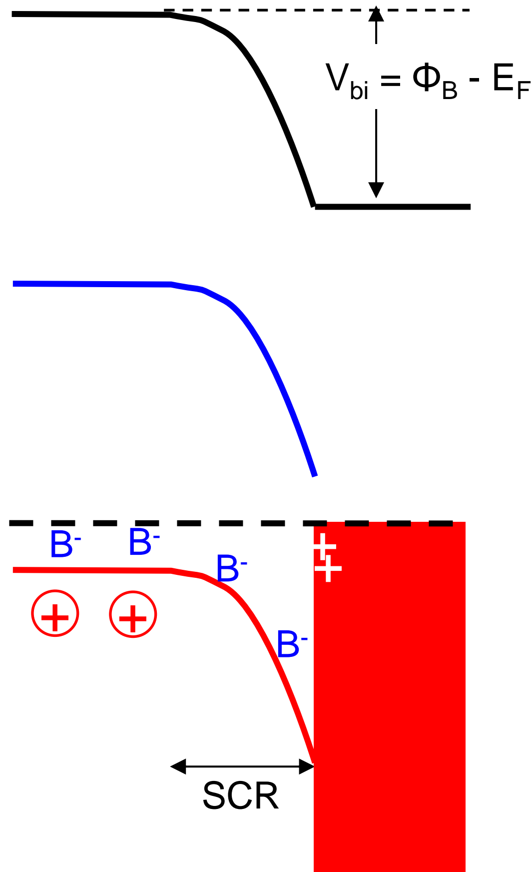
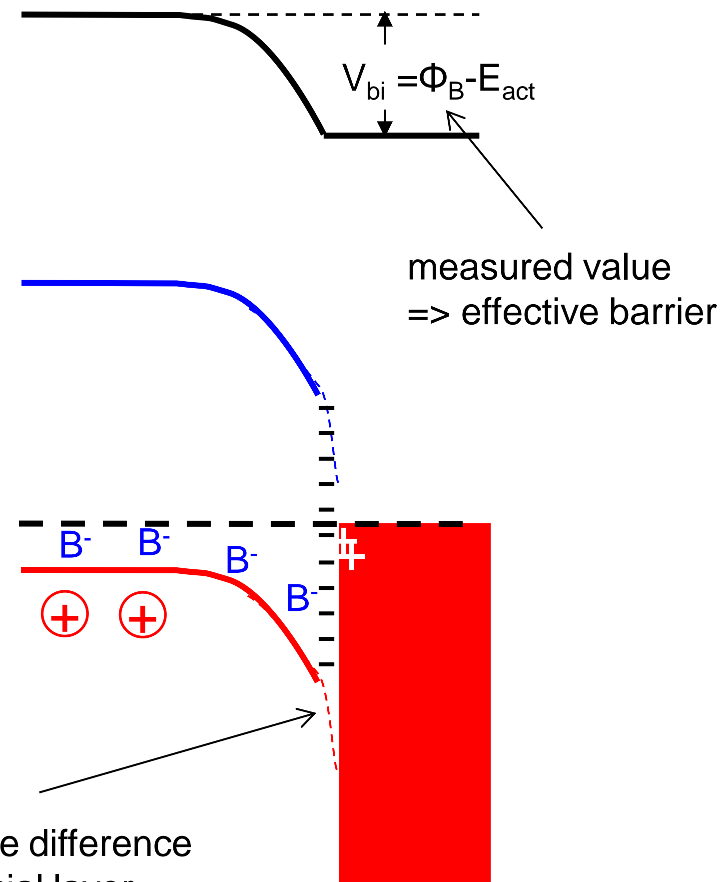
Ideal Schottky contact: Φ_B = 0.97 eV



Actually measured: Φ_B = 0.5 eV, difference due to interface states



see e.g. Schroeder, TED (1984)

Barrier heights (experimental)

