

## Renewable Energy

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# Content Chapter 2

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- Thermodynamics revision
  - Definitions
  - 1<sup>st</sup> law (energy conservation)
  - 2<sup>nd</sup> law (entropy)
  - “1<sup>st</sup> Law minus 2<sup>nd</sup> Law” => Exergy
- Review of thermodynamic power cycles
  - Rankine, Brayton, combined cycles, engines
- Thermodynamic power cycles relevant for renewable energy applications
- Review of thermodynamic heat pump and refrigeration cycles
  - ORC

# Learning outcomes

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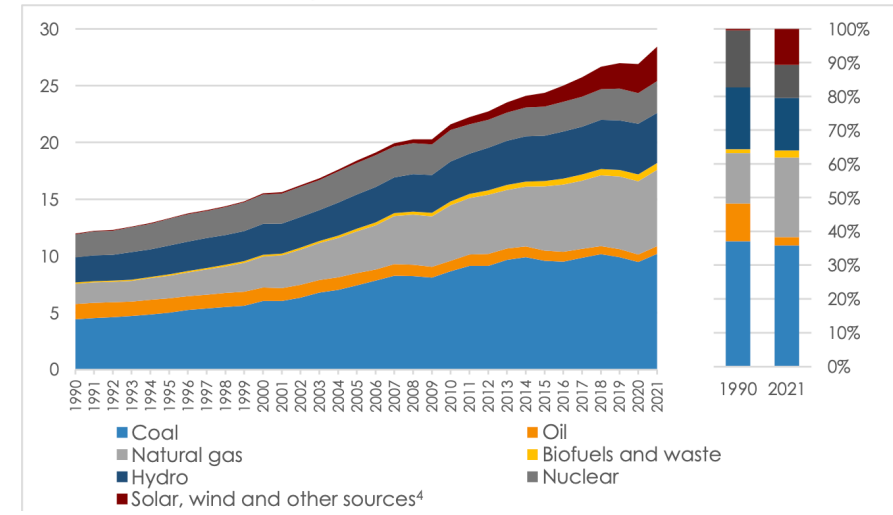
- Understand and apply 1<sup>st</sup> and 2<sup>nd</sup> law of thermodynamics, and exergy concept to relevant systems and cycles
- Apply theory to thermodynamic cycles relevant for renewable energy sources

- Current global power production

28'428 TWh => 3245 GW (100% annual load factor)  
In reality more power is installed as the annual load factor is of course <100%.

38. World electricity generation by source, 1990-2021

Petawatt hours and percentage



39. World electricity generation by source, 1990, 2000, 2010, 2020 and 2021

Terawatt hours

Source	1990	2000	2010	2020	2021
Thermal	7,701.0	10,112.2	14,792.6	17,183.1	18,187.0
- Coal	4,441.6	6,042.1	8,667.2	9,483.5	10,185.0
- Oil	1,339.1	1,198.6	919.3	660.7	694.0
- Natural gas	1,789.2	2,707.2	4,863.8	6,442.5	6,699.5
- Biofuels and waste	131.2	164.2	342.3	596.4	608.5
Nuclear	2,019.8	2,589.0	2,756.3	2,676.4	2,798.9
Hydro	2,193.0	2,706.8	3,528.6	4,463.4	4,408.3
Solar, wind and other sources <sup>4</sup>	61.5	103.8	510.9	2,565.4	3,034.3
<b>Total</b>	<b>11,975.3</b>	<b>15,511.9</b>	<b>21,588.3</b>	<b>26,888.3</b>	<b>28,428.5</b>

→ Steam cycles

→ Gas + combined cycles

→ Integrated steam cycles

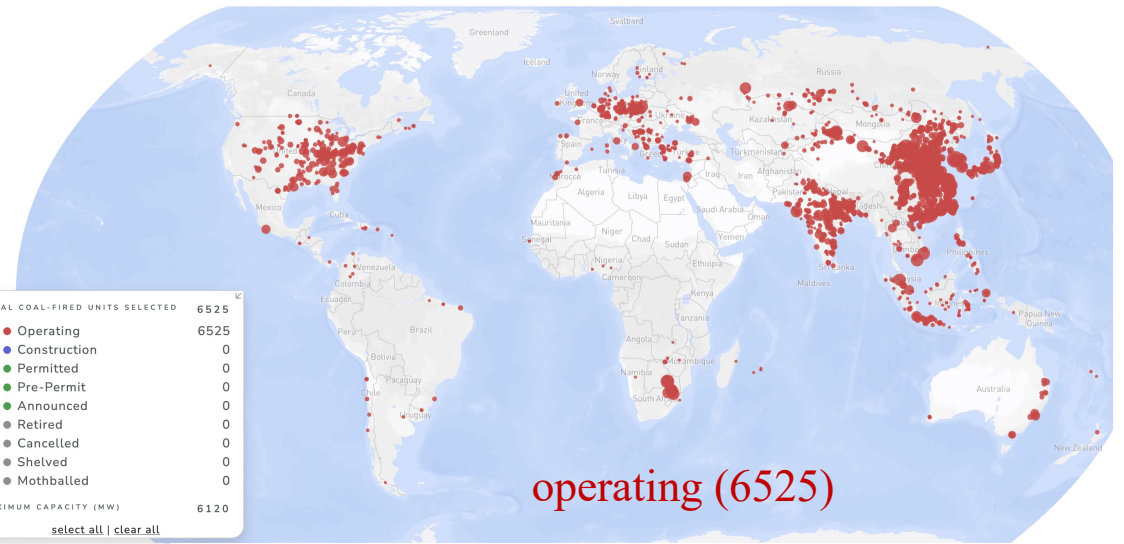
→ Steam cycle

→ incl. Rankine cycles



<https://globalenergymonitor.org/projects/global-coal-plant-tracker/tracker>

# Example : coal plants



# Context

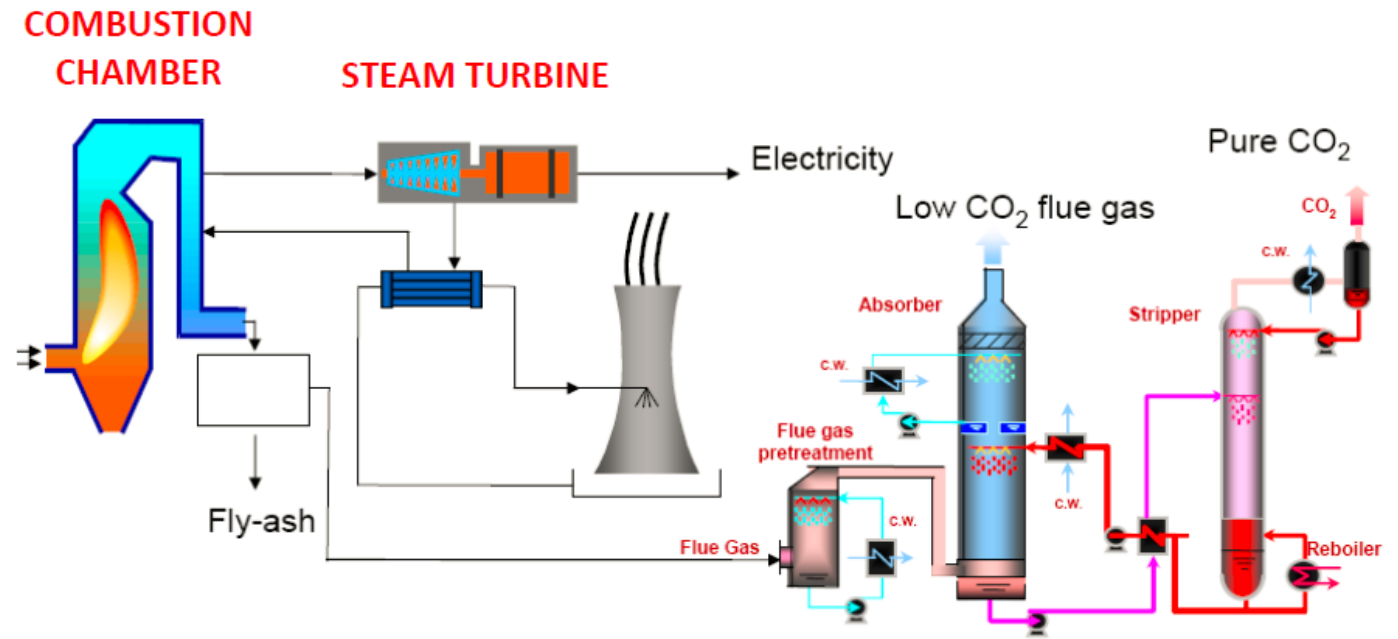
- Energy conversion systems overview:

Service	'Traditional' systems	'Advanced' (or 'new') systems
HEAT (low temperature)	Combustion (fossil fuel, wood) Electrical	Heat pumps Solar thermal Cogeneration
HEAT (high temperature)		Efficient clean combustion Cogeneration Concentrated solar thermal
MOBILITY	Internal combustion engines Electrical (train, bus) Aviation turbines	High efficiency engines Hybrid drives Fuel Cell vehicles, E-vehicles Liquid biofuels
ELECTRICITY	Fossil thermal (coal, gas) Nuclear (PWR, BWR) Hydro (river, dams)	<b>Optimised fossil &amp; biomass power plants</b> <b>Nuclear Generation-IV</b> Hydro (tidal, wave) <b>Solar (photovoltaics)</b> <b>Solar (concentrated thermal)</b> Wind turbines

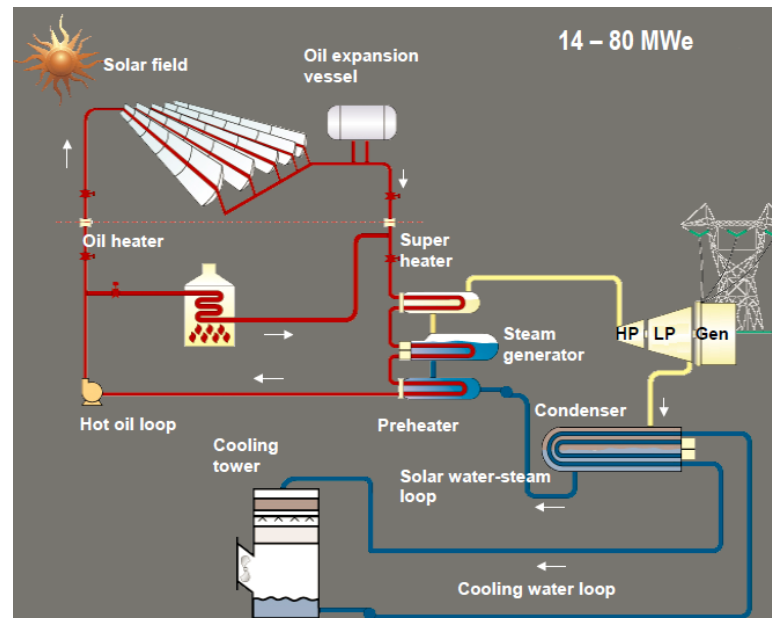
- Systems rely on **power cycles** and turbomachinery: heat → mechanical energy → electricity
- Heating/cooling applications rely on heat/refrigeration **pumping cycles**

