

# Modern PV-Technologies

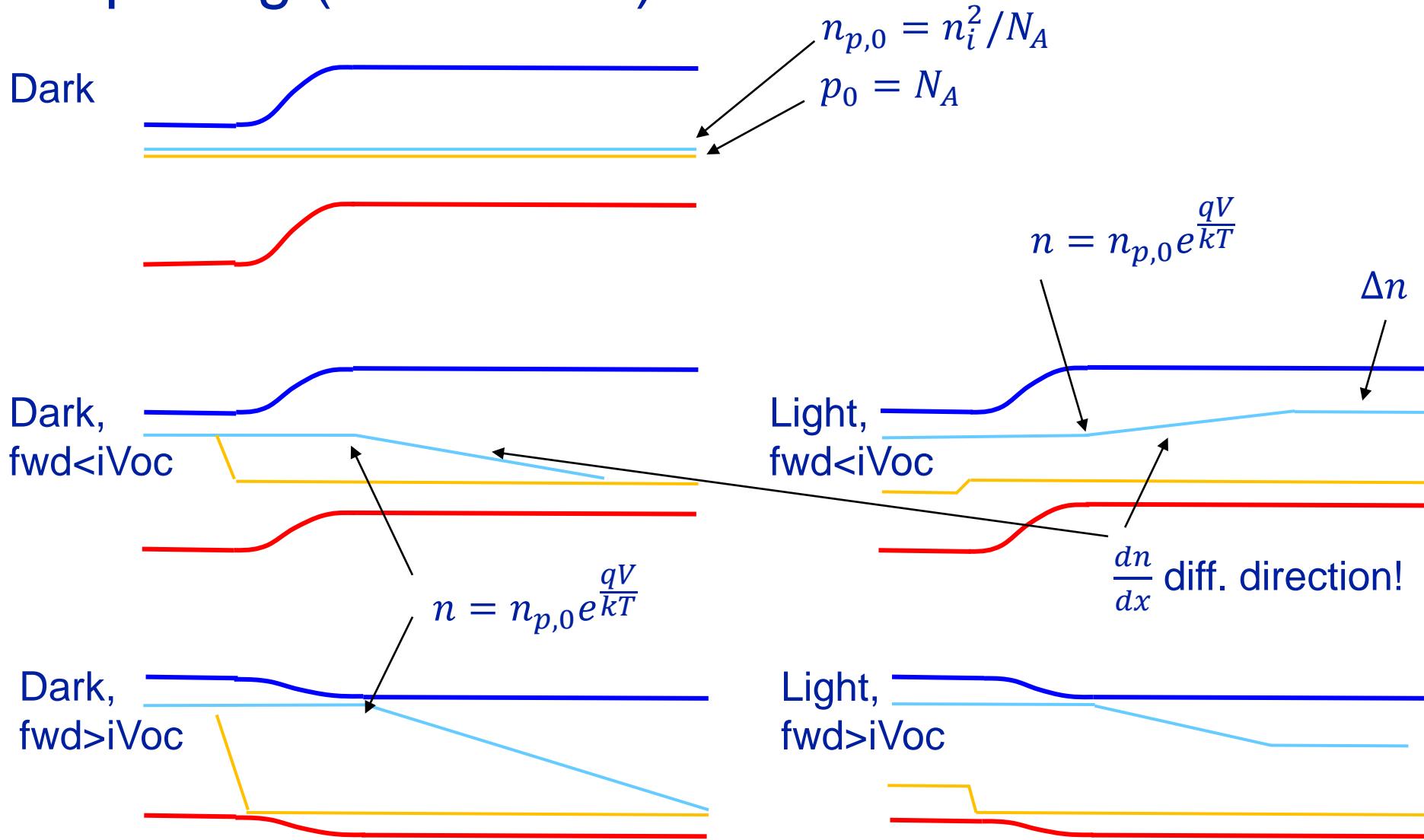
## 3.3: Junctions

F.-J. Haug

Ecole Polytechnique Fédérale de Lausanne  
PV-Lab

■ Modern PV – Junctions

# QFL splitting (infinite cell)



# Current-voltage characteristic

Simple form of j-V characteristics

$$j = j_0(e^{qV/kT} - 1) - j_{ph}$$

Short circuit current ( $V = 0$ ):

$$j_{sc} = j_{ph}$$

Open circuit voltage ( $j = 0$ ):

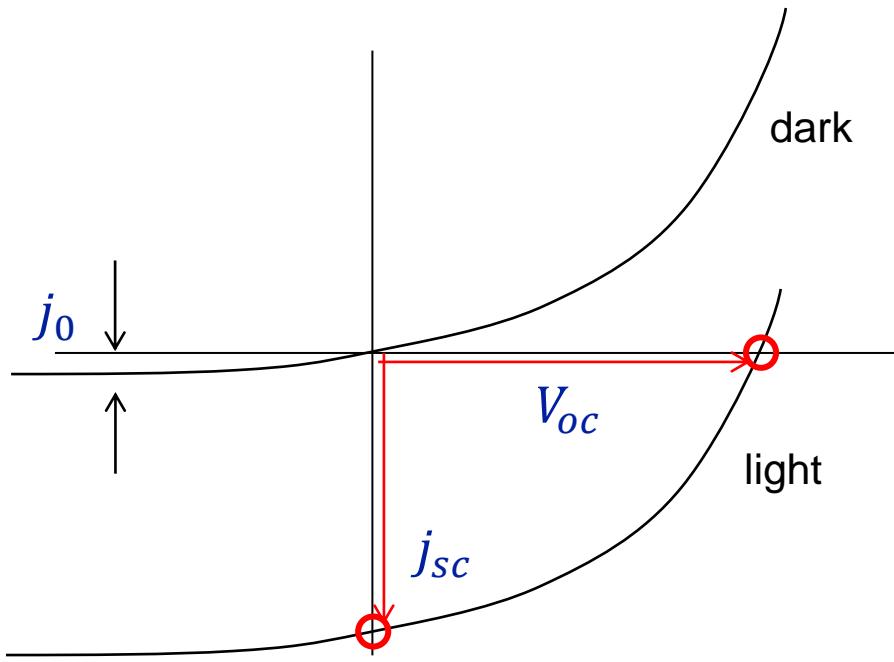
$$V_{oc} = \frac{kT}{q} \ln \left( \frac{j_{ph}}{j_0} + 1 \right)$$

Knobs to turn for high  $V_{oc}$ :

$kT/q$  is fixed by operating conditions (ambient to approx. +70°C)

$j_{sc}$  is fixed by solar irradiation; slight control via absorption enhancement

$j_0$  should be as small as possible



Ideal  $j_0$  for diffusion transport in infinite cell (almost valid for silicon):

$$j_0 = \left( \frac{qD_n n_i^2}{L_n N_A} + \frac{qD_p n_i^2}{L_p N_D} \right)$$

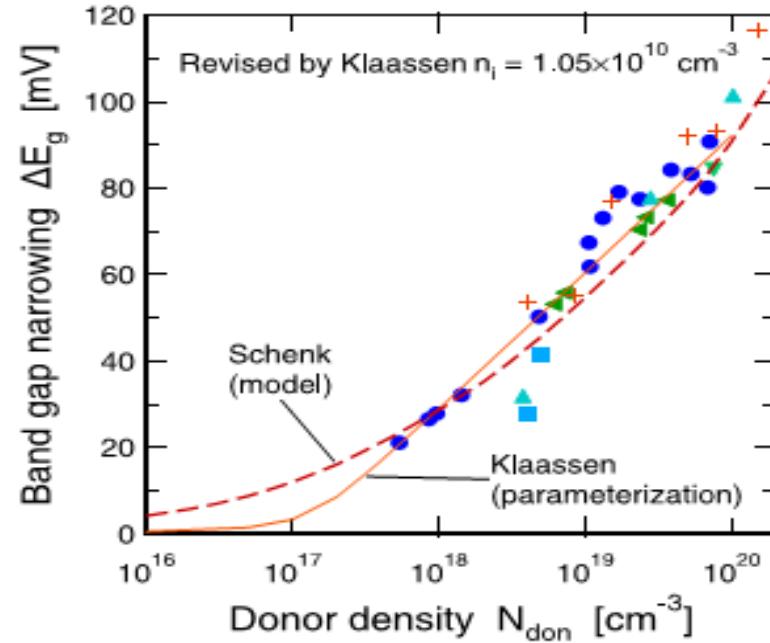
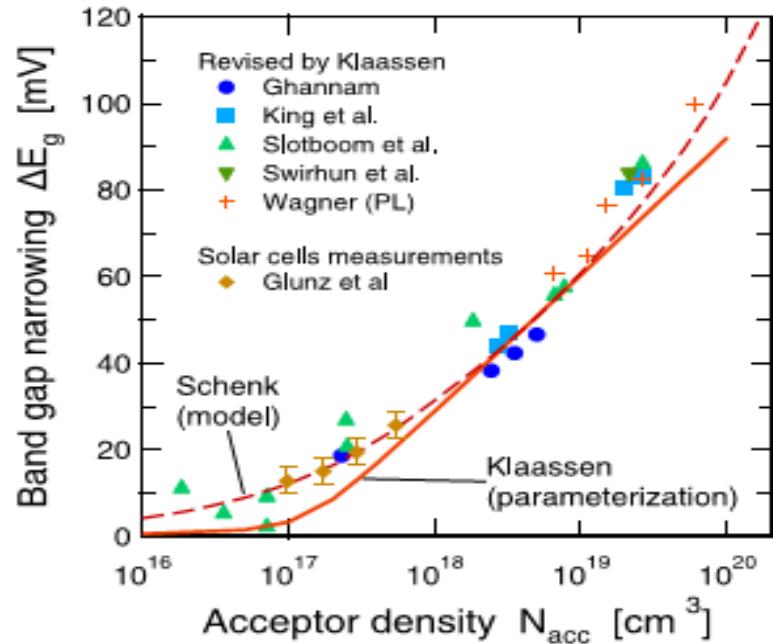
contribution of p-type absorber:

$$j_0 = \frac{qD_n n_i^2}{L_n N_A} = \frac{qn_i^2}{N_A} \cdot \sqrt{\frac{D_n}{\tau_n}}$$

Knobs to turn for small  $j_0$ :

increase  $N_A$  (but...)