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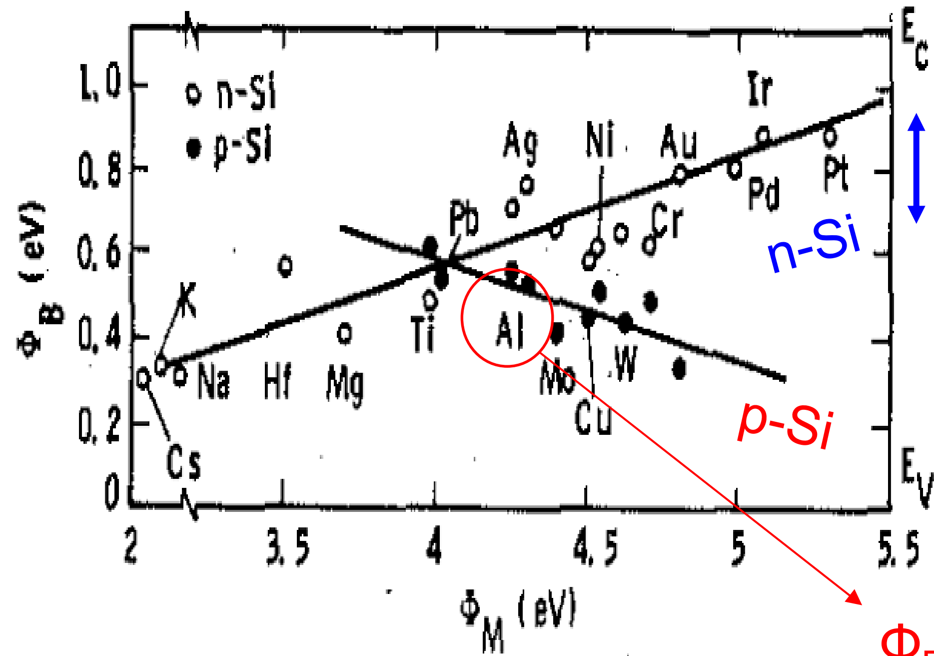
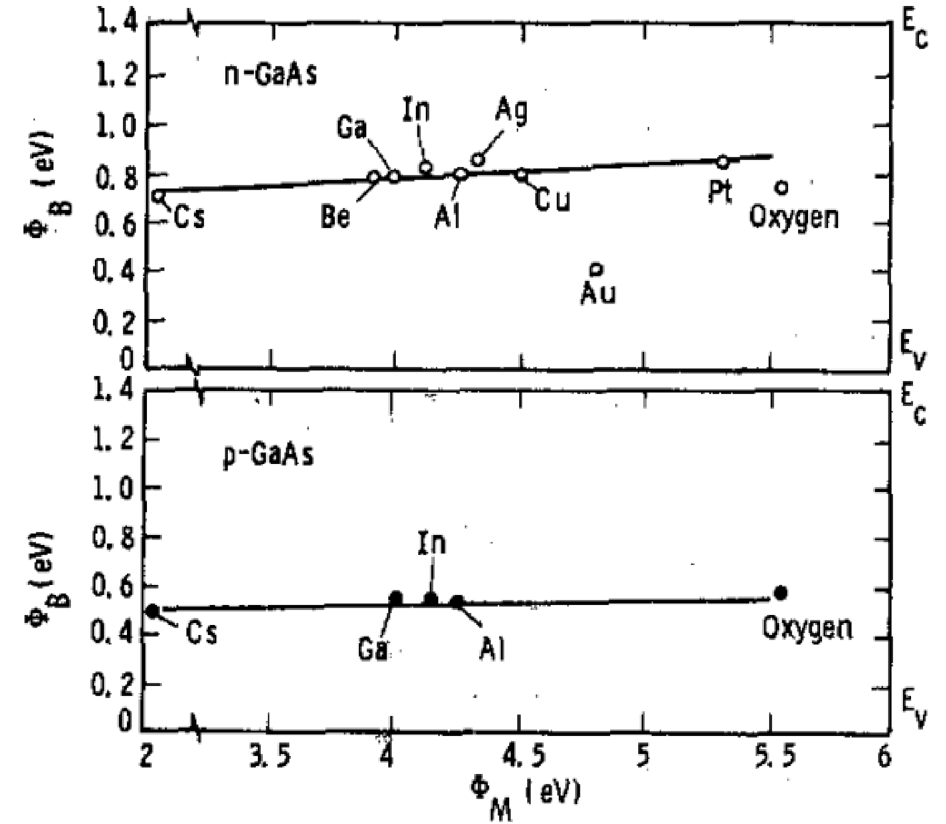


rule for common metals on n-Si $\Phi_B = 2/3$ of E_g, "E_F pinning"

$\Phi_{B,Al}$ = 0.5 eV (was 0.97 eV from work function)

Likewise: 1/3 rule for p-Si (referenced to VB edge)



Pinning even worse for GaAs

Schroeder, TED (1984)

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Minority recombination at metallic contacts

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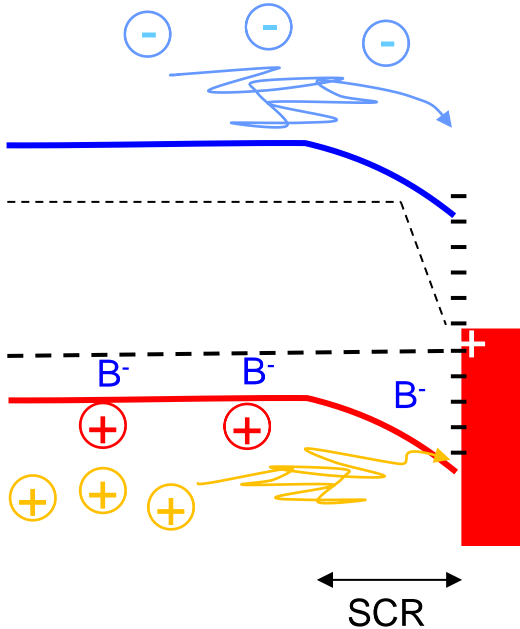
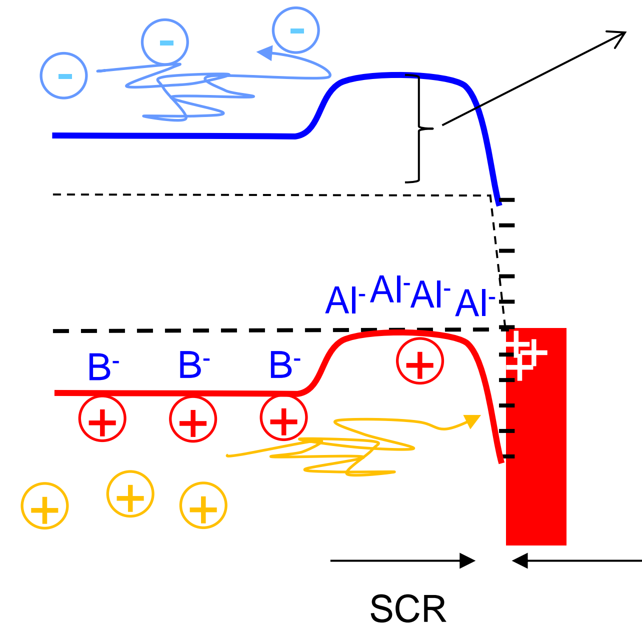
Remember contact from above, add QFL splitting