# Examples

- Coal plant with CO<sub>2</sub> separation

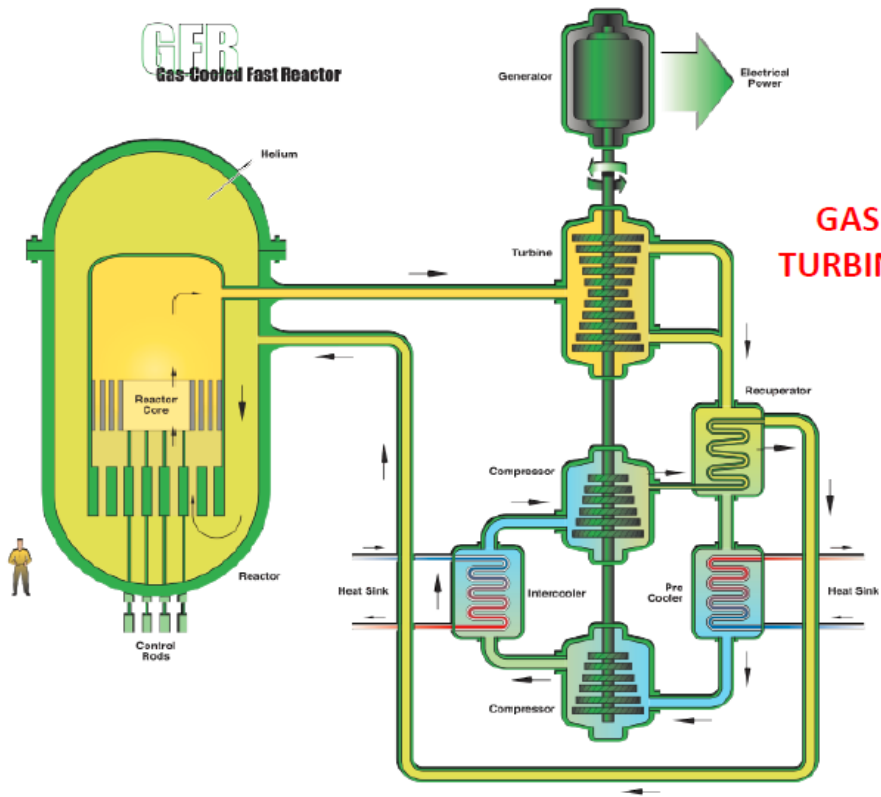


- Concentrated solar power

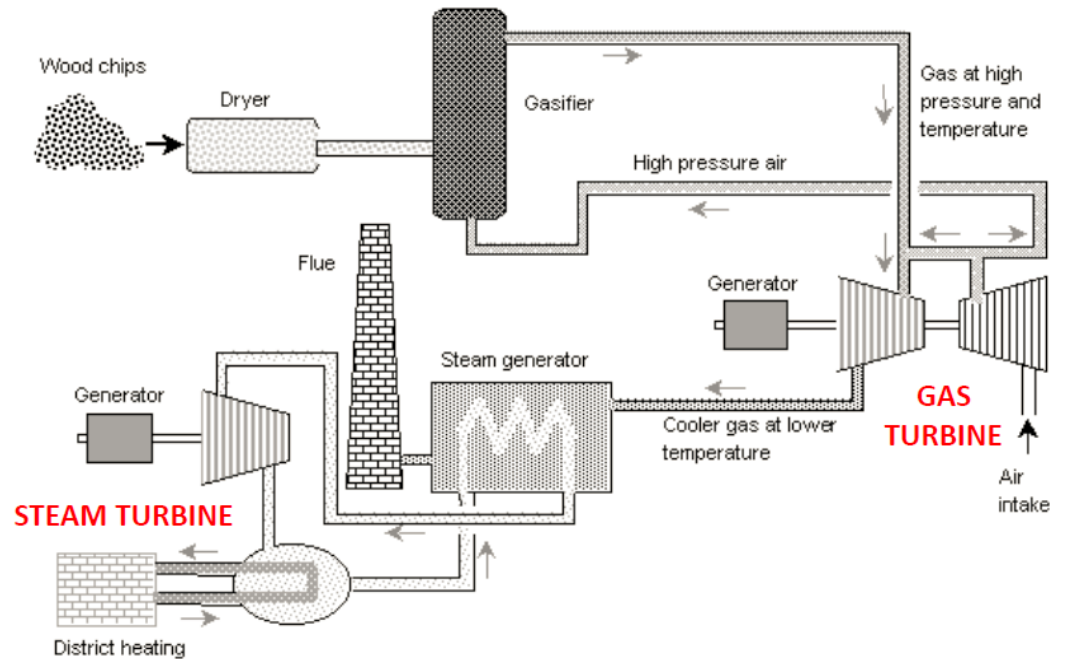


# Examples

– (Advanced) nuclear

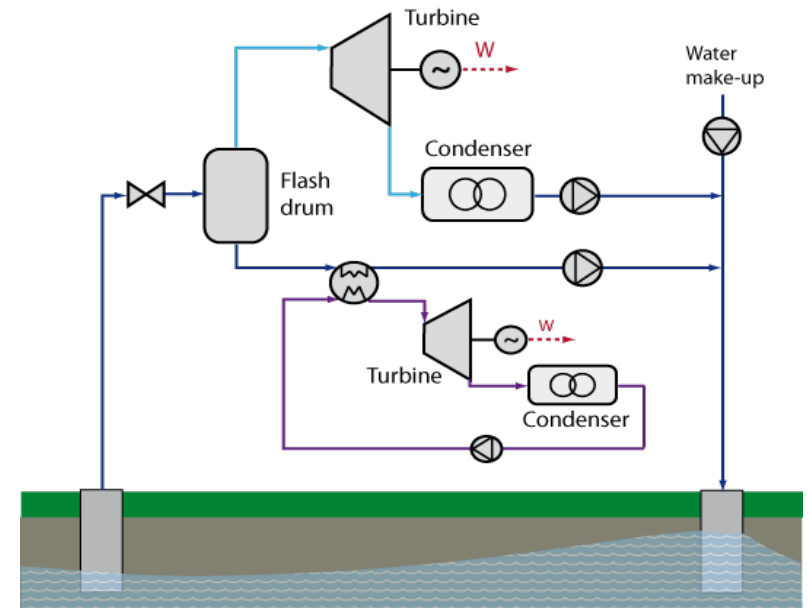
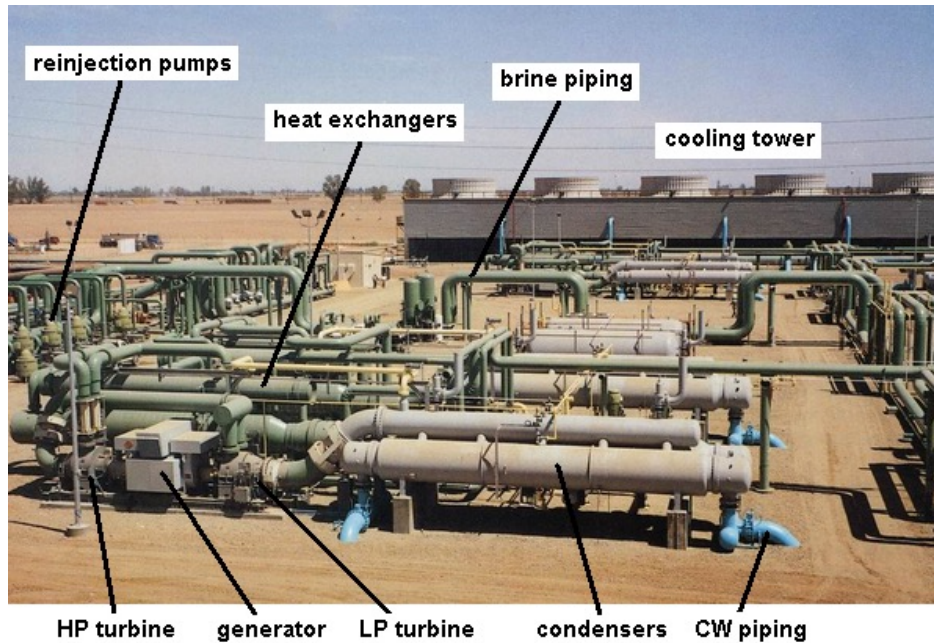


Biomass-fired combined cycle:



# Examples

- Enhanced geothermal systems (EGS)



# 1<sup>st</sup> law for closed and open systems

- Energy conservation for **open** systems:

$$\Delta E = \Delta U + \Delta PE + \Delta KE = \overset{\text{heat}}{Q_{12}} - \overset{\text{work}}{W_{12}} + \overset{\text{enthalpy}}{E_{\text{in}}} - E_{\text{out}}$$

*internal*
*potential*
*kinetic*

$$\left[ \begin{array}{c} \text{time rate of change} \\ \text{of the energy contained} \\ \text{within the control volume} \\ \text{at time } t \end{array} \right] = \left[ \begin{array}{c} \text{net rate of energy} \\ \text{transferred in across} \\ \text{system boundary by heat transfer} \\ \text{at time } t \end{array} \right] - \left[ \begin{array}{c} \text{net rate of energy} \\ \text{transferred out across} \\ \text{system boundary by work transfer} \\ \text{at time } t \end{array} \right] + \left[ \begin{array}{c} \text{net rate of energy} \\ \text{transferred into the} \\ \text{control volume} \\ \text{accompanying mass flow} \end{array} \right]$$



# 1<sup>st</sup> law for open systems

- Energy conservation for open systems: (i.e. with mass transfer / enthalpy)
  - Requires **mass conservation**:

$$\frac{dm_{cv}}{dt} = \sum_i \dot{m}_i - \sum_e \dot{m}_e$$

- Energy conservation:

$$\frac{dE_{cv}}{dt} = \dot{Q} - \dot{W}_{\text{total work}} + \sum_i \dot{m}_i \left( u_i + \frac{w_i^2}{2} + gz_i \right) - \sum_e \dot{m}_e \left( u_e + \frac{w_e^2}{2} + gz_e \right)$$

*(w = fluid speed)*

$$\frac{dE_{cv}}{dt} = \dot{Q}_{cv} - \dot{W}_{\text{effective work}} + \sum_i \dot{m}_i \left( h_i + \frac{w_i^2}{2} + gz_i \right) - \sum_e \dot{m}_e \left( h_e + \frac{w_e^2}{2} + gz_e \right)$$

*enthalpy  $h = u + pV$  (work term due to mass transfer in/out)*

(cv : control volume)

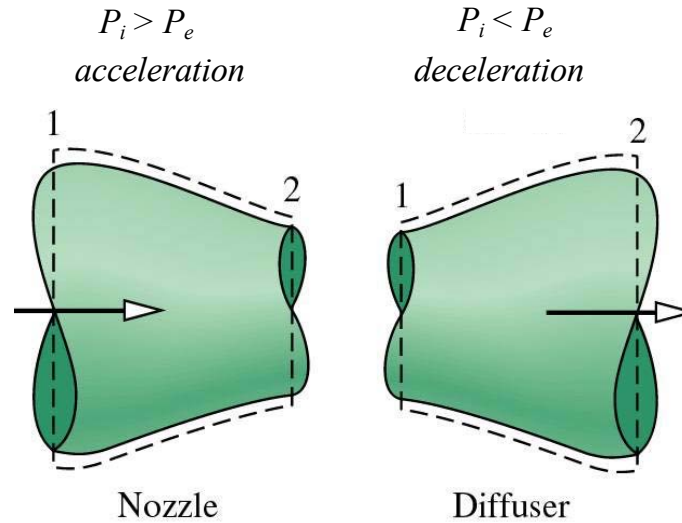
# 1<sup>st</sup> law for closed and open systems

- Energy conservation for open systems: Applications:
  - Nozzle, diffusor

$$h_i + \frac{w_i^2}{2} = h_e + \frac{w_e^2}{2}$$

( $w$  = fluid speed)

total enthalpy is conserved

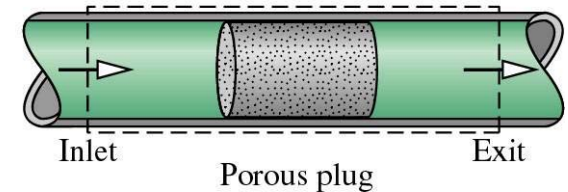
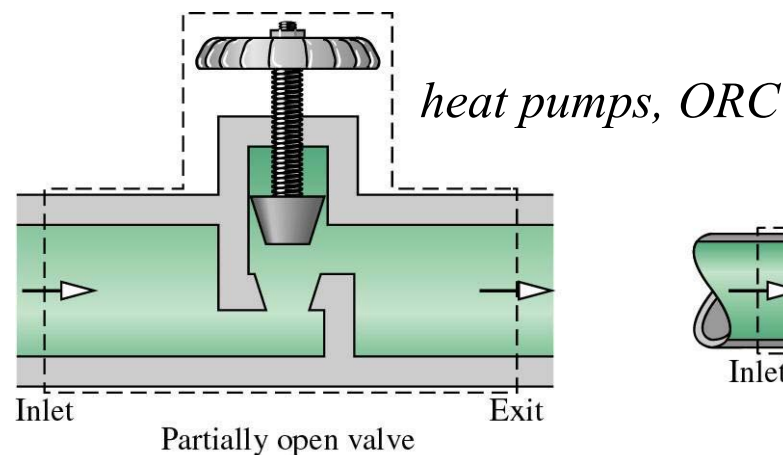


turbines

- Throttling valves

$$h_i = h_e$$

$$h = u + Pv$$



$$P_i > P_e \Rightarrow v_i < v_e \Rightarrow w_i < w_e$$



# 1<sup>st</sup> law for closed and open systems

- Energy conservation for open systems: Applications:
  - Turbine, compressor, pump, fan