## Band gap narrowing (BGN)

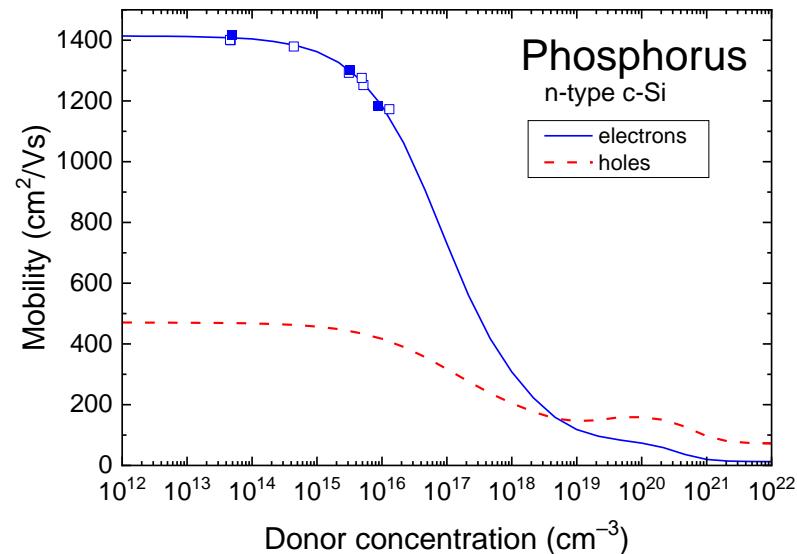
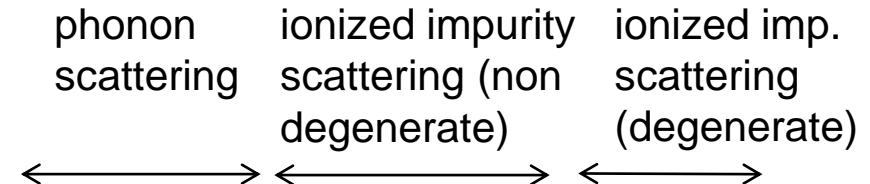
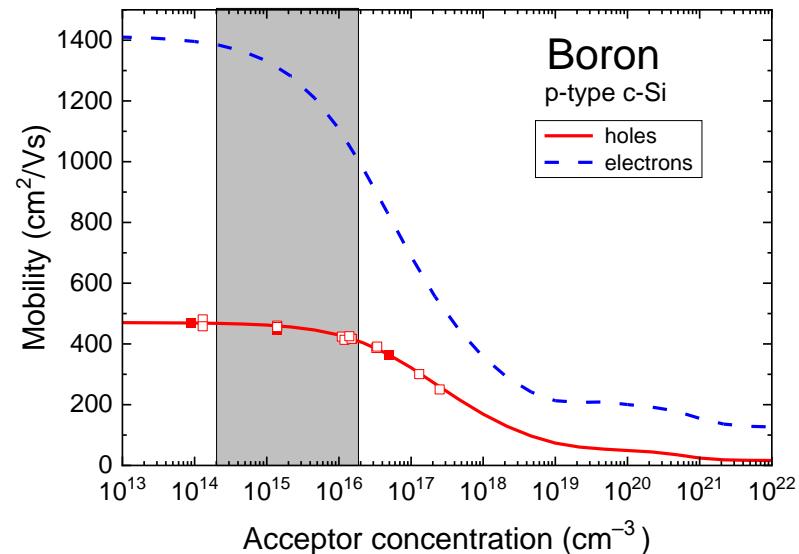


$$\text{Remember: } n_i^2 \sim e^{-\frac{E_g}{kT}} = e^{-\frac{E_{g,0}-\Delta E_g}{kT}}$$

On BGN models: e.g. Altermatt, J. Comput. Electron. (2011)

# Diffusion coefficient

$$\text{Einstein relation: } D = \mu \cdot \frac{kT}{q}$$

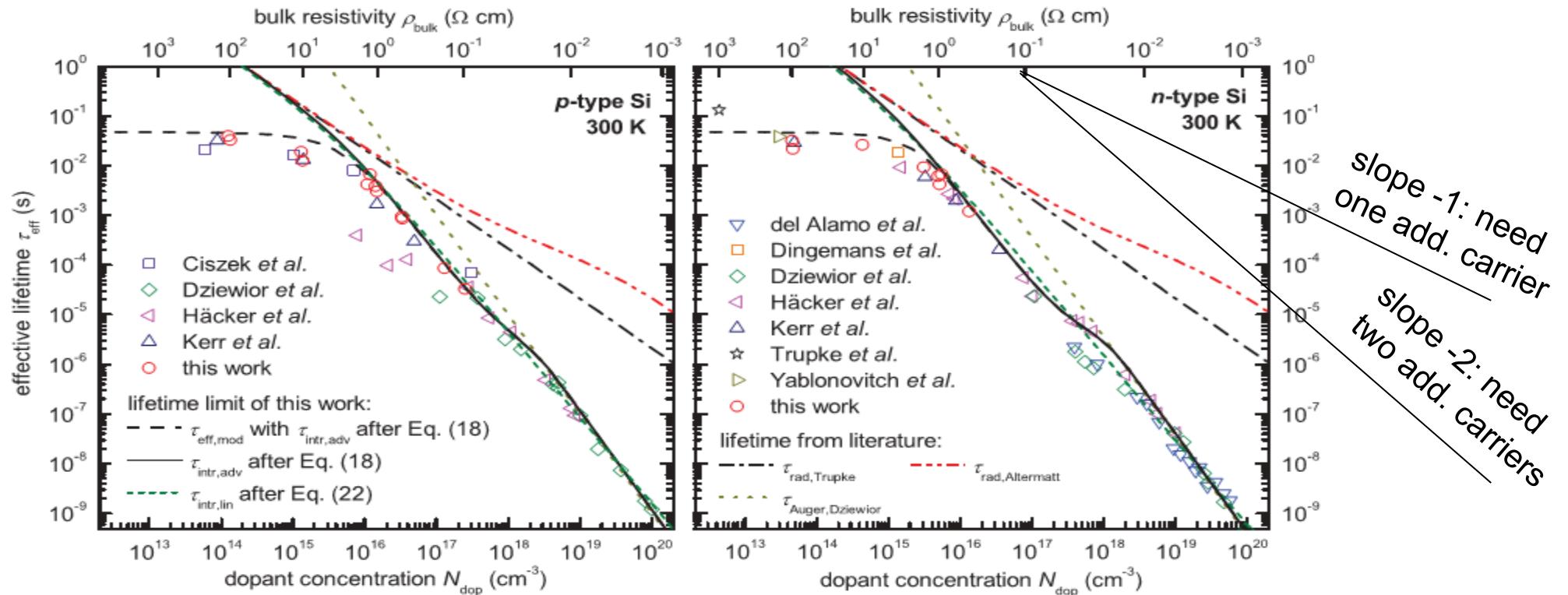


High doping will decrease  $D$  (both majority and minority, but slightly differently)

Majority mobility: Thurber, JECS (1980, 1981)  
 Minority mobility: Swirhun, TED (1986)

# Minority carrier lifetime

$$\tau^{-1} = \tau_{Auger}^{-1} + \tau_{rad}^{-1} + \tau_{bulk}^{-1}$$



High doping will also decrease  $\tau$ !

reviews on Auger-limited lifetimes: Kerr, PPV (2003)  
Richter, PRB (2012)  
Niewelt, SEM (2022)

# Steady state minority carrier density – QFL splitting

Recombination rate:  $R = \Delta n / \tau$

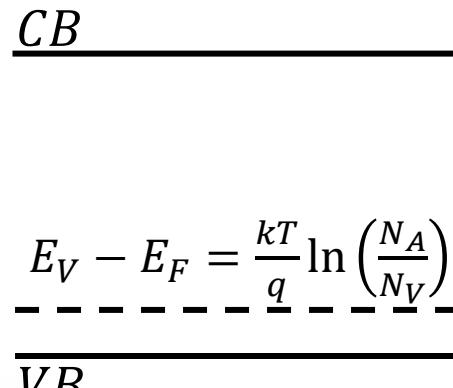
When no carriers are extracted (e.g. semiconductor w/o contacts or solar cell at  $V_{oc}$ ):  
 $\Rightarrow$  Recombination rate  $R = \text{Optical generation rate } G$

$\Delta n = G\tau$  (excess minority carrier density in steady state)