- electrons (minority) feel QFL gradient and easily recombine easily via interface states

Solution: introduce strongly doped region ("BSF")!



larger $E_C - E_F$ => fewer electrons for diffusion twds. interface

- electron density is reduced in BSF region
- added benefit: holes tunnel narrow barrier more easily (lower ρ_c)

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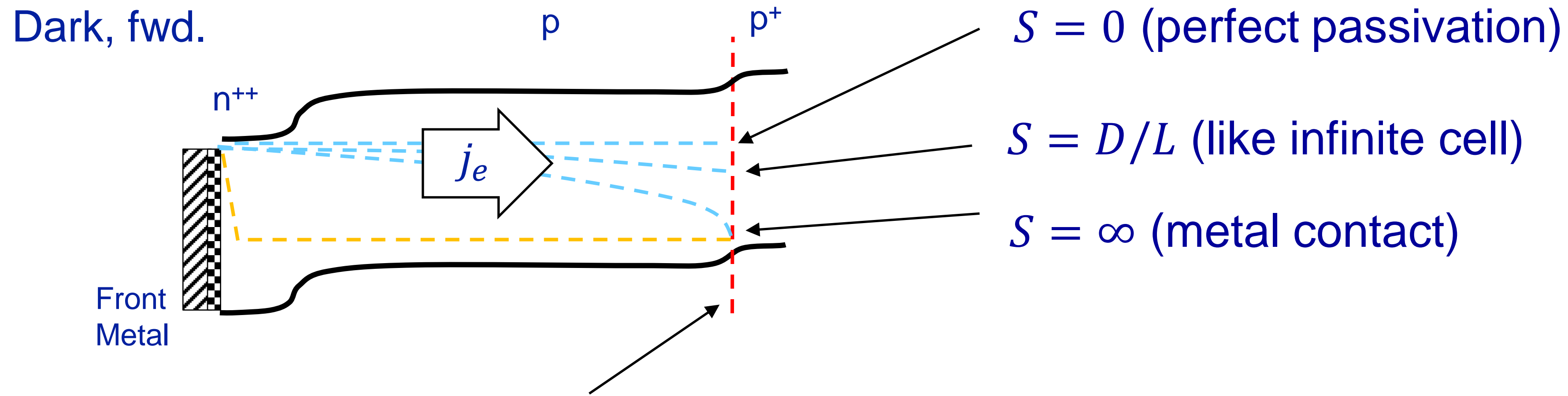
Surface recombination velocity

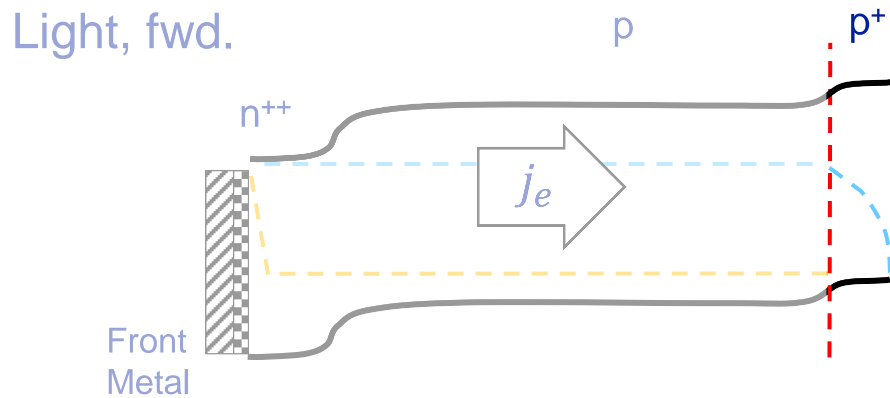


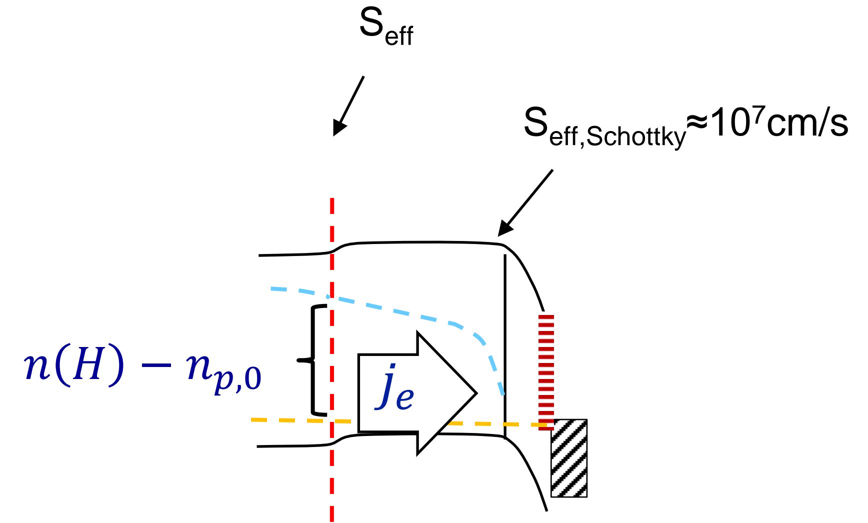
Ignore details of back contact, define
eff. surface recombination velocity S_{eff} by: $j(H) = qS_{eff}(n(H) - n_{p,0})$

$$j_{0,B} = \underbrace{\frac{qDn_i^2}{L_n N_A}}_{j_{0,p}^{\infty}} \cdot \underbrace{\frac{S \cdot \cosh H/L_n + D/L \cdot \sinh H/L_n}{S \cdot \sinh H/L_n + D/L \cdot \cosh H/L_n}}_{G_F \text{ (geometry factor)}}$$