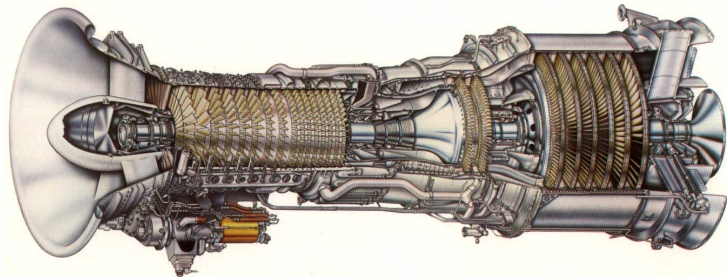
$$0 = -\dot{W} + \dot{m} \left( h_i + \frac{w_i^2}{2} + gz_i \right) - \dot{m} \left( h_e + \frac{w_e^2}{2} + gz_e \right)$$

work =  $\Delta h_{\text{fluid}}$

(~adiabatic)



GE, Roots\* API 617 OIB



GE, LM2500 gas turbine, ships, ca. 30 MW



Voith-Kaplan turbine, 200 MW, diameter 10.5m

- Heat exchanger

$$0 = \sum_{\text{inlets:}i} \dot{m}_i h_i - \sum_{\text{outlets:}j} \dot{m}_j h_j$$



Brazetek heat exchanger

# Efficiency

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- Energy efficiency or performance metric can be introduced for single components or complete systems
  - always need a proper definition!
  - indicates how well an energy conversion or transfer process is accomplished

- General:

$$\text{Efficiency} = \frac{\text{desired output}}{\text{required input}}$$

# Efficiency

- Example - Efficiency of *combustion systems*:

Efficiency of combustion processes is related to the *heating value of a fuel*, which is the amount of heat released when a unit amount of fuel at room temperature is completely burned and the combustion products are cooled to room temperature.

- Combustion efficiency:

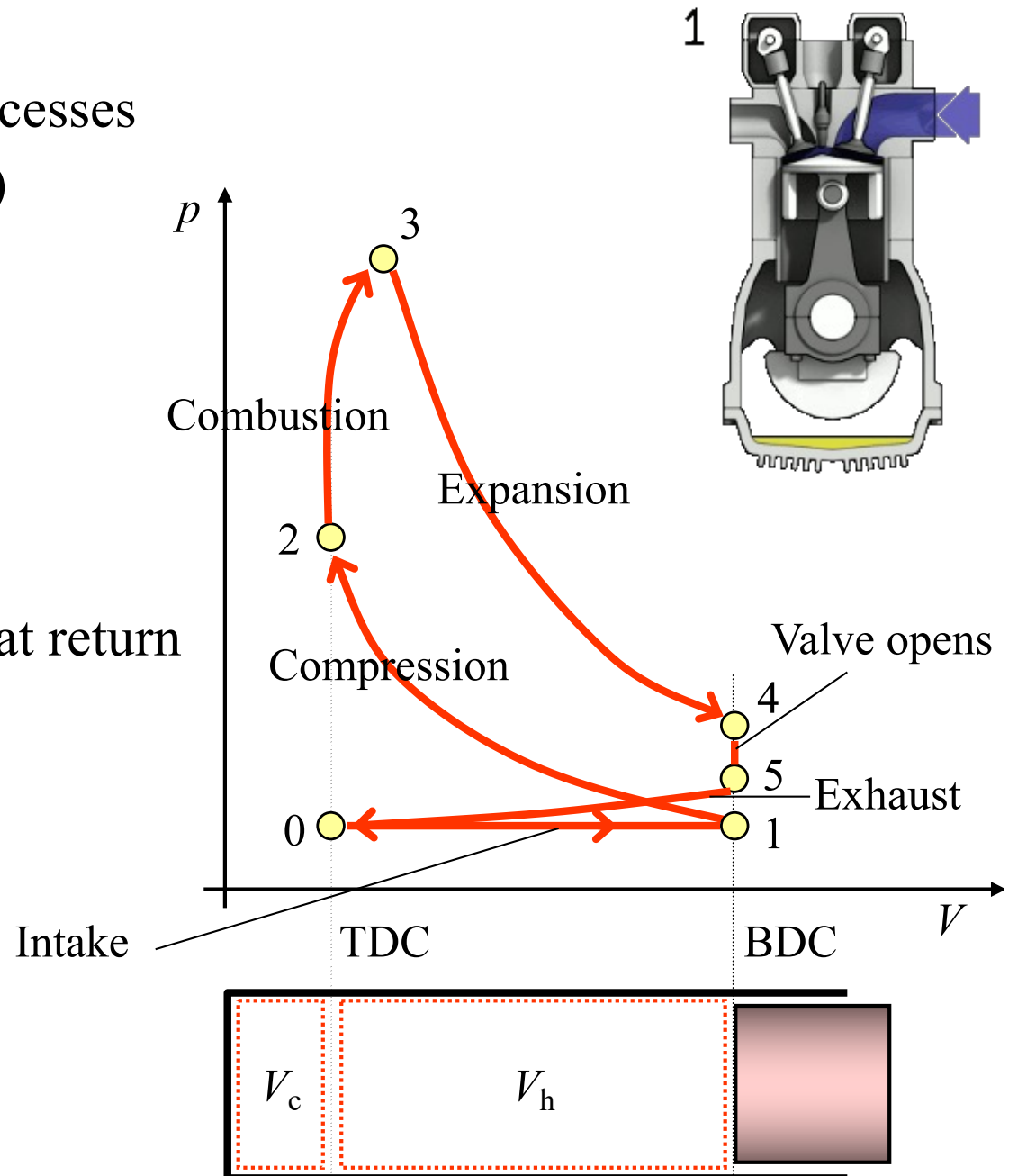
$$\eta_{\text{combustion}} = \frac{\text{amount of heat released during combustion}}{\text{heating value of the fuel burned}}$$
$$= \frac{\dot{Q}}{\dot{m}HV}$$

- Heating values (HV):
  - **Higher** heating values (HHV):  
water is condensed (boilers etc.)
  - **Lower** heating values (LHV):  
water exhaust remains vapor (cars, jet engines, etc.)

Fuel	HHV MJ/kg	LHV MJ/kg
Hydrogen	141.80	119.96
Methane	55.50	50.00
Ethane	51.90	47.80
Propane	50.35	46.35
Butane	49.50	45.75
Gasoline	47.30	44.4
Kerosene	46.20	43.00
Diesel	44.80	43.4
Coal (Anthracite)	32.50	
Coal (Lignite)	15.00	
Wood	21.7	20

# Processes and Cycles

- Definitions:
  - Process: special types of processes
    - Isothermal ( $T = \text{constant}$ )
    - Isobaric ( $p = \text{constant}$ )
    - Isochoric ( $v = \text{constant}$ )
    - Isentropic ( $s = \text{constant}$ )
    - Adiabatic ( $\dot{Q} = 0$ )
  - Cycle: series of processes that return a system to its initial state  
E.g. 4-stroke engine



(TDC: top dead center)  
(BDC: bottom dead center)

# Energy for closed systems

- Cycle analysis:

$$\Delta E = 0 = Q_{\text{cycle}} - W_{\text{cycle}}$$

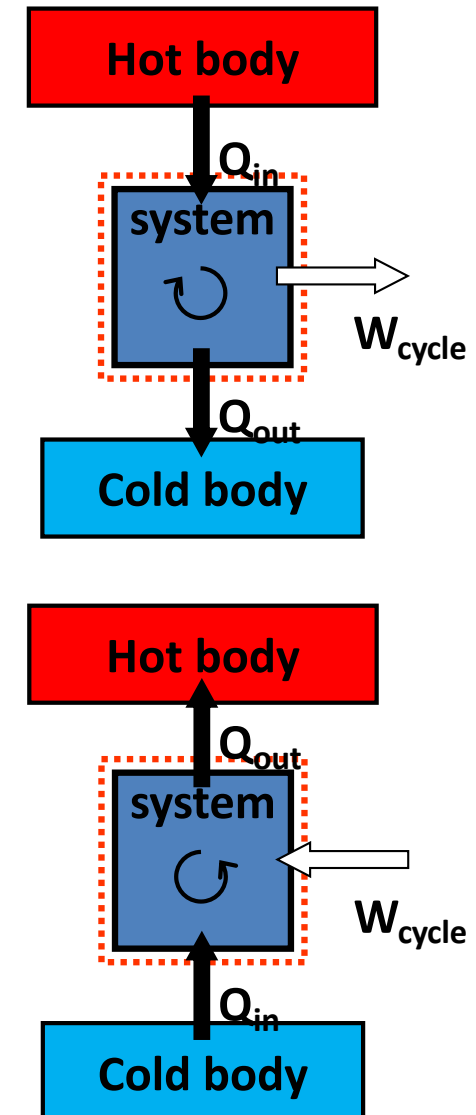
- Power cycles:

$$\eta_{\text{th}} = \frac{W_{\text{cycle}}}{Q_{\text{in}}} = 1 - \frac{|Q_{\text{out}}|}{Q_{\text{in}}} \quad \text{Carnot}$$

- Refrigeration and heat pump cycles:

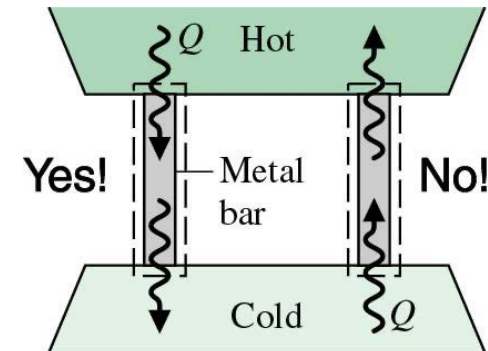
$$\text{COP}_{\text{cm}} = \frac{Q_{\text{in}}}{|W_{\text{cycle}}|} = \frac{Q_{\text{in}}}{|Q_{\text{out}}| - Q_{\text{in}}} \quad \begin{array}{l} Q_{\text{in}}: \text{Heat extracted at cold source} \\ Q_{\text{out}}: \text{Heat rejected at hot source} \end{array}$$

$$\text{COP}_{\text{hm}} = \frac{Q_{\text{out}}}{W_{\text{cycle}}} = \frac{|Q_{\text{out}}|}{|Q_{\text{out}}| - Q_{\text{in}}} = \text{COP}_{\text{cm}} + 1$$

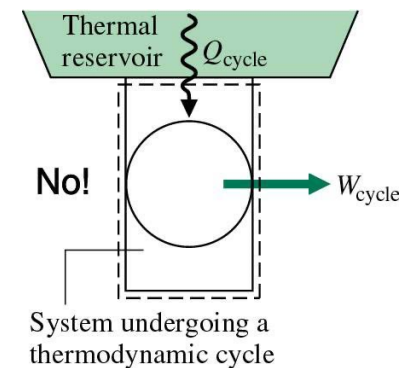


# 2<sup>nd</sup> law of thermodynamics

- It is impossible for a system to operate in such a way that the only result would be an energy transfer by heat from a cooler to a hotter body.



- It is impossible for any system to operate in a thermodynamic cycle and deliver a net amount of energy by work to its surrounding while receiving energy by heat transfer from a single thermal reservoir.