Dark:  
thermal equilibrium,  
unique Fermi level

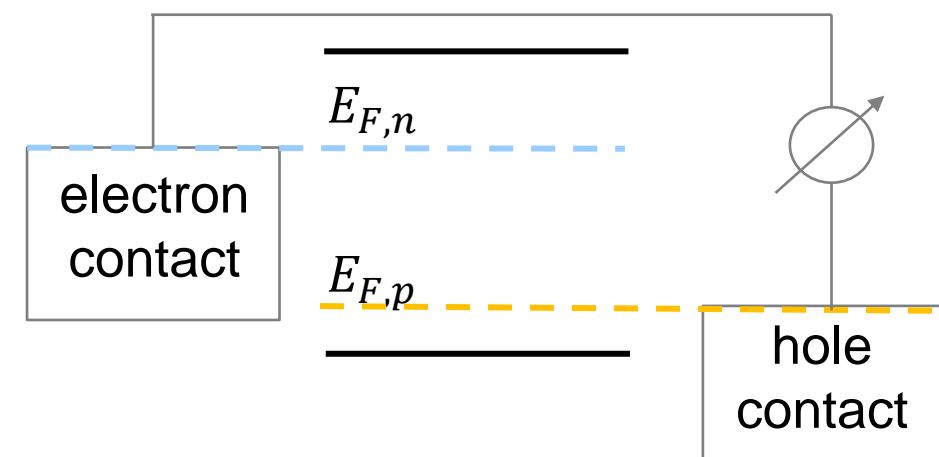
Illuminated:  
Define independent  
quasi Fermi levels (QFLs)

With idealized contacts:  
QFL splitting equal to  
achievable voltage



$$E_{F,n} - E_C = \frac{kT}{q} \ln \left( \frac{n_0 + \Delta n}{N_C} \right)$$

$$E_V - E_{F,p} = \frac{kT}{q} \ln \left( \frac{p_0 + \Delta n}{N_V} \right)$$



For ideal contacts: QFL splitting equal to external voltage

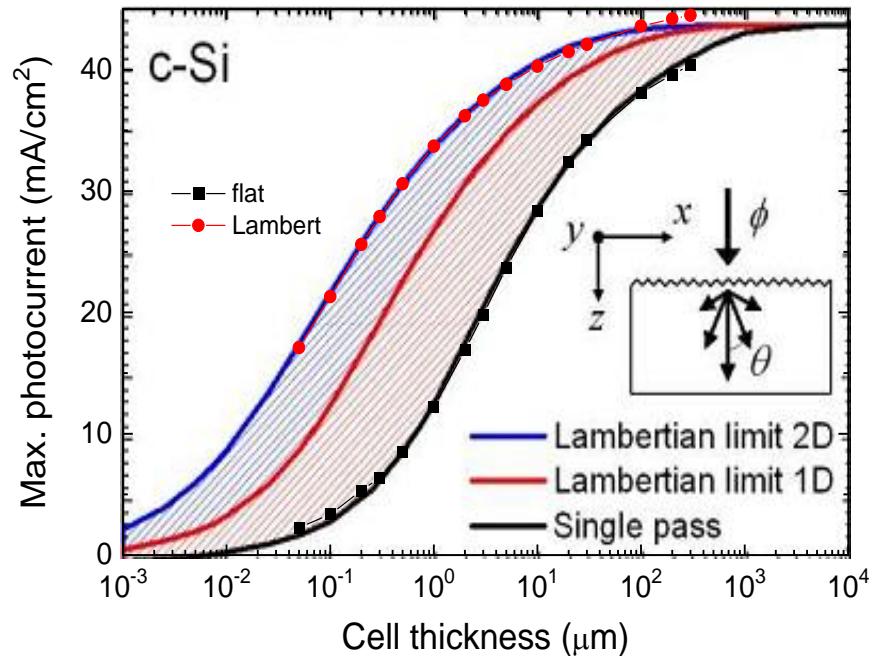
Assume

- $N_A = 10^{16} \text{ cm}^{-3}$  ( $= p_0$ )
- $G \approx 10^{19} \text{ cm}^{-3}\text{s}^{-3}$
- $\tau \approx 1 \text{ ms}$  (minority carrier lifetime)

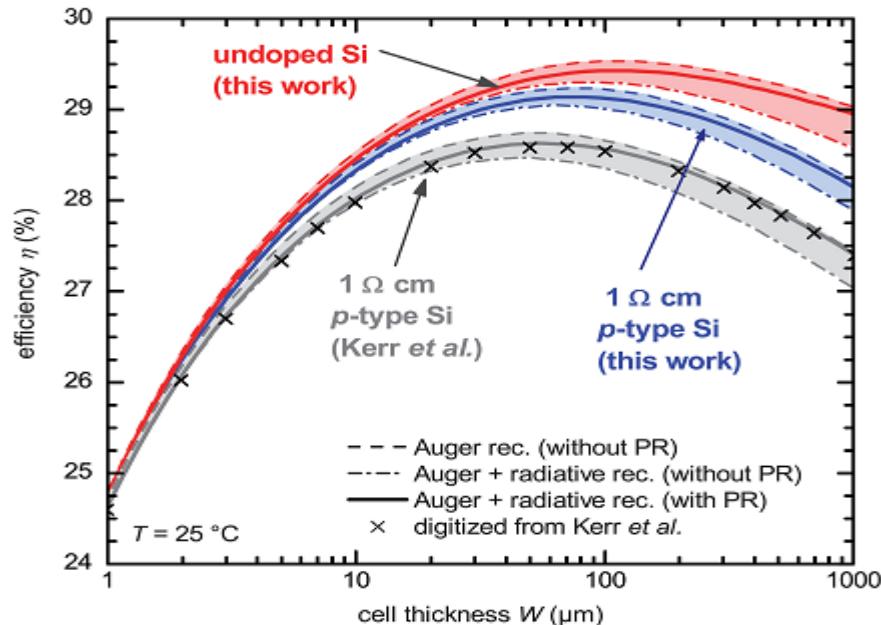
$$\Delta n = G\tau \approx 10^{16} \text{ cm}^{-3}$$

$$iV_{oc} = \frac{kT}{q} \ln \frac{np}{n_i^2} \approx 720 \text{ mV}$$

## Photocurrent



## Efficiency



## Conclusion:

- dope as little as possible and reduce recombination volume (thin cells) !
- maximize  $j_{sc}$

Then:  $\eta_{max} = 29.4\text{-}29.5\%$

On limiting  $j_{sc}$ : e.g. Bozzola, EU-PVSEC (2011)

On limiting efficiency: Richter, JPV (2013),  
Schäfer SEM (2018)  
Niewelt, SEM (2022)

# EPFL Impact of surfaces

Equilibrium (p-type)

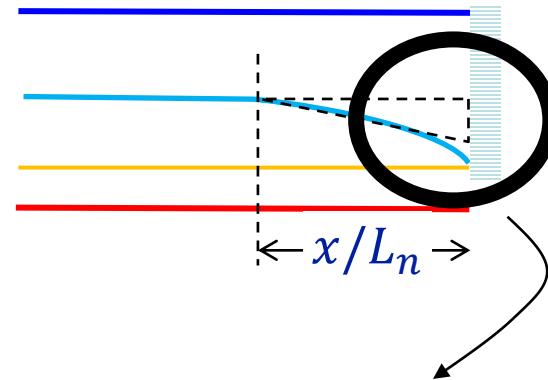


with illumination:

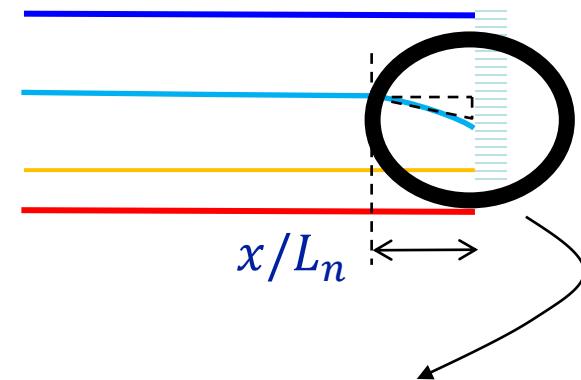
$$p \approx p_0, n \approx n_0 + \Delta n$$



with  $S \approx 10^5 \text{ cm/s}$   
(metal contact)



with  $S \approx 10..100 \text{ cm/s}$   
(oxide passivation)



exponential decay from bulk to surface with  $L_n = \sqrt{D_n \tau_n}$   
in c-Si ( $\tau_n = 1..10 \text{ ms}$ ):  $L_n \approx 5 \text{ mm}$  but  $d \approx 150 \mu\text{m}$

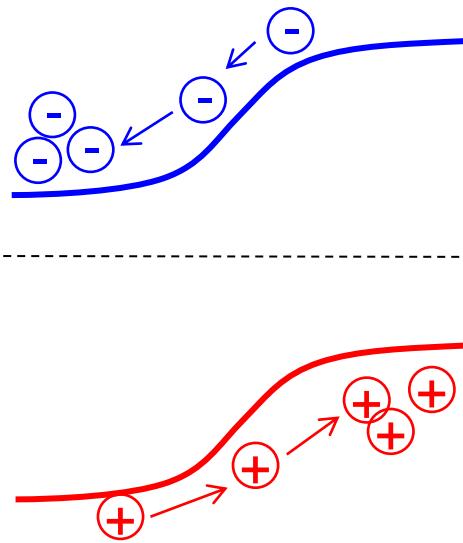
But: wafer thickness  $d \approx 150 \mu\text{m}$

$$\frac{1}{\tau_{eff}} = \frac{1}{\tau_n} + \frac{S}{2d}$$

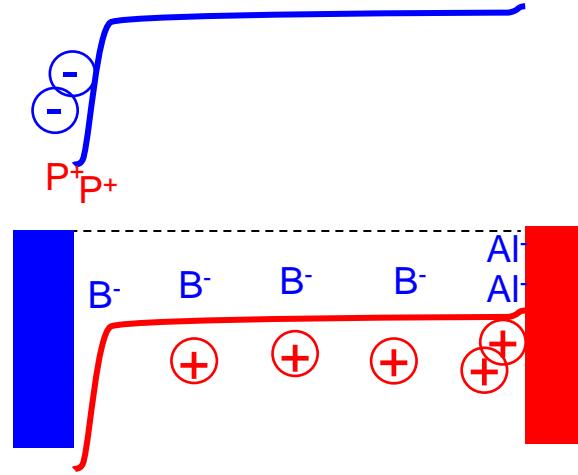
- => surface recombination limits  $\Delta n$  and thus  $V_{oc}$
- => for large  $L_n$  of c-Si, surface passivation is imperative

# How to get current out of the cell

What you often see...