S_{eff} ~ 300 cm/s for 1 Ohm cm material
S_{eff} ~ 500 cm/s for 2 Ohm cm

Back-surface field





Use same formalism as for p-n junction:

- minority carrier density fixed at virtual interface by bulk QFL splitting

$$j = qS_{eff}\Delta n$$

- injection into highly doped BSF region:

$$\Delta n = n_{p,0}\exp(qV/kt)$$

- From there again j_0 formalism with G_F, but:
  shorter lifetime, lower diffusivity, higher n_i, SRV of metal contact

=> Bulk properties cancel out

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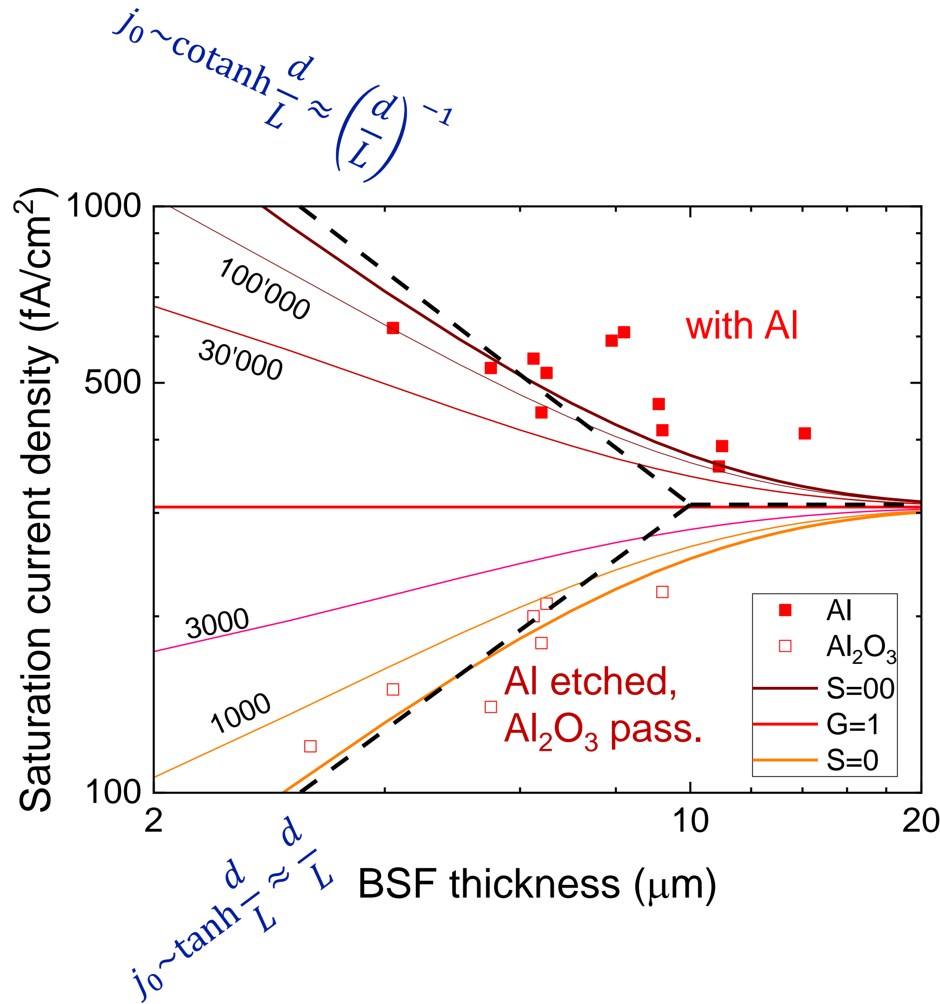
Example: Al-BSF



Approximate model for j_0:

- H = d_{BSF}
- N_A = const = $3x10^{18}/cm^3$ (Al saturation conc.)

Two branches:

- S ≈ ∞ (metal contact)
  => better for thick BSF
- S ≈ 0 (dielectric w. field effect)
  => better for thin BSF

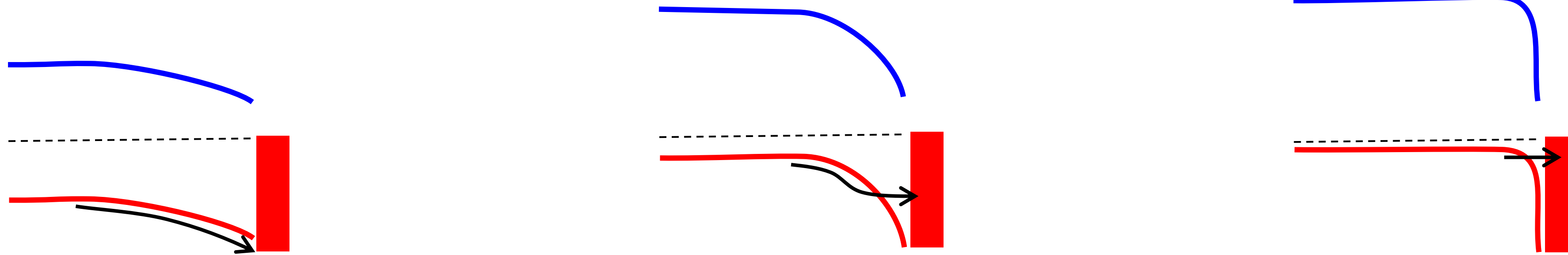
Data: Rüdiger, JAP (2011)