- It is impossible for any system to operate in a way that system entropy is destroyed.

$$S_2 - S_1 = \sum_j \frac{Q_j}{T_j} + \sigma$$

↓  
 internal entropy production

$$\left\{ \begin{array}{l} >0 \text{ irreversibilities} \\ =0 \text{ no irreversibilities} \\ <0 \text{ impossible} \end{array} \right.$$

# Entropy balance – closed systems

$$\left[ \begin{array}{c} \text{change in the} \\ \text{amount of entropy} \\ \text{contained within system} \\ \text{during time interval} \end{array} \right] = \left[ \begin{array}{c} \text{net amount of entropy} \\ \text{transferred in across} \\ \text{system boundary} \\ \text{during time interval} \end{array} \right] + \left[ \begin{array}{c} \text{amount of entropy} \\ \text{produced within} \\ \text{system during} \\ \text{time interval} \end{array} \right]$$

- General:

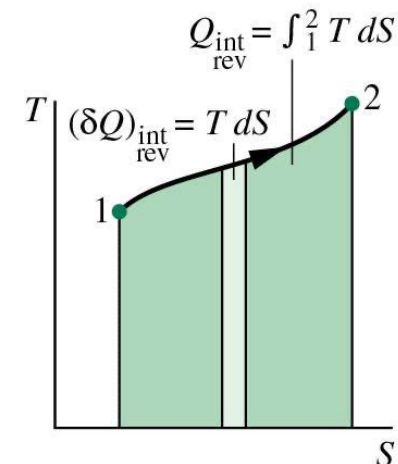
$$S_2 - S_1 = \int_1^2 \left( \frac{\delta Q}{T} \right)_b + \sigma = \sum_j \frac{Q_j}{T_j} + \sigma \quad \frac{dS}{dt} = \sum_j \frac{\dot{Q}_j}{T_j} + \dot{\sigma}$$

- Internally reversible processes:

$$S_2 - S_1 = \left( \int_1^2 \frac{\delta Q}{T} \right)_{\text{int rev}} \quad \frac{dS}{dt} = \left( \sum_j \frac{\dot{Q}_j}{T_j} \right)_{\text{int rev}}$$

S = State function:  
process **independent**

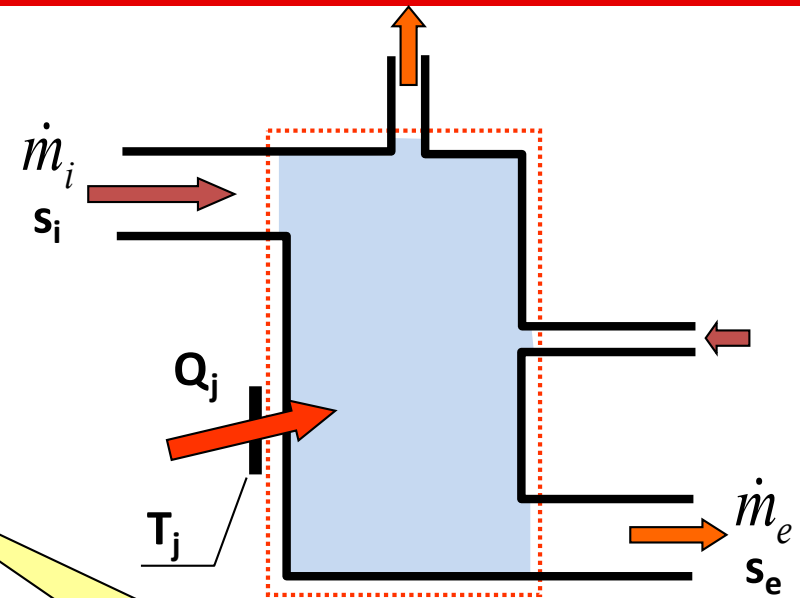
heat transfer : process **dependent**



# Entropy balance – open systems

- Entropy balance for an open system:

$$\frac{dS_{cv}}{dt} = \sum_j \frac{\dot{Q}_j}{T_j} + \underbrace{\sum_i \dot{m}_i s_i - \sum_e \dot{m}_e s_e}_{\text{Convective entropy transport}} + \dot{\sigma}_{cv}$$



**Rate of entropy change** in control volume

**Entropy transfer** due to heat transfer (in or out) over system boundary

**Convective entropy transport**

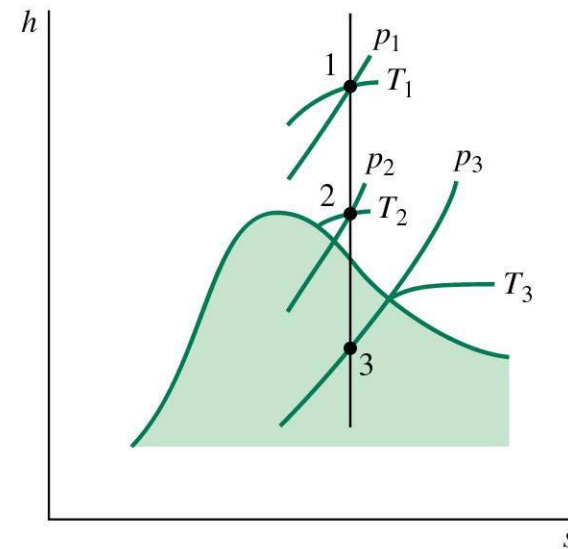
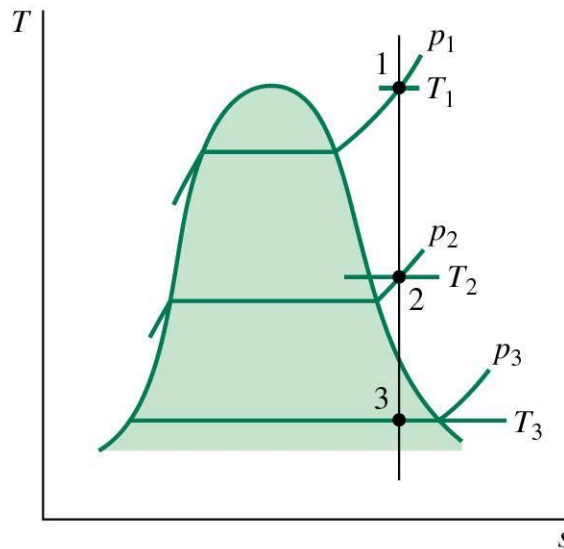
**Entropy production** within the control volume

- Simplifications for steady state systems, or systems with only one inlet/outlet



# Isentropic processes

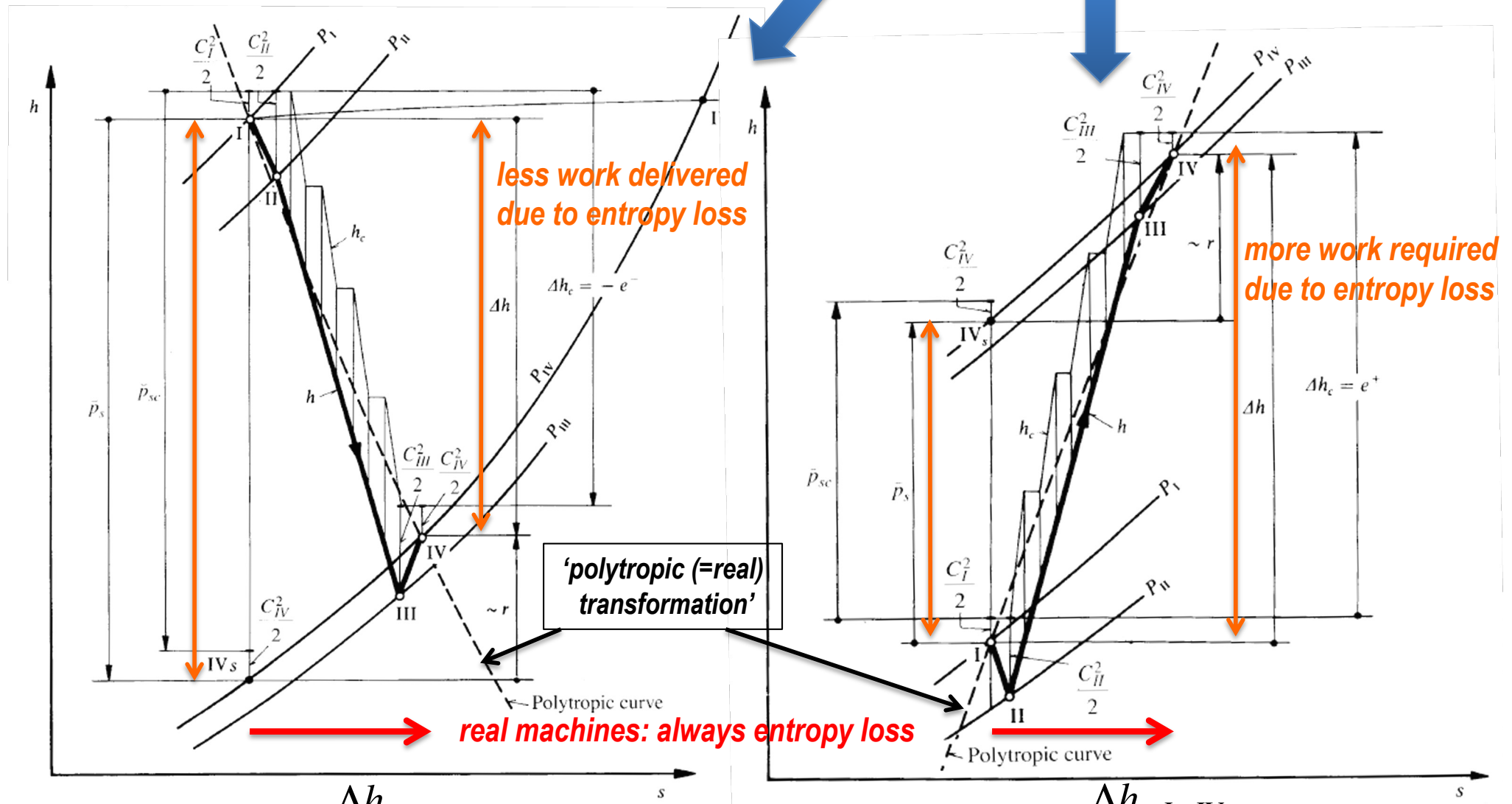
- Isentropic = constant entropy.
- Isentropic processes are processes where the entropy at the initial and final state are equal.
- Isentropic processes, e.g.: closed system, reversible and adiabatic process



- Isentropic (turbine) efficiencies:

$$\eta_{t,s} = \frac{\dot{W} / \dot{m}}{(\dot{W} / \dot{m})_s} = \frac{h_1 - h_2}{h_1 - h_{2,s}}$$