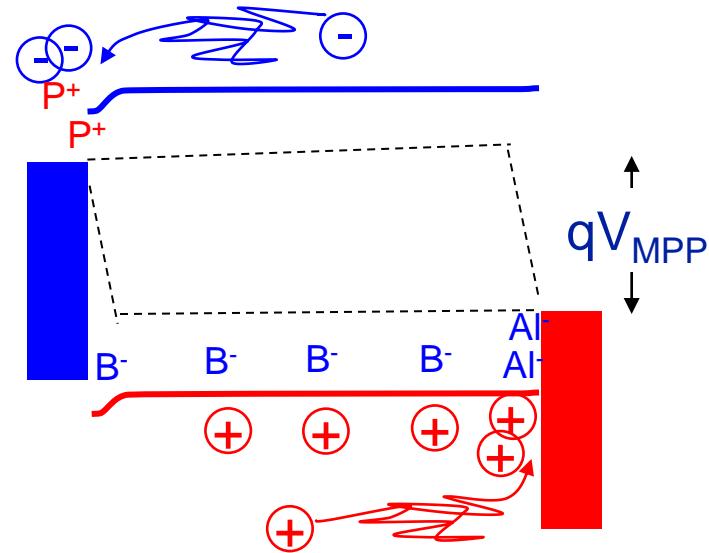


... how it actually looks in dark



the field extends over  
<1 $\mu$ m, most of the  
200  $\mu$ m wafer is neutral

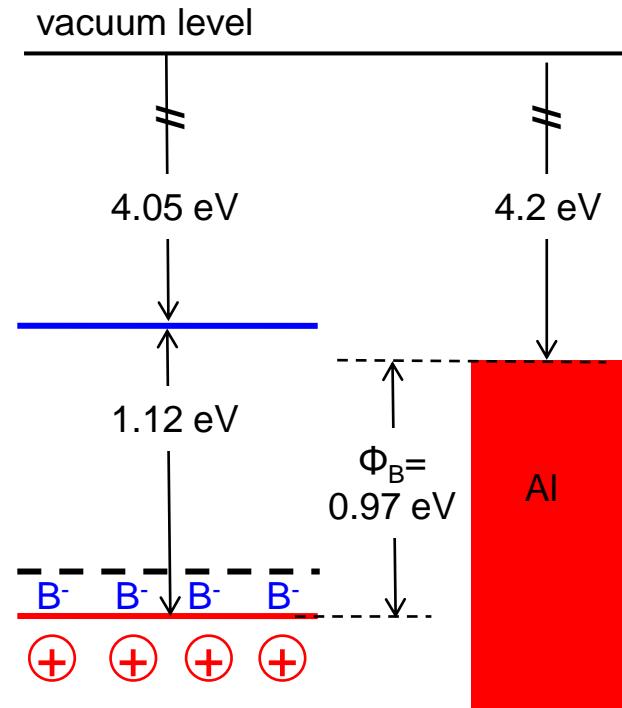
...and how it really works



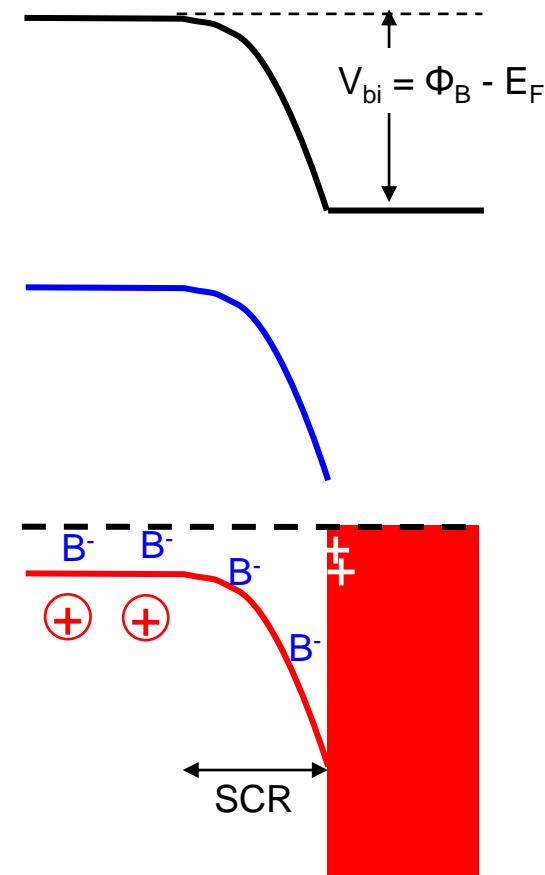
charges diffuse randomly  
until they “see” a contact region  
(may be doped, but need not!)