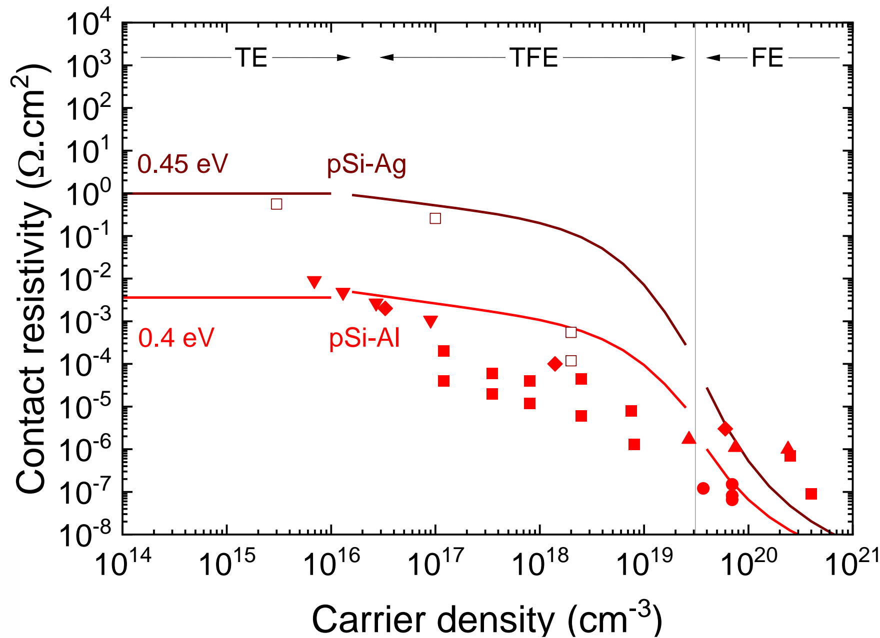
Contact resistance of a tunnelling contact

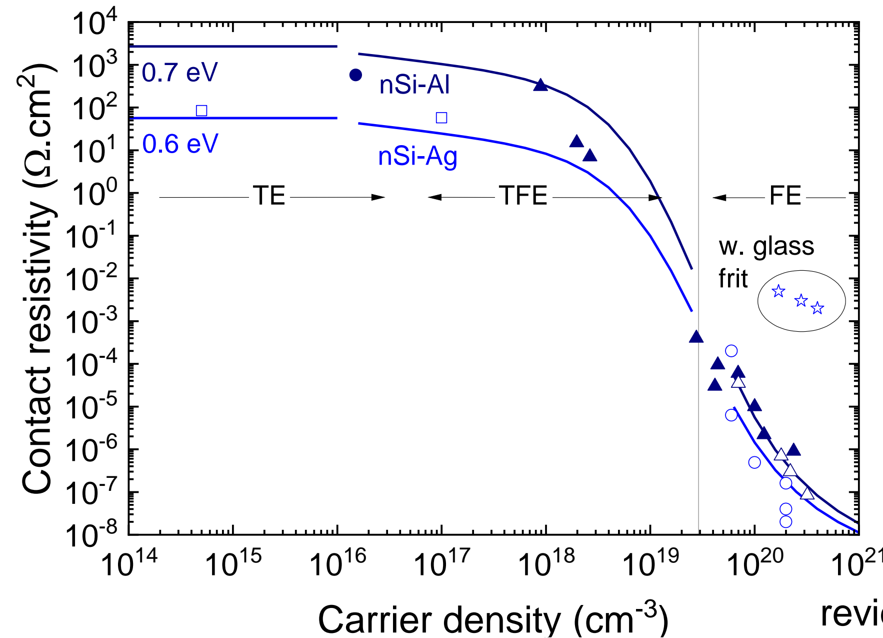
Weak doping:
thermionic emission
(TE, std. Schottky theory)

Intermediate:
thermionic field emission
(TFE)

High doping:
Field emission
(FE, tunnelling)







Padovani, SSE (1966)
Yu, SSE (1970)
review by: Schroeder, TED (1984)

Drawbacks of highly doped regions

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- Band gap narrowing by merging with adjacent band edge

  => enhanced recombination statistics (scales with $\exp\left\{-\frac{E_g-\Delta E_g}{kT}\right\}$)

- Inactive doping atoms

  clustering into dopant-defect pairs (esp. phosphorous)

  => yet more recombination

- Parasitic absorption

  absorption by free carrier plasma

One solution: precise control of doping density and location,
=> complicated process