# h-s diagram of fluid expansion/compression



$$\eta_{Ts} = \frac{\Delta h_{I-IV}}{\Delta h_{s,I-IV}}$$

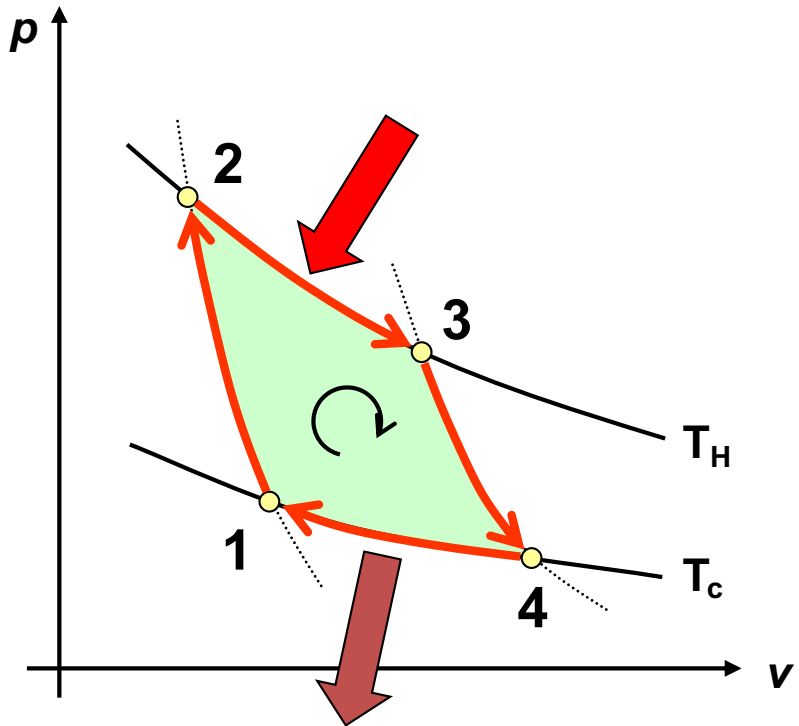
isentropic turbine efficiency

$$\eta_{Cs} = \frac{\Delta h_{s,I-IV}}{\Delta h_{I-IV}}$$

isentropic compressor efficiency

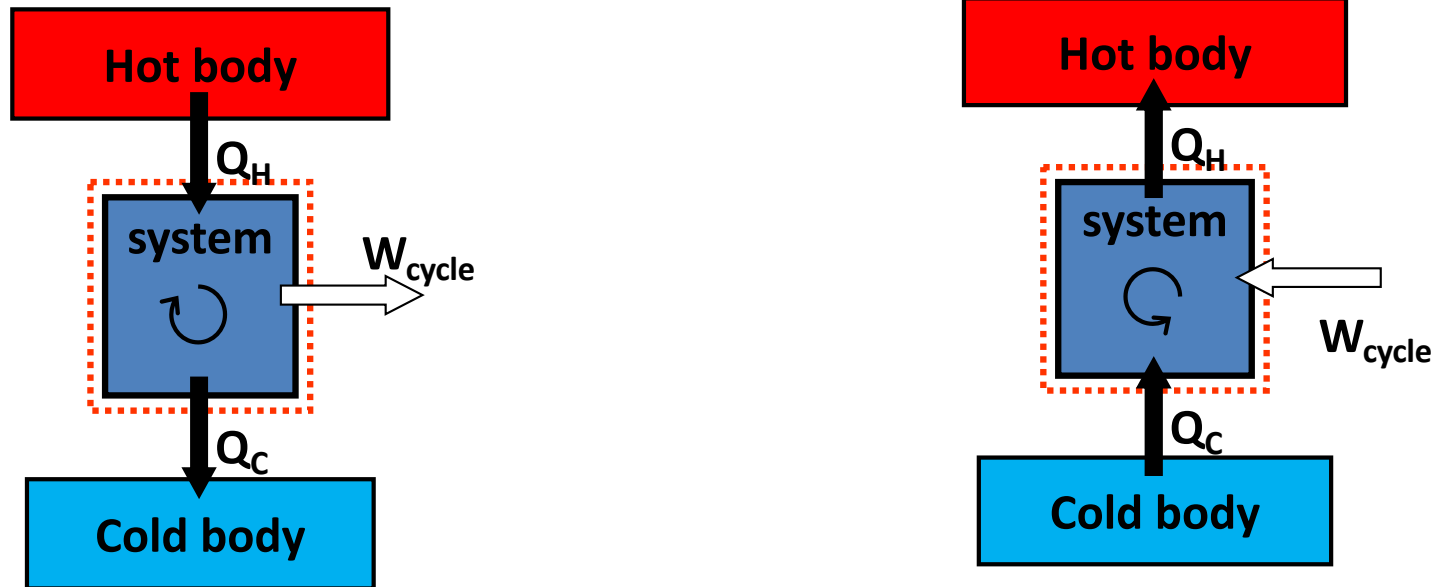
# Carnot cycle

- Carnot cycle:  
cycle that undergoes four reversible processes
- Two isothermal processes at two different temperature levels.  
Require heat to be delivered or rejected
- Two isentropic processes
- Reverse direction => refrigeration or heat pump cycle
- Efficiency given by Carnot efficiency or COP



# Carnot efficiency

- Maximum efficiencies of power and refrigeration/heat pump cycles:



Efficiency	$\eta_{th} = \frac{W_{cycle}}{Q_H} = 1 - \frac{Q_C}{Q_H}$	$COP_{cm} = \frac{Q_C}{W_{cycle}} = \frac{Q_C}{Q_H - Q_C}$	$COP_{hm} = \frac{Q_H}{W_{cycle}} = \frac{Q_H}{Q_H - Q_C}$
Max. efficiency (Carnot)	$\eta_{th,max} = 1 - \left( \frac{Q_C}{Q_H} \right)_{rev\ cycle} = 1 - \frac{T_C}{T_H}$	$COP_{cm,max} = \frac{T_C}{T_H - T_C}$	$COP_{hm,max} = \frac{T_H}{T_H - T_C}$

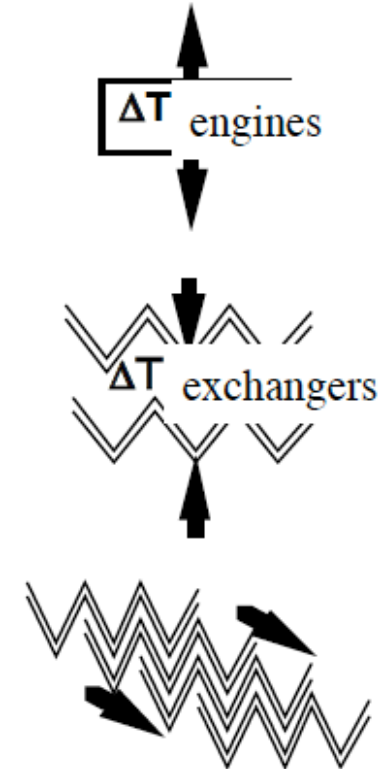
Efficiency independent of process, components, fluids, only dependent on temperature of reservoirs

Best case -> exergy efficiency = 1 -> delivered work equals received heat exergy

# Consequences of the 2<sup>nd</sup> Law

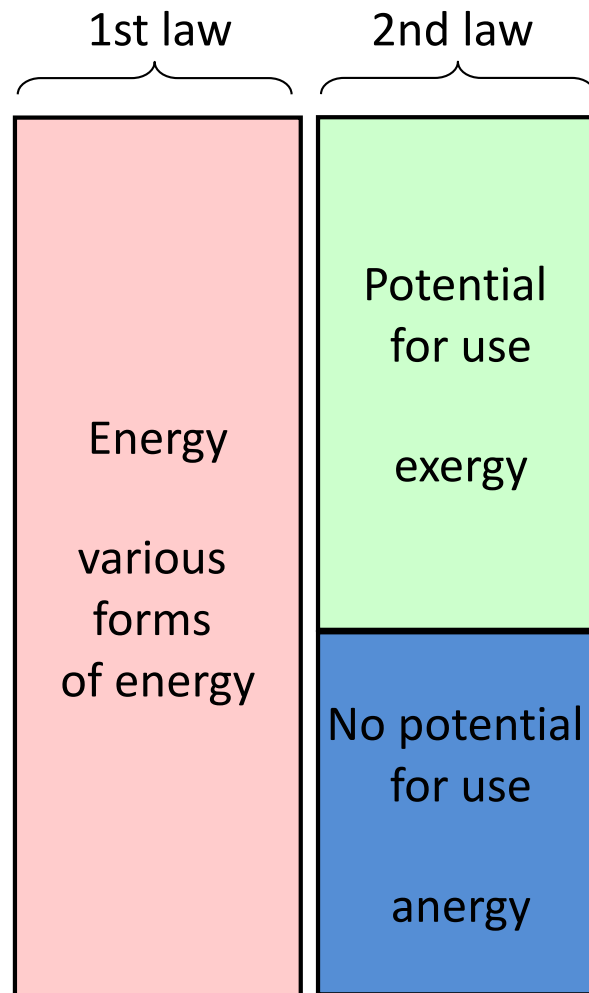
## Practical implications from the second law:

- **Increase the temperature differences of the engine cycles.** (Superposed cycles, increased higher temperature)
- **Limit the temperature drop during heat transfer** (Increase the heat exchange surfaces (but take care of the pressure drop), counter current heat exchange)
- **Multiply the use of a same thermal source** (Cogeneration, heat exchanger cascade, extraction in turbine, superposed cycles)



# Exergy

- What is the potential for use?



# Exergy

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- Exergy – Definition:

$$Ex = U - U_0 + KE + PE - T_0 (S - S_0) + p_0 (V - V_0)$$

- Specific exergy:

$$ex = u - u_0 + ke + pe - T_0 (s - s_0) + p_0 (v - v_0)$$

- Exergy difference between two states:

$$Ex_2 - Ex_1 = (U_2 - U_1) + (KE_2 - KE_1) + (PE_2 - PE_1) - T_0 (S_2 - S_1) + p_0 (V_2 - V_1)$$

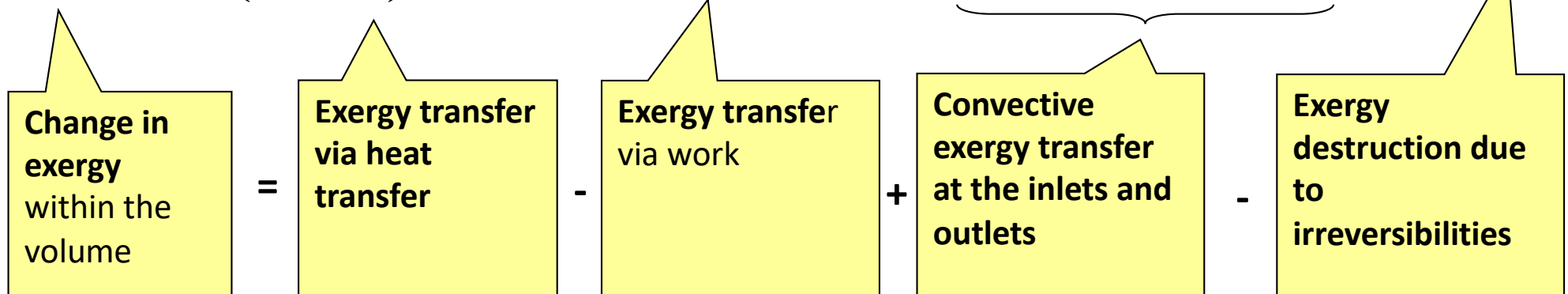
- Specific exergy difference between two states:

$$ex_2 - ex_1 = (u_2 - u_1) + (ke_2 - ke_1) + (pe_2 - pe_1) - T_0 (s_2 - s_1) + p_0 (v_2 - v_1)$$

# Exergy balance - open systems

- Open systems – Exergy:

$$\frac{dEx}{dt} = \sum_j \left( 1 - \frac{T_0}{T_j} \right) \dot{Q}_j - \left( \dot{W} - p_0 \frac{dV}{dt} \right) + \underbrace{\sum_i \dot{m}_i ex_{f,i} - \sum_e \dot{m}_e ex_{f,e}}_{\text{Convective exergy transfer at the inlets and outlets}} - T_0 \dot{\sigma}$$



- With flow exergy:

$$ex_f = u - u_0 + ke + pe - T_0 (s - s_0) + p_0 (v - v_0) + (p - p_0)v$$

$$ex_f = h - h_0 + ke + pe - T_0 (s - s_0)$$

$$ex_f = ex + (p - p_0)v$$



# Exergy efficiency

- Exergy efficiency expresses the work-equivalent efficiency of energy resource utilization

$$\varepsilon_{ex} = \frac{\text{used exergy}}{\text{provided exergy}} \quad \nearrow \quad \eta = \frac{\text{used energy}}{\text{provided energy}}$$

energy efficiency

- Components:

- Turbine: 
$$\varepsilon_{ex} = \frac{(\dot{W} / \dot{m})}{ex_{f,i} - ex_{f,e}}$$

- Compressor/pump: 
$$\varepsilon_{ex} = \frac{ex_{f,e} - ex_{f,i}}{(-\dot{W}_{cv} / \dot{m})}$$

- Heat exchanger:  
(non/mixing)

$$\varepsilon_{ex} = \frac{m_c (ex_{f,e,c} - ex_{f,i,c})}{m_h (ex_{f,i,h} - ex_{f,e,h})} \quad \varepsilon_{ex} = \frac{m_2 (ex_{f,3} - ex_{f,2})}{m_1 (ex_{f,1} - ex_{f,3})}$$

# Turbine

Work **OUTPUT**

(enthalpy balance):

$$\dot{E}^- = \dot{Y}^+ - \dot{Q}_a^- = \sum_j [h_{cj} \dot{M}_j^+] - \dot{Q}_a^-$$

$\dot{M}$ : steam mass flow rate

$$\dot{E}^- = \dot{M}_1 h_{c1} - \dot{M}_2 h_{c2} - \dot{M}_3 h_{c3} - \dot{M}_4 h_{c4} - \dot{M}_5 h_{c5} - \dot{M}_6 h_{c6} - \dot{Q}_a^-$$

$$\dot{E}^- = \dot{E}_y^+ - \dot{L}$$

Exergy **balance**:

$$\dot{E}_y^+ = \sum_j [k_{czj} \dot{M}_j^+] = \dot{M}_1 k_{c1} - \dot{M}_2 k_{c2} - \dot{M}_3 k_{c3} - \dot{M}_4 k_{c4} - \dot{M}_5 k_{c5} - \dot{M}_6 k_{c6}$$