# Working principle of metallic rear contact

Before contact

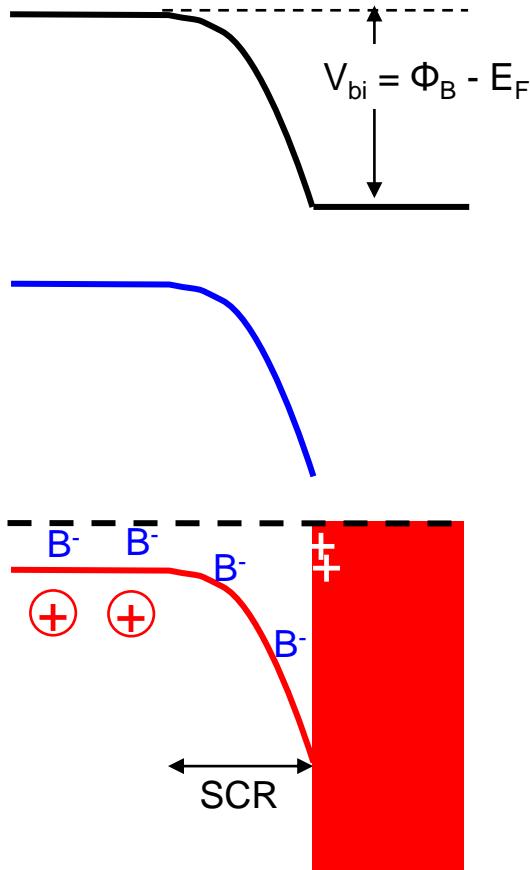


Ideal Schottky contact

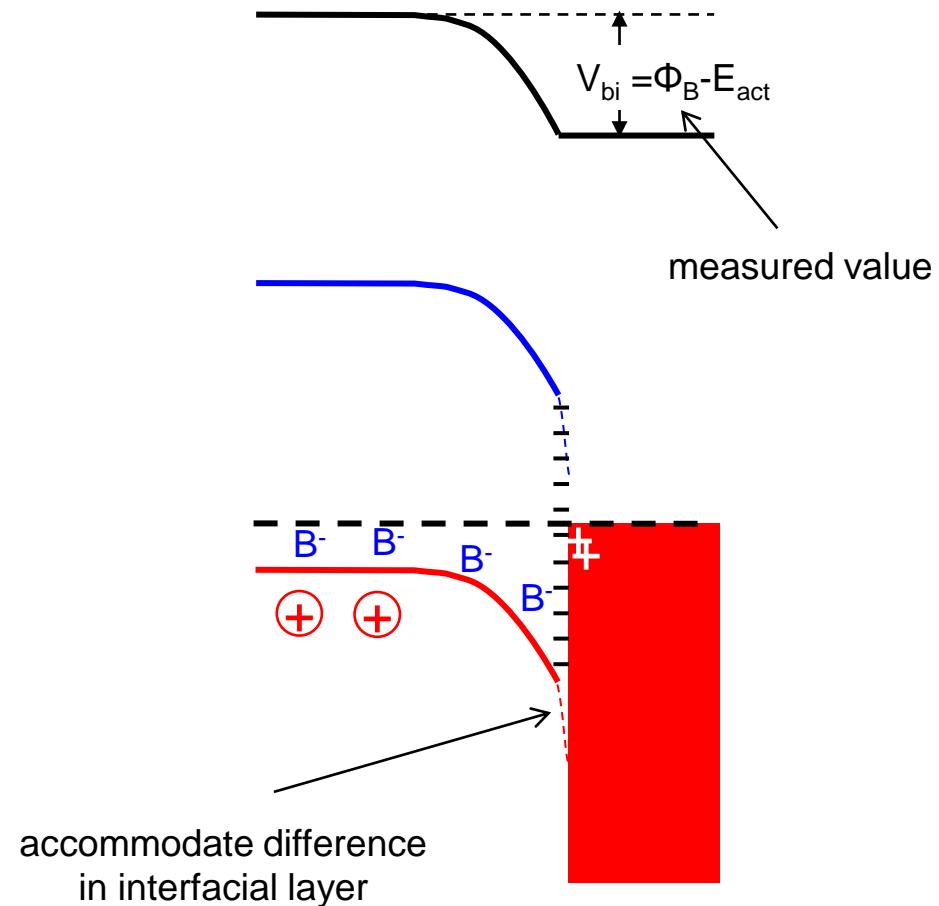


# p-type contact with Fermi-level pinning

Ideal Schottky contact:  $\Phi_B = 0.97 \text{ eV}$

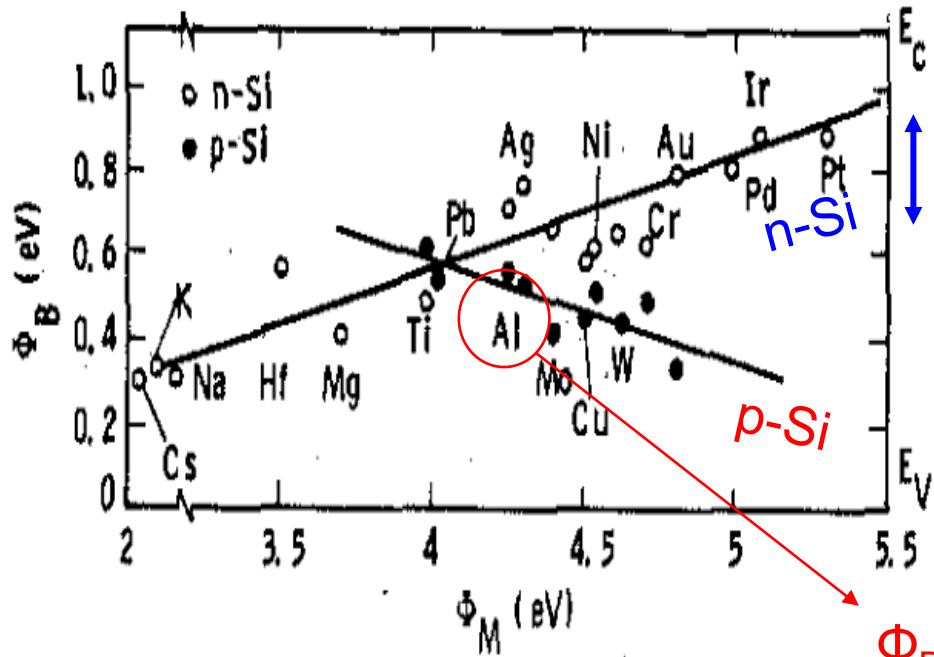


Actually measured:  $\Phi_B = 0.5 \text{ eV}$ , difference due to interface states



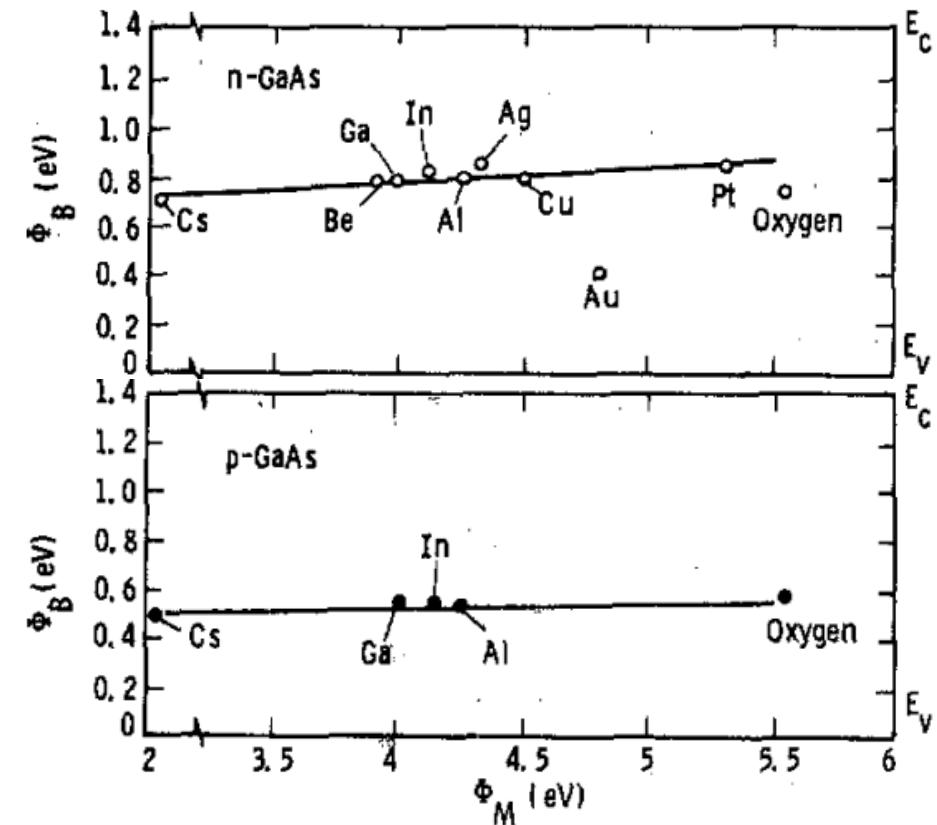
see e.g. Schroeder, TED (1984)

# Barrier heights (experimental)



rule for common metals on n-Si  
 $\Phi_B = 2/3$  of  $E_g$ , "E<sub>F</sub> pinning"  
 $\Phi_{B,Al} = 0.5$  eV  
(was 0.97 eV from work function)

Likewise: 1/3 rule for p-Si (referenced to VB edge)



Pinning even worse for GaAs

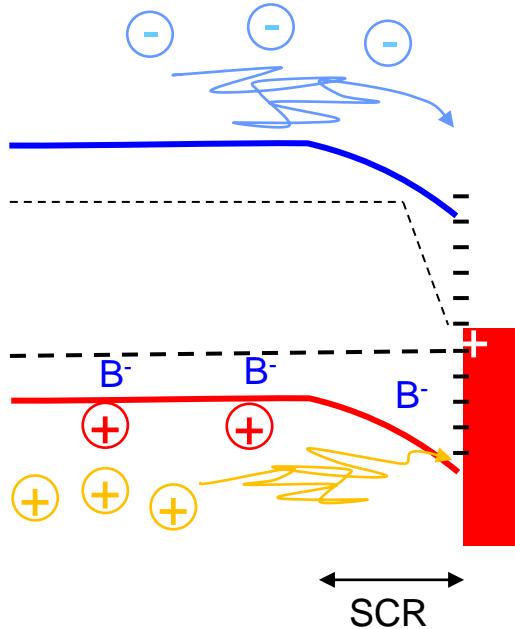
Schroeder, TED (1984)

# EPFL Minority recombination at metallic contacts

18

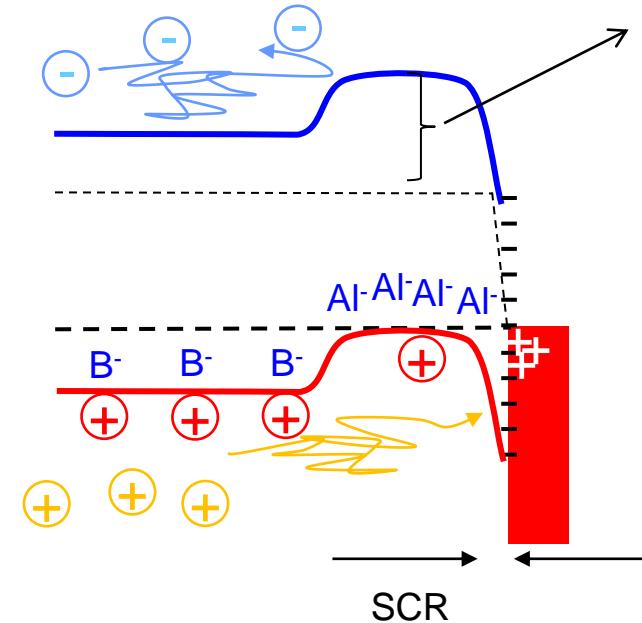
F.-J. Haug

Remember contact from above,  
add QFL splitting



- electrons (minority) feel QFL gradient and easily recombine easily via interface states

Solution: introduce strongly doped region ("BSF")!

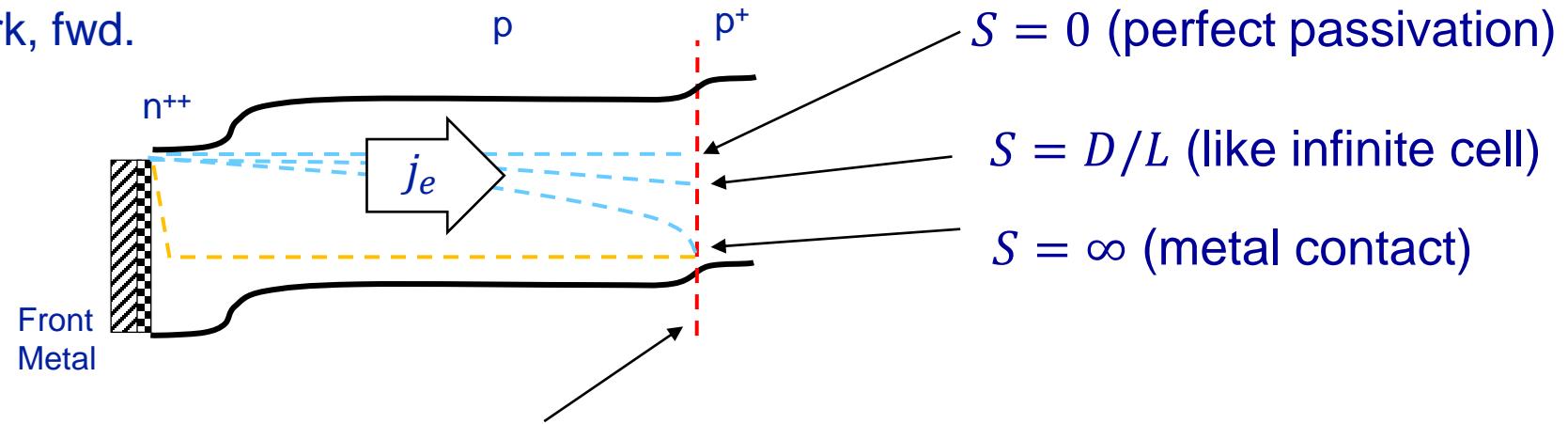


larger  $E_C - E_F$   
=> fewer electrons  
can diffuse to the  
interface

- electron density is reduced in BSF region
- added benefit: holes tunnel narrow barrier more easily (lower  $\rho_c$ )

# Surface recombination velocity

Dark, fwd.