Efficiency for given j_0 and j_{sc}

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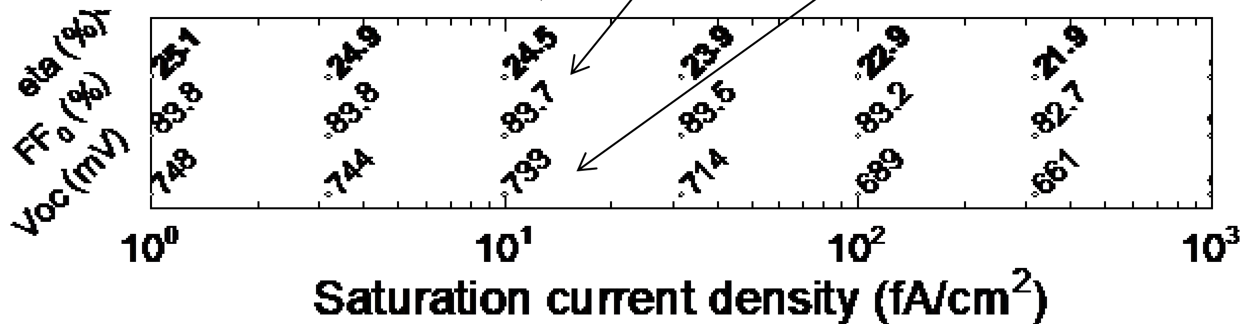
$$\eta_0 = V_{oc} \cdot FF_0 \cdot j_{Sc}$$

$$FF_0 = \frac{\frac{qV_{oc}}{kT} - \ln\left(\frac{qV_{oc}}{kT} + 0.72\right)}{\frac{qV_{oc}}{kT} + 1}$$

$V_{oc} = \frac{kT}{q} \ln \frac{j_{sc}}{j_0}$, assume $j_{sc} \approx 40 \text{ mA cm}^{-2}$



Approximation formulae: Green, SSC (1982)

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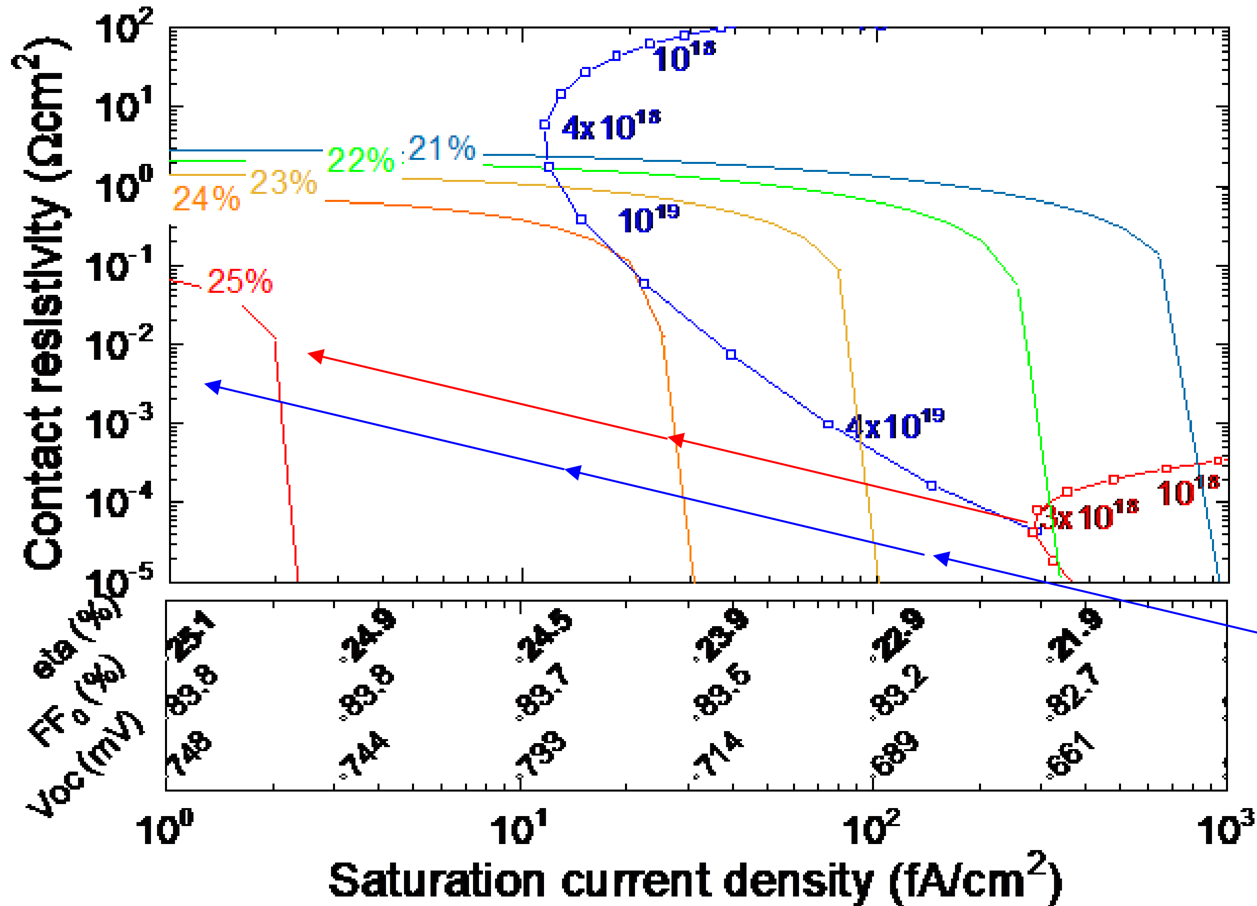
Combine ρ_c and j_0 for given j_{sc}



Efficiency contours with series resistance:

$$FF_s = FF_0\left(1 - 1.1\frac{R_s I_{sc}}{V_{oc}}\right) + \frac{\left(\frac{R_s I_{sc}}{V_{oc}}\right)^2}{5.4}$$

$$\eta = V_{oc} \cdot FF_S \cdot j_{sc}$$

BSF contact (10^{-12} A/cm², 10^{-4} Ωcm²) => 1% coverage

Ag front contact: needs higher N_{surf}, 0.1% eff. coverage

Green, SSC (1982)