Exergy efficiency:

$$\eta = \frac{\dot{E}^-}{\dot{E}_y^+} = 1 - \frac{\dot{L}}{\dot{E}_y^+} = \frac{\sum_j [h_{cj} \dot{M}_j^+] - \dot{Q}_a^-}{\sum_j [k_{cj} \dot{M}_j^+]}$$

Exergy **loss**:

$$\dot{L} = T_a \sum_j [s_j \dot{M}_j^-] + \dot{Q}_a^-$$

$$\dot{L} = T_a (\dot{M}_2 s_2 + \dot{M}_3 s_3 + \dot{M}_4 s_4 + \dot{M}_5 s_5 + \dot{M}_6 s_6 - \dot{M}_1 s_1) + \dot{Q}_a^-$$

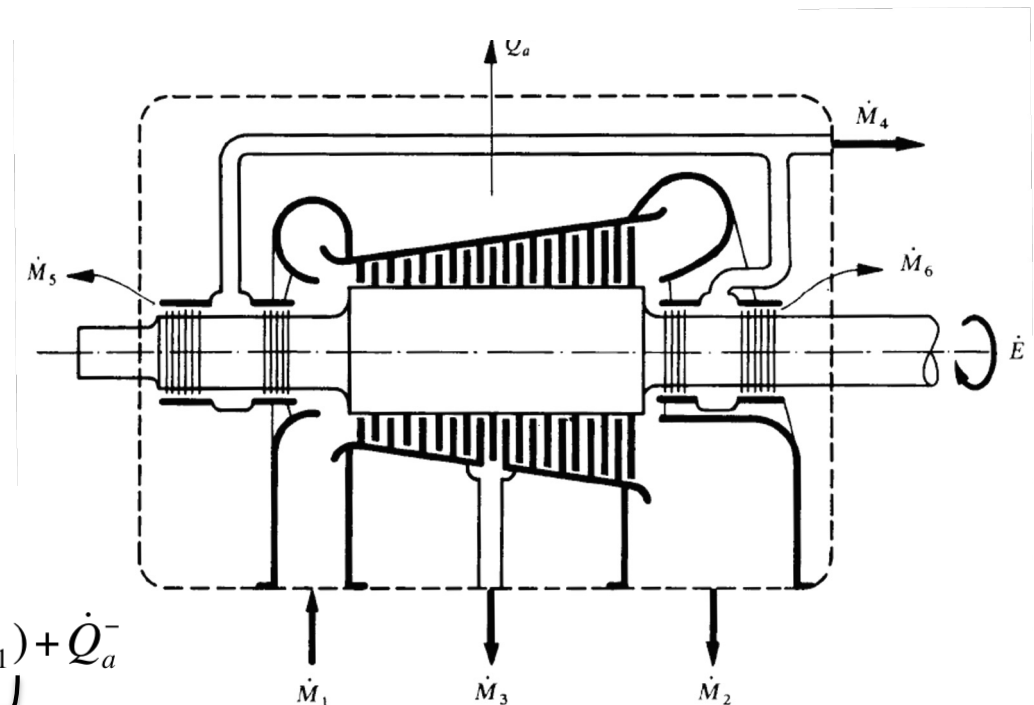


Fig. 10.42 A schematic representation of a steam turbine with extraction.

dissipation in the steam network (inlet, outlet, blades, channels, labyrinth seals)

# Compressor

## Work INPUT

$$\dot{E}^+ = \dot{Y}^- = \sum_j [h_{cj} \dot{M}_j^-] = \dot{M}_2 h_{c2} + \dot{M}_3 h_{c3} + \dot{M}_4 h_{c4} - \dot{M}_1 h_{c1}$$

(enthalpy balance):

$$\text{Exergy : } \dot{E}_y^- = \sum_j [k_{cj} \dot{M}_j^-] = \dot{M}_2 k_{c2} + \dot{M}_3 k_{c3} + \dot{M}_4 k_{c4} - \dot{M}_1 k_{c1}$$

$$\text{Balance : } \dot{E}_y^- = \dot{E}^+ - \dot{L}_r$$

Exergy efficiency:

$$\eta = \frac{\dot{E}_y^-}{\dot{E}^+} = 1 - \frac{\dot{L}_r}{\dot{E}^+} = \frac{\sum_j [k_{cj} \dot{M}_j^-]}{\sum_j [h_{cj} \dot{M}_j^-]}$$

Exergy loss:

$$\dot{L}_r = T_a \sum_j [s_j \dot{M}_j^-] = T_a (\dot{M}_2 s_2 + \dot{M}_3 s_3 + \dot{M}_4 s_4 - \dot{M}_1 s_1)$$

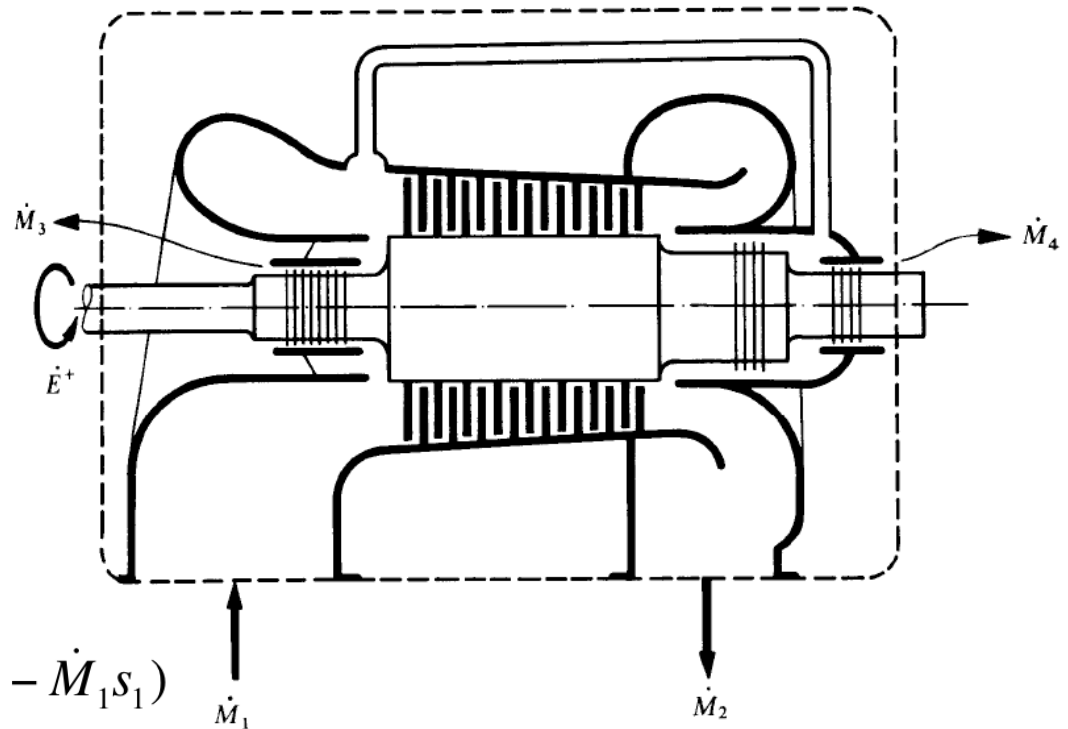


Fig. 10.43 A schematic representation of an axial compressor.

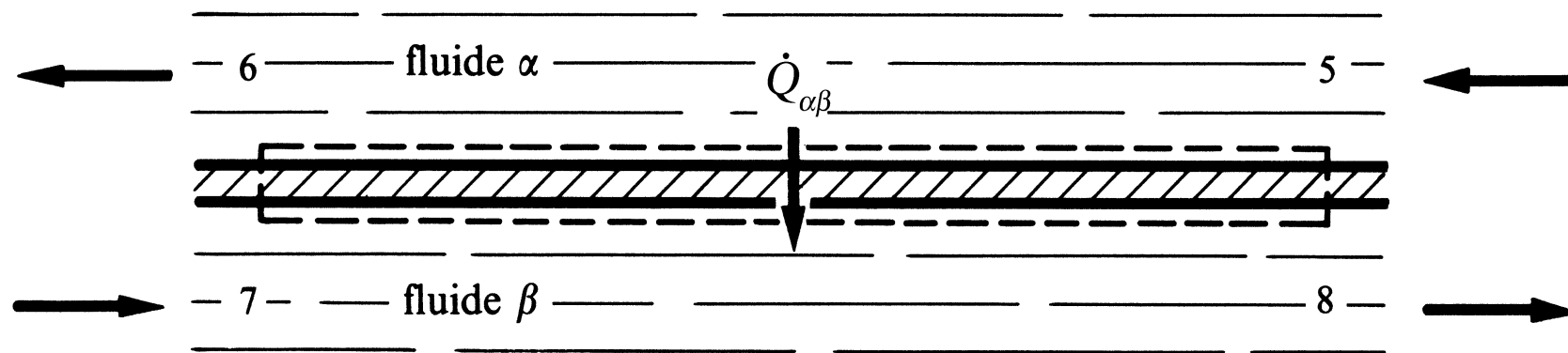
*fluid dissipation in the network (inlet, outlet, blades, channels, labyrinth seals)*

# Example of countercurrent HEX (steady state)

Heat transfer in counter-current between two fluids, steady state.

f.ex. fluid  $\beta$  heats up, evaporates, and superheats

(application: steam generator fluid ( $\beta$ ) heated by exit gas ( $\alpha$ ) of a gas turbine)



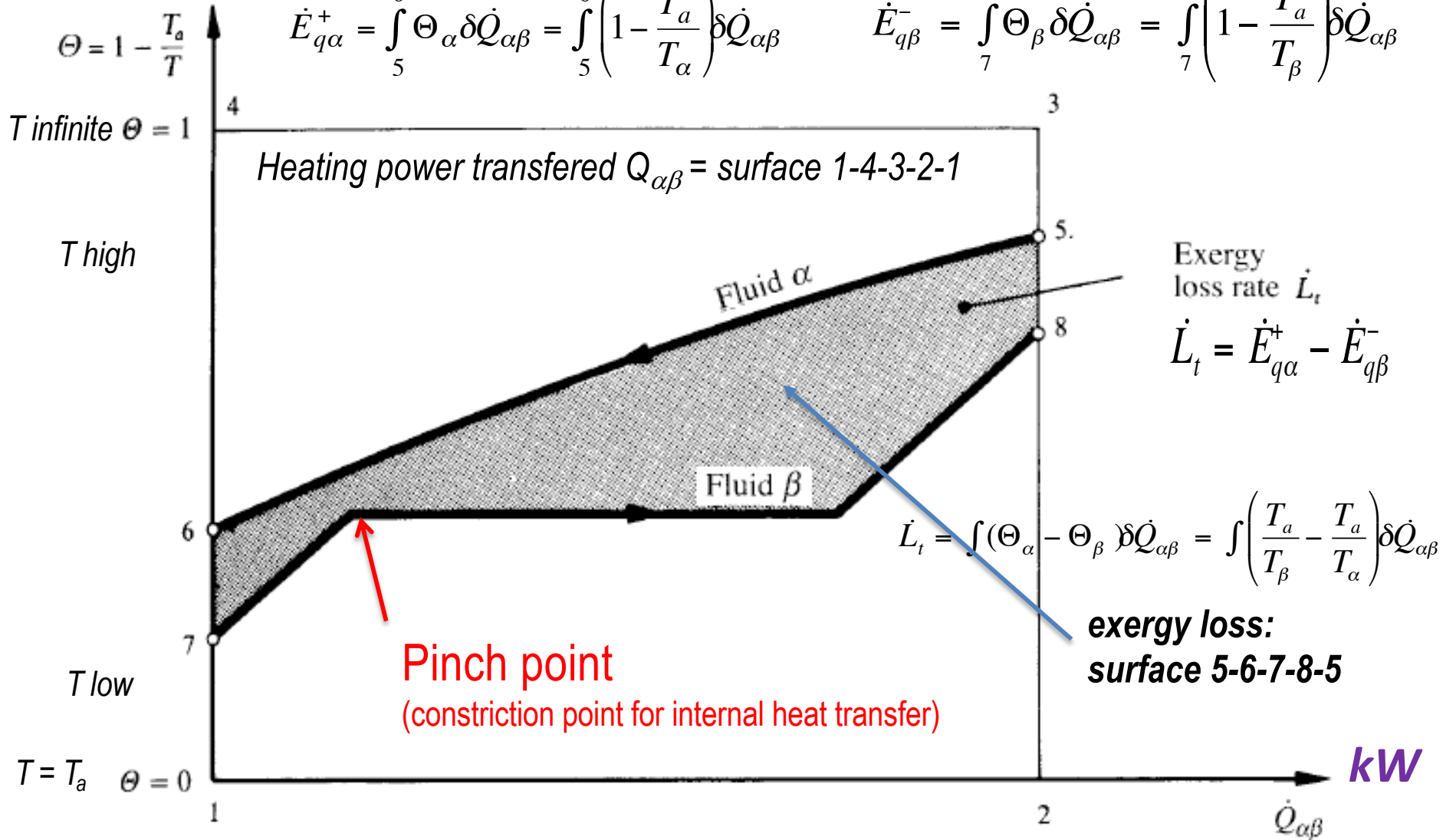
# => graphical representation, in terms of power (kW)