Ignore details of back contact, define  
eff. surface recombination velocity  $S_{eff}$  by:  $j(H) = qS_{eff}(n(H) - n_{p,0})$

$$j_{0,B} = \frac{qDn_i^2}{L_n N_A} \cdot \frac{S \cdot \cosh H/L_n + D/L \cdot \sinh H/L_n}{S \cdot \sinh H/L_n + D/L \cdot \cosh H/L_n}$$

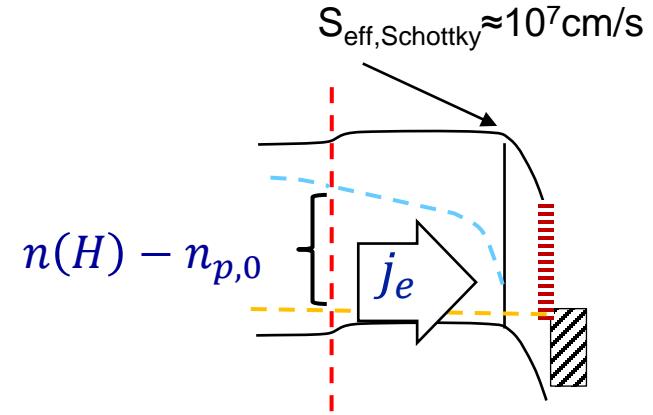
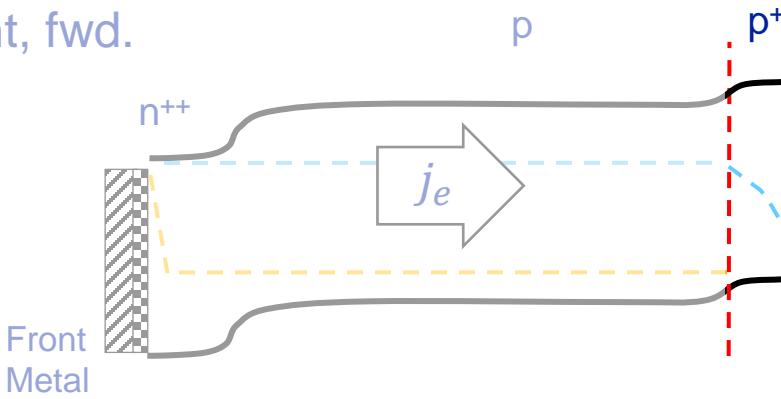
$\underbrace{j_{0,p}^\infty}_{\text{geometry factor}} \quad \underbrace{G_F}_{\text{(geometry factor)}}$

$S_{eff} \sim 300 \text{ cm/s}$  for 1 Ohm cm material

$S_{eff} \sim 500 \text{ cm/s}$  for 2 Ohm cm

# Back-surface field

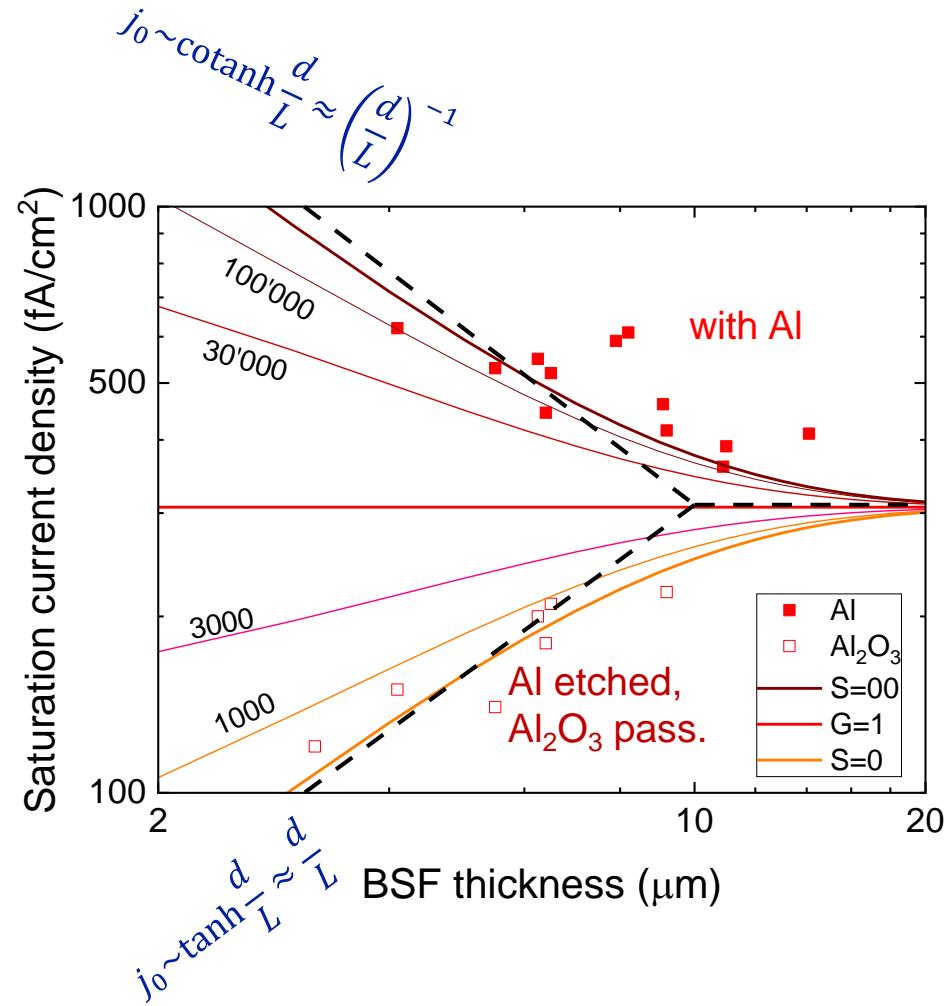
Light, fwd.



Use same formalism as for p-n junction:

- minority carrier density fixed at virtual interface by bulk QFL splitting
- injection into highly doped BSF region (shorter lifetime, lower diffusivity, higher  $n_i$ )

# Example: Al-BSF



Simple model for  $j_0$ :  
approximate with  $H = d_{\text{BSF}}$ ,  
 $N_A = \text{const} = 3 \times 10^{18}/\text{cm}^3$  (Al saturation conc.)

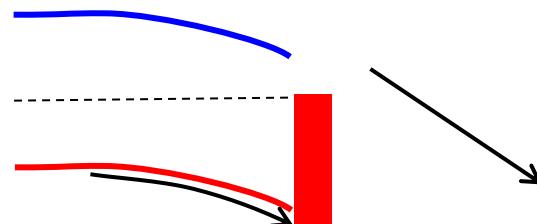
Two branches:

- $S \approx \infty$  (metal contact)  
=> better for thick BSF
- $S \approx 0$  (dielectric w. field effect)  
=> better for thin BSF

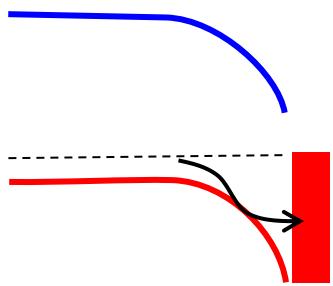
Data: Rüdiger, JAP (2011)

# Contact resistance of a tunnelling contact

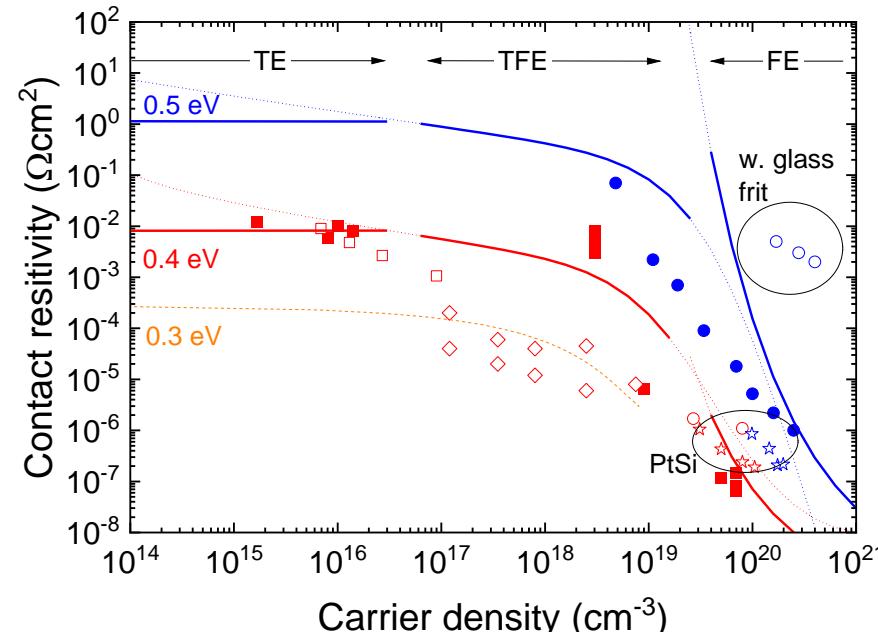
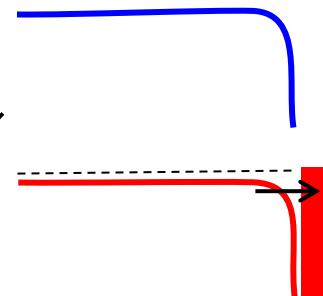
Weak doping:  
thermionic emission  
(TE, std. Schottky theory)