Young, E. Proc. (2014)

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Architectures with improved passivation

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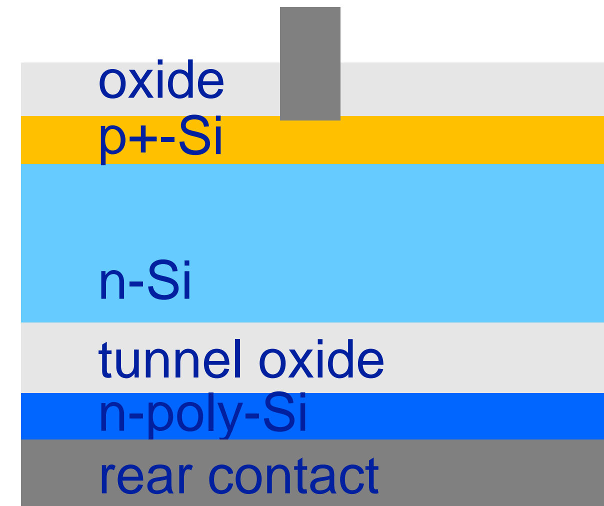
HIT (Hetero junction with Interlayer Technology): Voc = 740-750 mV

Taguchi, JPV (2014)

full area concept
chemical passivation by a-Si:H
contacts & field effect by doped a-Si:H
no direct contact btw. c-Si and metal!

TOPCon (Tunnel Oxide Passivating Contacts): Voc = 715 mV



Feldmann, SEM (2014)

full area back contact
chemical passivation by tunnel oxide

(probably used by SunPower as well)

c.f. Gan, Proc. IEEE PVSC (1990)

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a-Si:H passivating contacts

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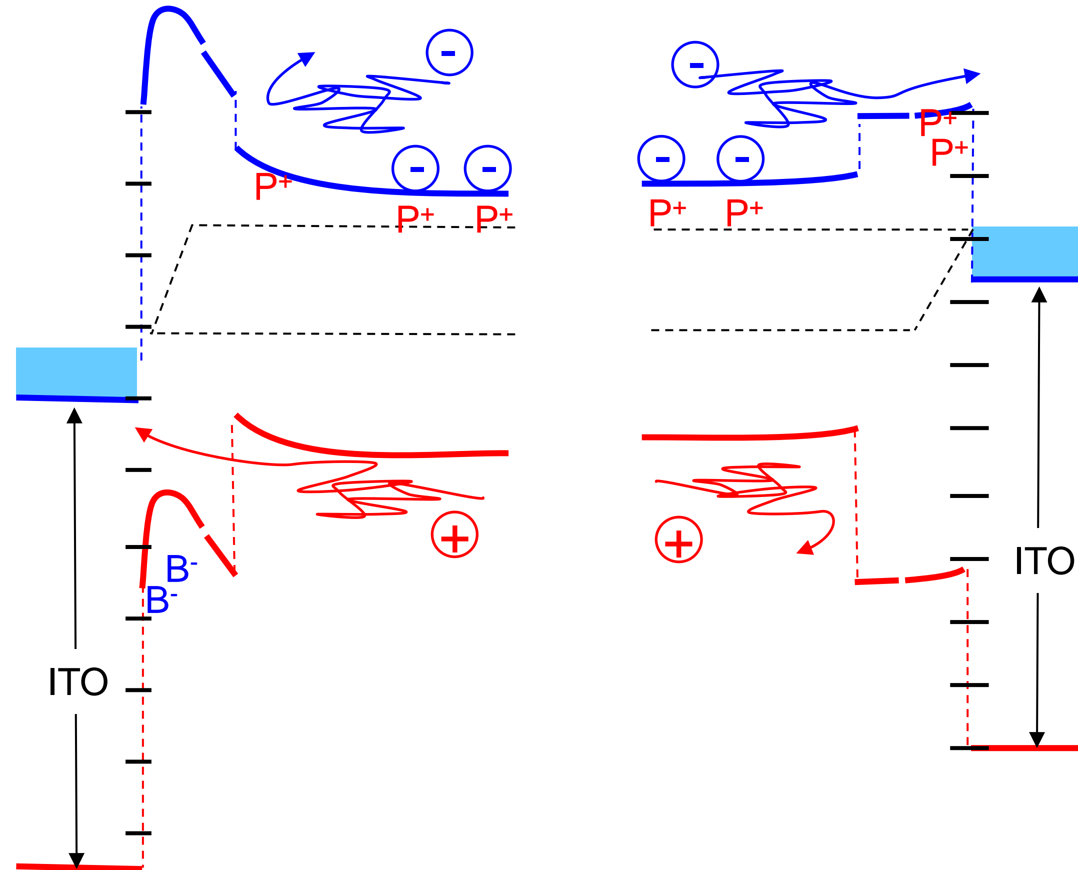
passivate interface states at c-Si surface with a-Si:H
VBO > CBO: efficient hole repulsion (minority carriers)
p-layer pulls wafer surface into inversion