Heat-exergy received from  $\alpha$ :  
surface 2-5-6-1-2

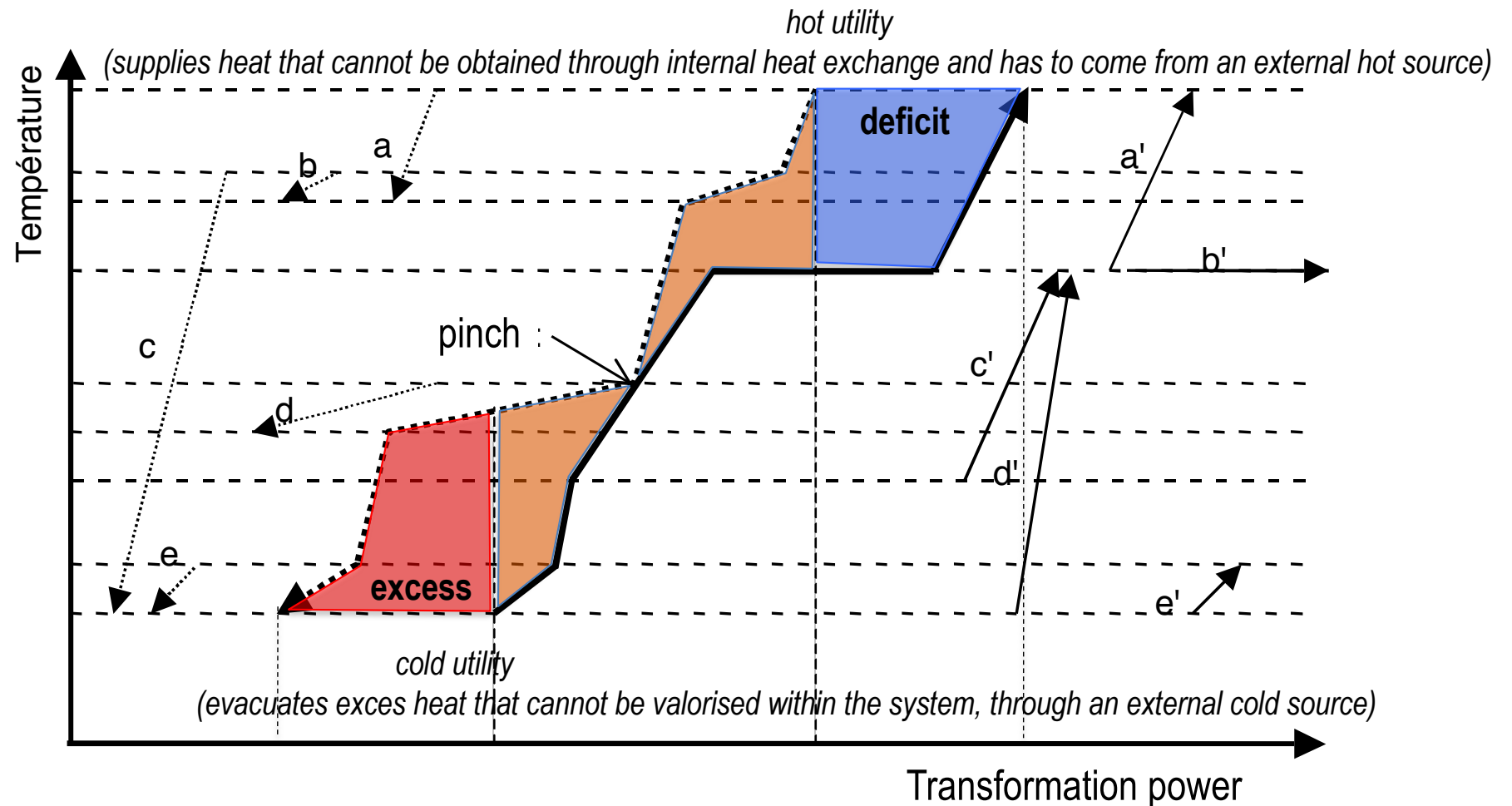
Heat-exergy given to  $\beta$ :  
surface 1-7-8-2-1

$$\dot{E}_{q\alpha}^+ = \int_5^6 \Theta_\alpha \delta\dot{Q}_{\alpha\beta} = \int_5^6 \left(1 - \frac{T_a}{T_\alpha}\right) \delta\dot{Q}_{\alpha\beta}$$

$$\dot{E}_{q\beta}^- = \int_7^8 \Theta_\beta \delta\dot{Q}_{\alpha\beta} = \int_7^8 \left(1 - \frac{T_a}{T_\beta}\right) \delta\dot{Q}_{\alpha\beta}$$



# => Pinch theory



All flows a, b, c, d, e are to cool → hot composite curve

All flows a', b', c', d', e' are to heat → cold composite curve

**Goal = maximise the internal heat transfer between the 2 composite curves**  
**(the orange zone represents the exergy losses due to internal heat transfer)**

# Comments

---

- basis for the conception of heat exchanger networks (HEN), and of the identification of hot and cold utilities; also indicates the possibility to introduce heat pump or cogeneration units in the system
- the pinch point fixes the limit which is possible to achieve with internal heat exchanges (crossing of the hot and cold composite curves)
- in practice, the  $\Delta T$  at the pinch cannot be zero (which would imply infinitely large heat exchanger surface); it is optimised for cost (=avoid too large heat exchanger surfaces) and pressure drop

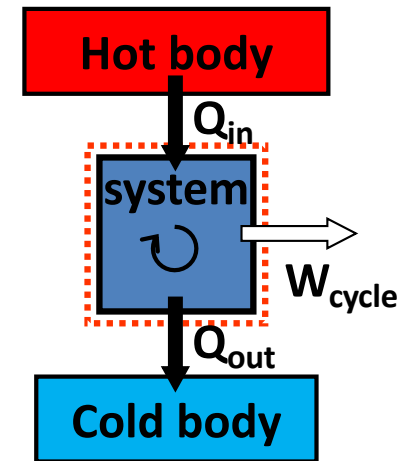
transferred power in a heat exchange =  $h.A.\Delta T$ , with:

$h$  = heat transfer coefficient ( $W/m^2.K$ ), material-dependent;

$A$  = exchange surface

# Power systems

- Produce net power output from an energy source, such as (fossil/renewable) fuel, nuclear, solar, biomass,...

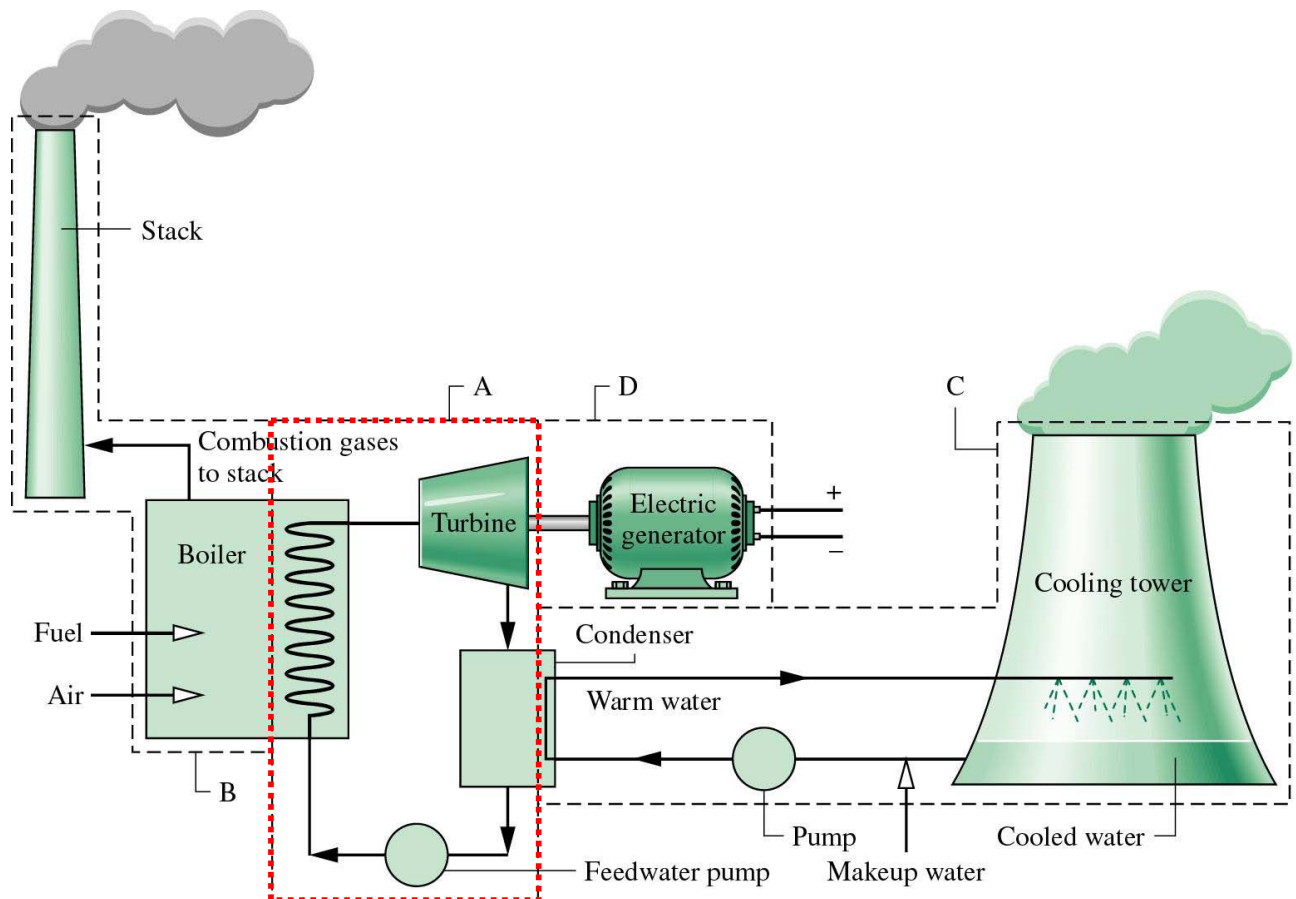


- Three major types of systems:
  - Vapor power plants (working fluid alternately vaporizes and condenses)
  - Gas turbine power plants (working fluid = gas, series of components)
  - Internal combustion engines (working fluid = gas, reciprocating)



# Vapor power systems

- Vapor power systems:
  - Water is the working fluid, which alternately vaporizes and condenses
  - **Majority of electrical power generation** done by these systems
  - Basic components in a simple system are:
    - Boiler
    - Turbine
    - Condenser
    - Pump



# Vapor power systems

- Idealized *Rankine* cycle:

- Turbine: *isentropic* expansion (1 → 2)

$$\dot{W}_t / \dot{m} = (h_1 - h_2)$$

- Condenser: *isobaric* heat transfer (2 → 3)

$$\dot{Q}_{\text{out}} / \dot{m} = (h_3 - h_2)$$

- Pump: *isentropic* compression (3 → 4)