Intermediate:  
thermionic field emission  
(TFE)



High doping:  
Field emission  
(FE, tunnelling)



Padovani, SSE (1966)  
Yu, SSE (1970)

review by: Schroeder, TED (1984)

- Band gap narrowing by merging with adjacent band edge  
=> enhanced recombination statistics (scales with  $\exp\left\{-\frac{E_g - \Delta E_g}{kT}\right\}$ )
- Inactive doping atoms  
clustering into dopant-defect pairs (esp. phosphorous)  
=> yet more recombination
- Parasitic absorption  
absorption by free carrier plasma

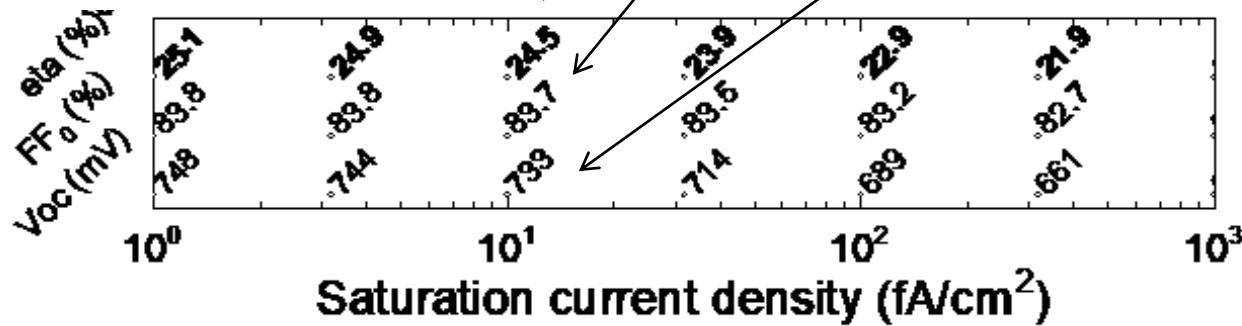
One solution: precise control of doping density and location,  
=> complicated process

# Efficiency for given $j_0$ and $j_{sc}$

$$\eta_0 = V_{oc} \cdot FF_0 \cdot j_{sc}$$

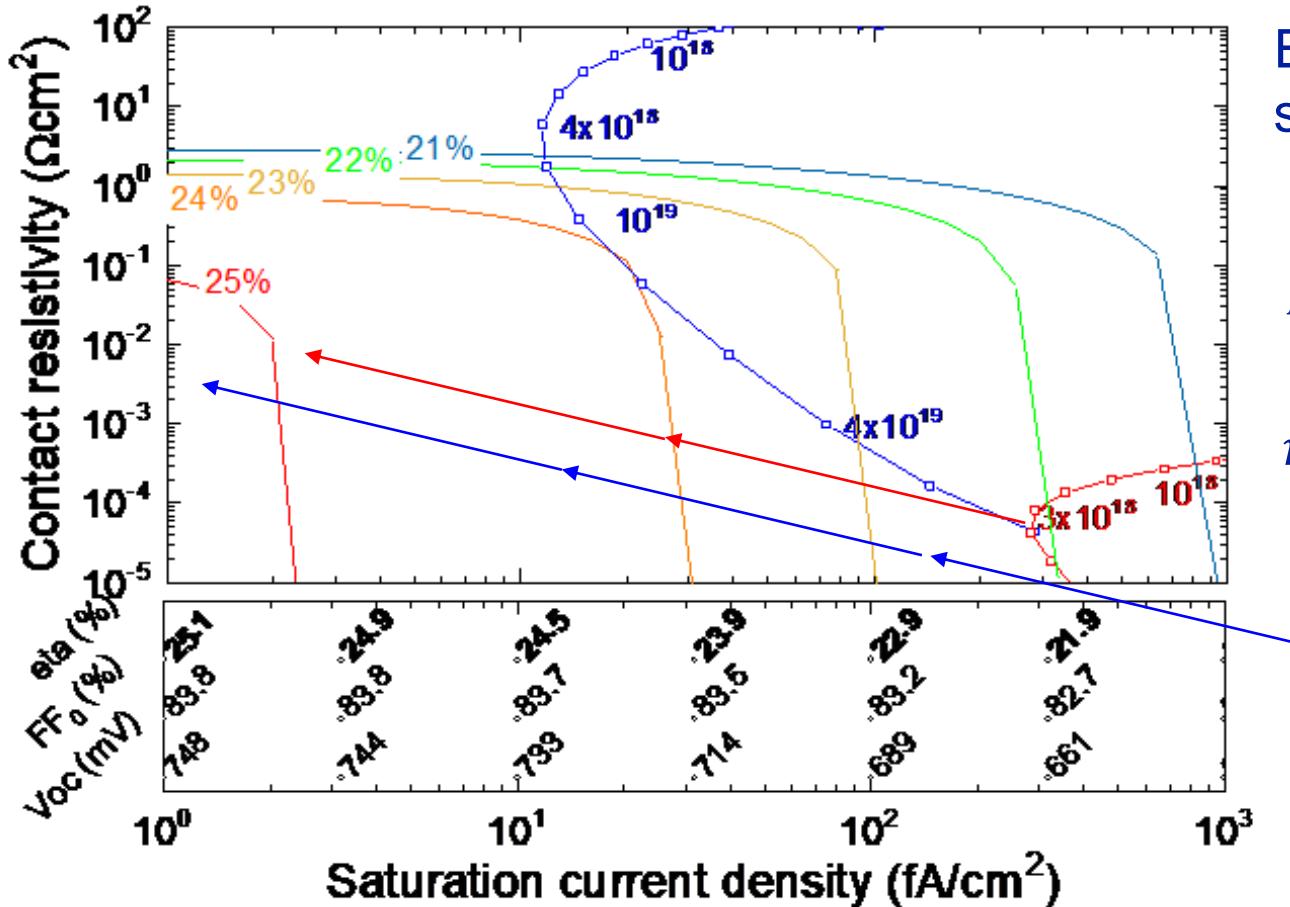
$$FF_0 = \frac{\frac{qV_{oc}}{kT} - \ln\left(\frac{qV_{oc}}{kT} + 0.72\right)}{\frac{qV_{oc}}{kT} + 1}$$

$$V_{oc} = \frac{kT}{q} \ln \frac{j_{sc}}{j_0}, \text{ assume } j_{sc} \approx 40 \text{ mA cm}^{-2}$$



Approximation formulae: Green, SSC (1982)

# Combine $\rho_c$ and $j_0$ for given $j_{sc}$



Efficiency contours with series resistance:

$$FF_s = FF_0 \left( 1 - 1.1 \frac{R_s I_{sc}}{V_{oc}} \right) + \frac{\left( \frac{R_s I_{sc}}{V_{oc}} \right)^2}{5.4}$$

$$\eta = V_{oc} \cdot FF_s \cdot j_{sc}$$

BSF contact ( $10^{-12} \text{ A}/\text{cm}^2$ ,  $10^{-4} \Omega\text{cm}^2$ )  $\Rightarrow$  1% coverage  
Ag front contact: needs higher  $N_{surf}$ , 0.1% eff. coverage

Green, SSC (1982)  
Young, E. Proc. (2014)

# Architectures with improved passivation

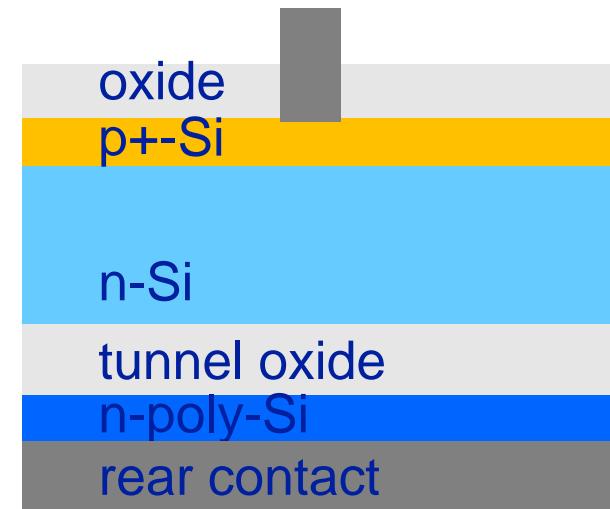
HIT (Hetero junction with Interlayer Technology):  $V_{oc} = 740\text{-}750 \text{ mV}$



Taguchi, JPV (2014)

full area concept  
chemical passivation by a-Si:H  
contacts & field effect by doped a-Si:H  
no direct contact btw. c-Si and metal!