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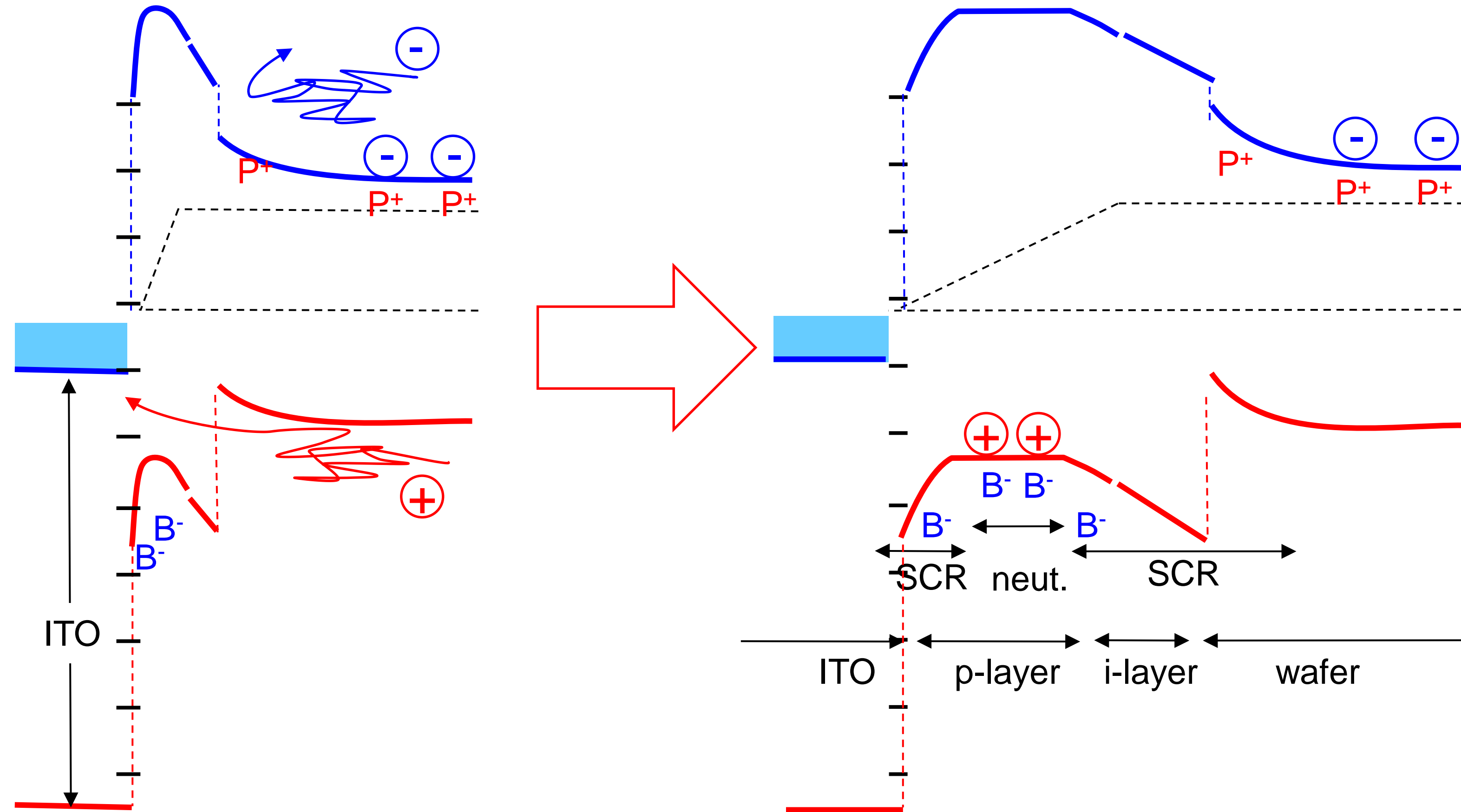
a-Si:H passivating contacts

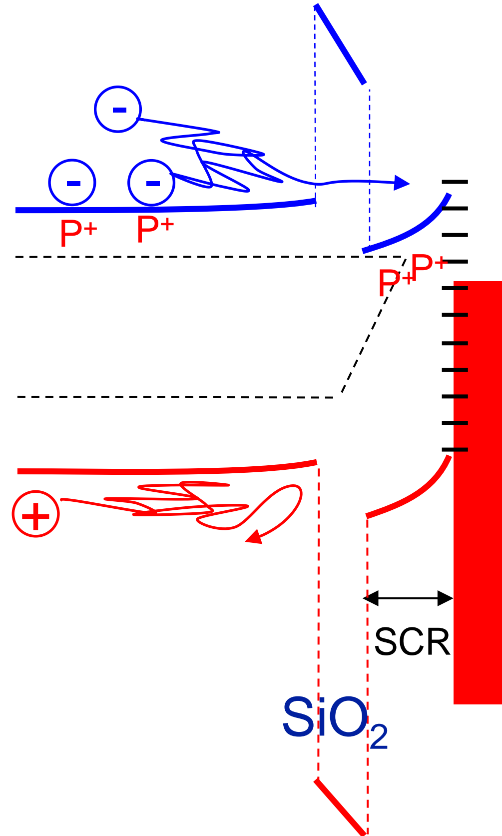
p-layer pulls wafer surface into inversion => p-n transition in defect-free wafer



SiO_2 passivating contacts

F.-J. Haug

SiO_2: VBO > CBO => slight preference for electron tunnelling, but works fine for p-contact with polycrystalline p-layer



BUT: needs ultra-thin tunnelling oxide (ca. 1 to 1.5 nm)

Gan, IEEE PVSC (1990)
Feldmann, SEM (2014)
Preibst, En. Proc. (2015)

Summary

- Apparent stagnation of efficiency (25% btw. 1999 and 2014)
- Continuous development of technology behind the scene
- Boost beyond 25% since 2014 along different lines
- Latest record efficiency: 28.1% by LONGI