TOPCon (Tunnel Oxide Passivating Contacts):  $V_{oc} = 715 \text{ mV}$

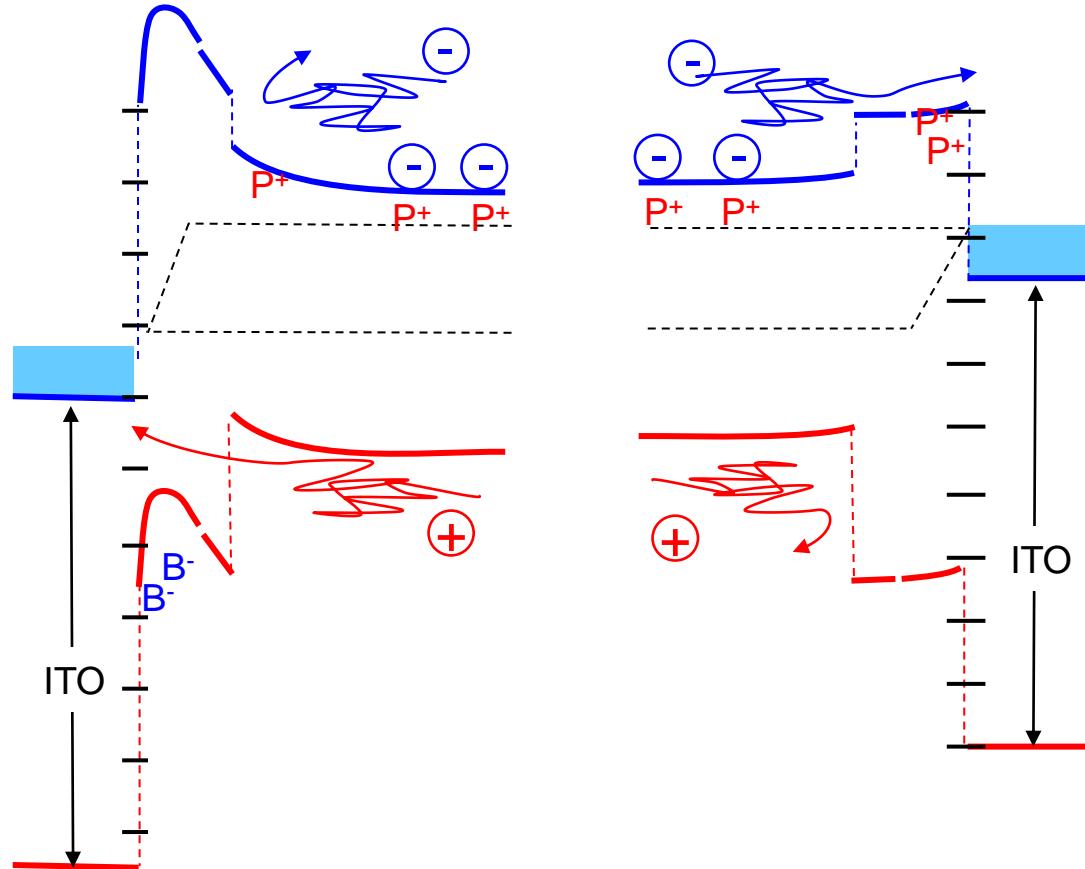


Feldmann, SEM (2014)

full area back contact  
chemical passivation by tunnel oxide  
(probably used by SunPower as well)  
c.f. Gan, Proc. IEEE PVSC (1990)

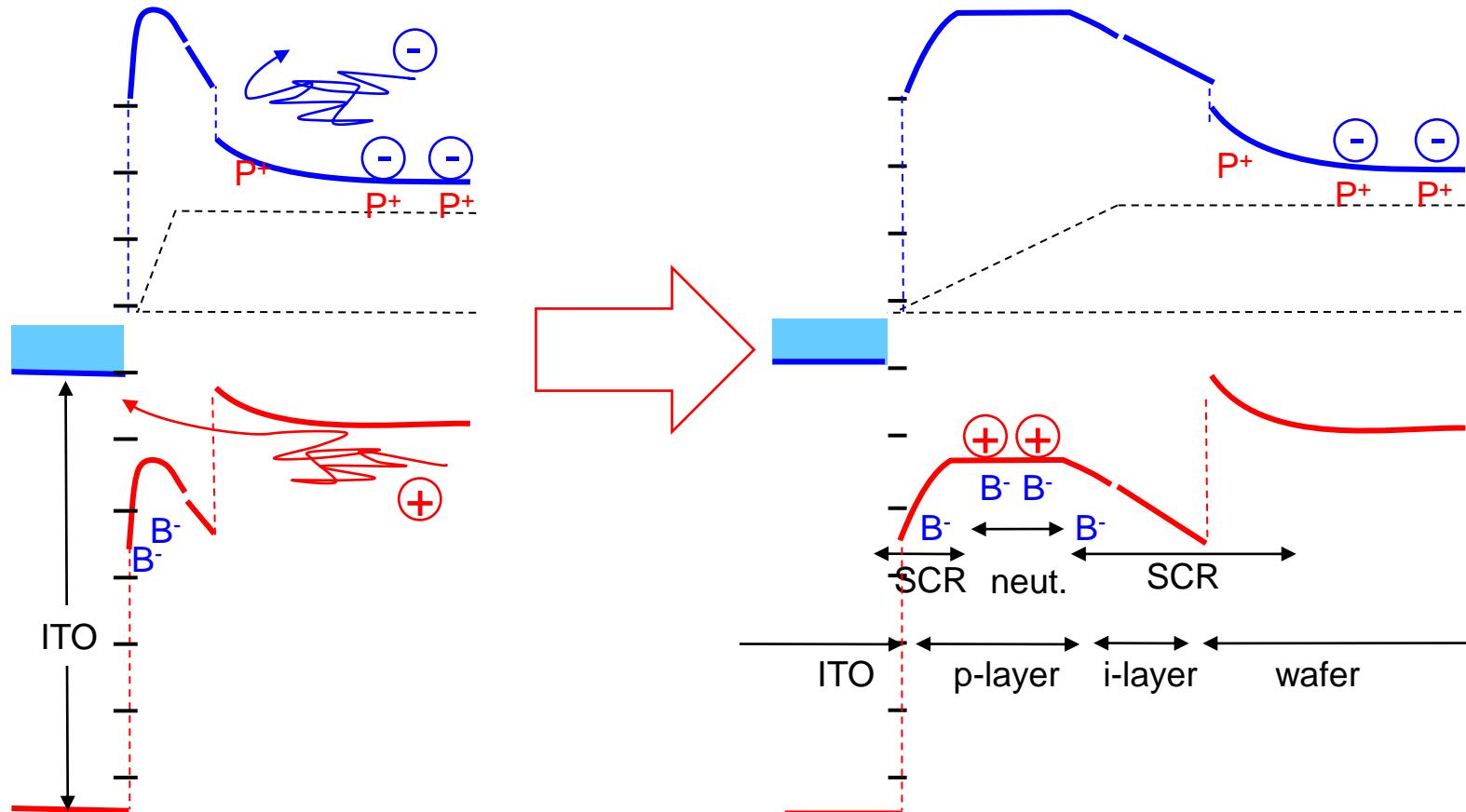
# a-Si:H passivating contacts

passivate interface states at c-Si surface with a-Si:H  
VBO > CBO: efficient hole repulsion (minority carriers)  
p-layer pulls wafer surface into inversion



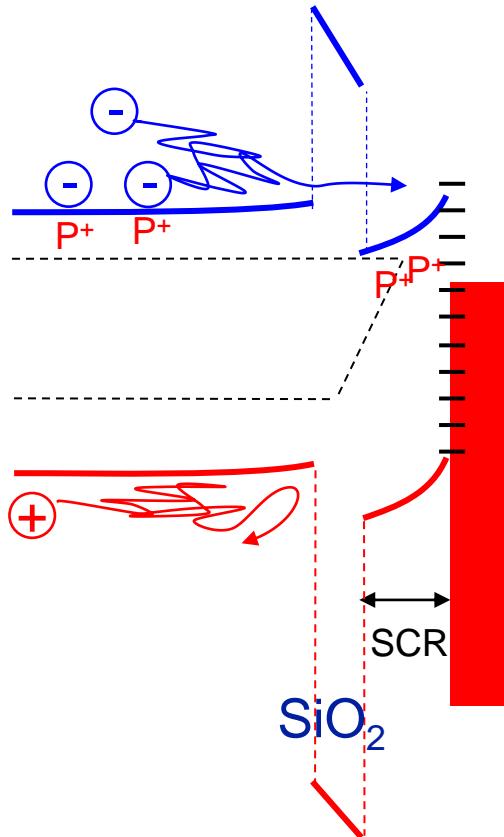
# a-Si:H passivating contacts

p-layer pulls wafer surface into inversion => p-n transition in defect-free wafer



# $\text{SiO}_2$ passivating contacts

$\text{SiO}_2$ : VBO > CBO => slight preference for electron tunnelling,  
but works fine for p-contact with polycrystalline p-layer



BUT: needs ultra-thin  
tunnelling oxide  
(ca. 1 to 1.5 nm)

Gan, IEEE PVSC (1990)  
Feldmann, SEM (2014)  
Preibst, En. Proc. (2015)

- Apparent stagnation of efficiency (25% btw. 1999 and 2014)
- Continuous development of technology behind the scene
- Boost beyond 25% since 2014 along different lines
- Latest record: 26.7% by Kaneka and 27.8% by LONGI