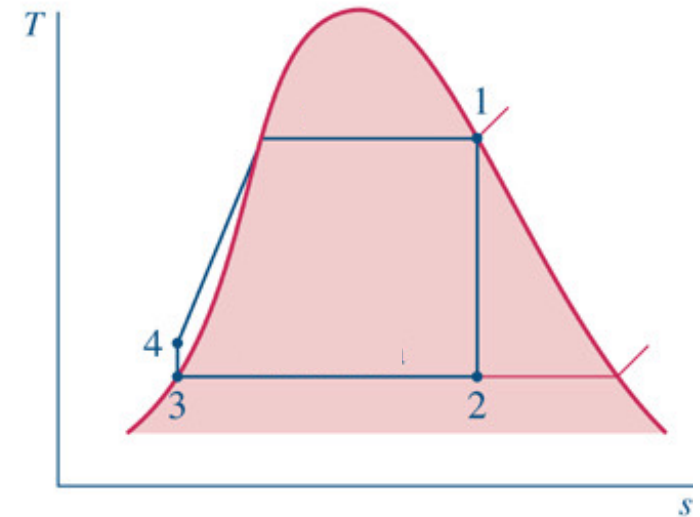
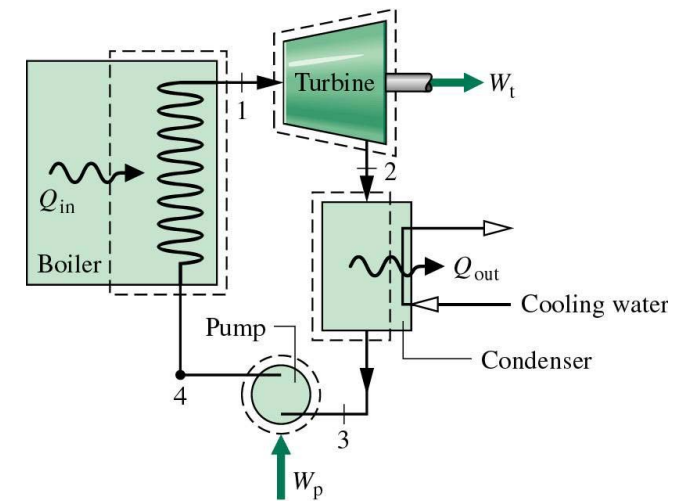
$$\dot{W}_p / \dot{m} = (h_3 - h_4)$$

- Boiler: *isobaric* heat transfer (4 → 1)

$$\dot{Q}_{\text{in}} / \dot{m} = (h_1 - h_4)$$

- Efficiency:

$$\eta = \frac{\dot{W}_t / \dot{m} + \dot{W}_p / \dot{m}}{\dot{Q}_{\text{in}} / \dot{m}} = \frac{(h_1 - h_2) + (h_3 - h_4)}{(h_1 - h_4)}$$

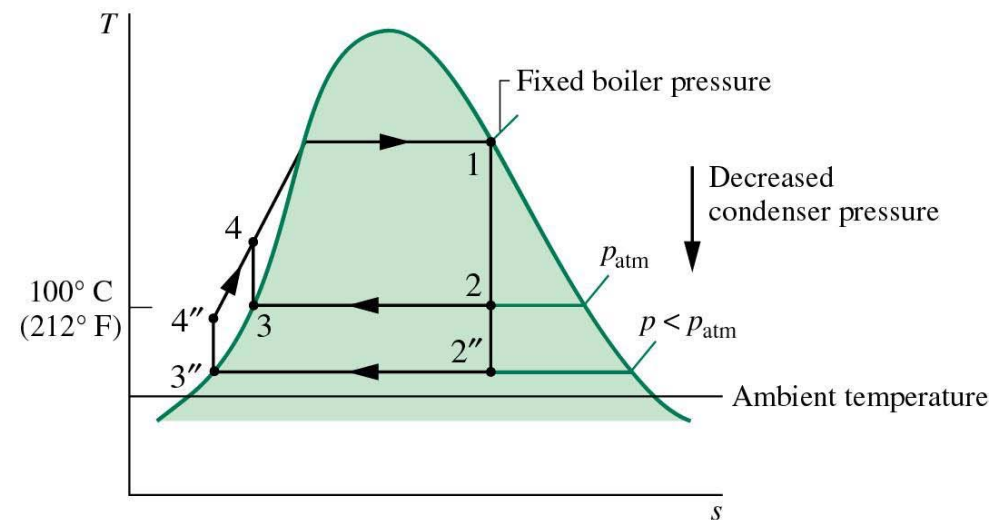
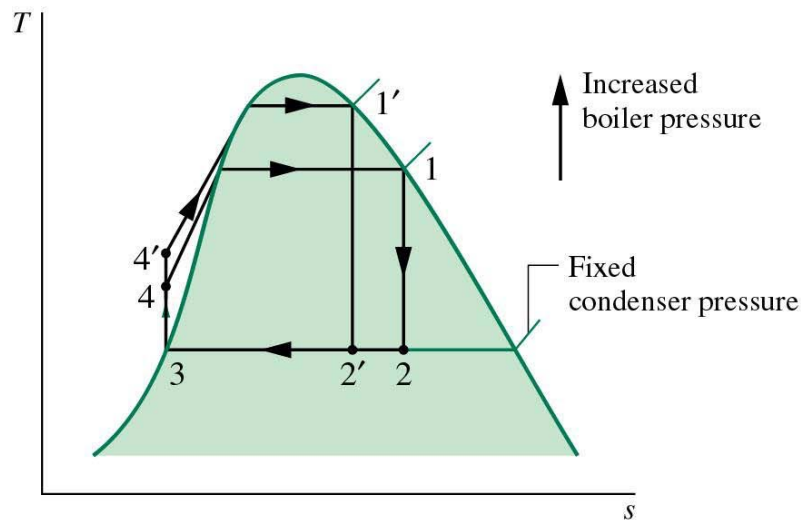


# Vapor power systems

- Idealized Rankine cycle: effects of components on performance:
  - Increase of average temperature at which energy is added and decrease of average temperature at which energy is rejected leads to increased efficiency (Carnot):

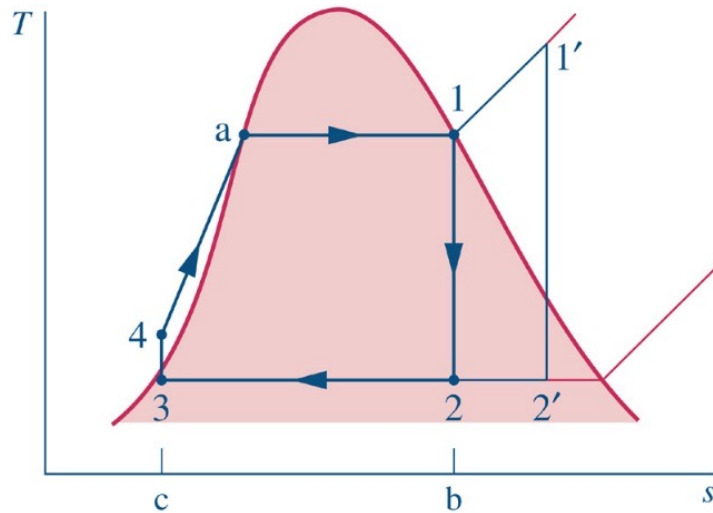
$$\eta_{\text{ideal}} = \frac{(\dot{Q}_{\text{in}} / \dot{m})_{\text{int,rev}} - (\dot{Q}_{\text{out}} / \dot{m})_{\text{int,rev}}}{(\dot{Q}_{\text{in}} / \dot{m})_{\text{int,rev}}} = 1 - \frac{T_{\text{out}}}{\bar{T}_{\text{in}}}$$

- Increase in boiler pressure and decrease in condenser pressures:



# Vapor power systems

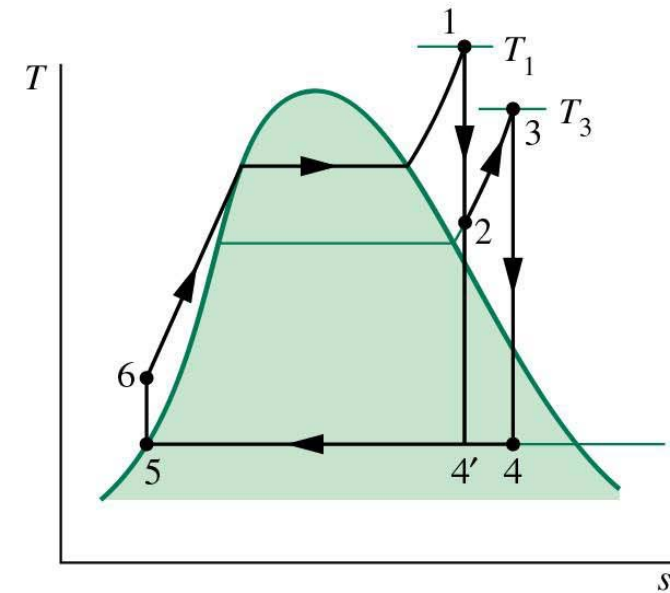
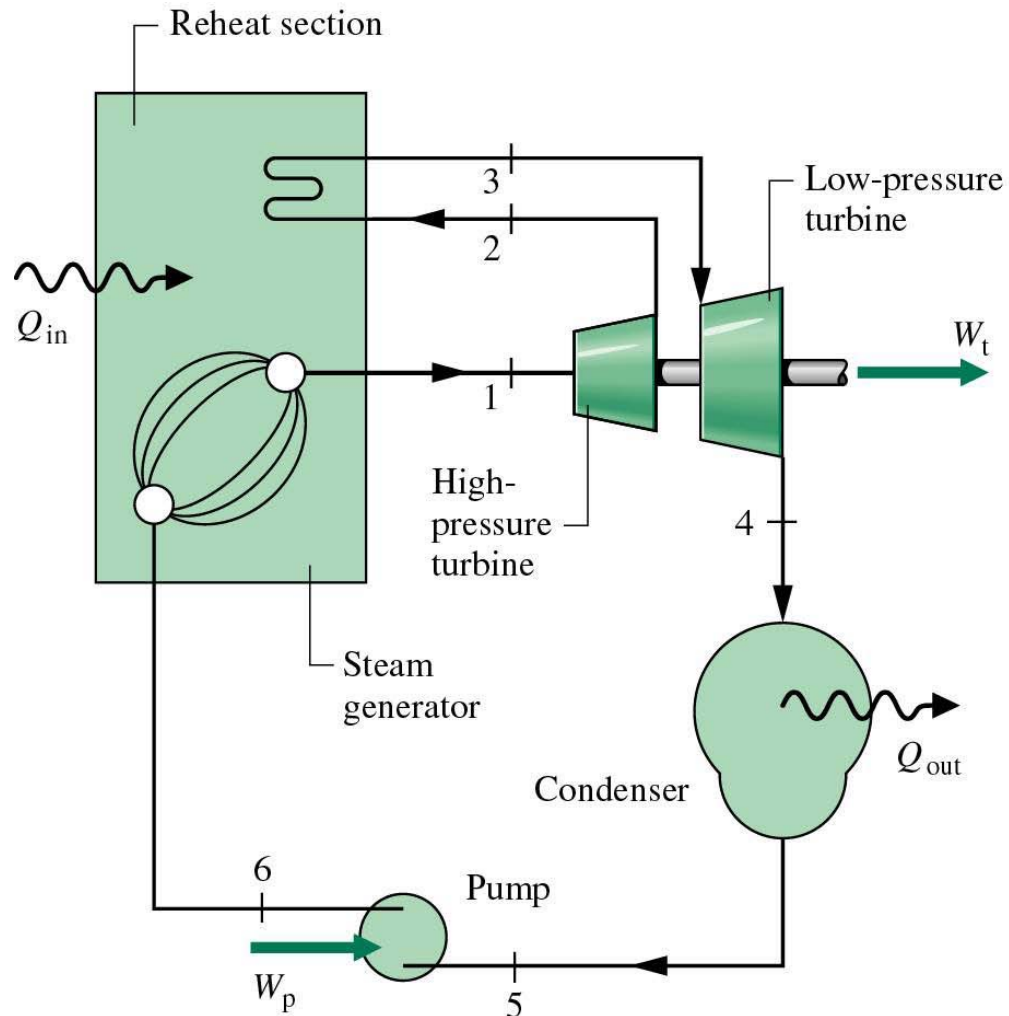
- Rankine cycle: improving performance:
  - **1.Superheating** (using additional heat exchanger, combination of boiler and heat exchanger is called steam generator)



Protects turbine (higher vapor quality  $x$ ) & increases efficiency (higher  $T$ )

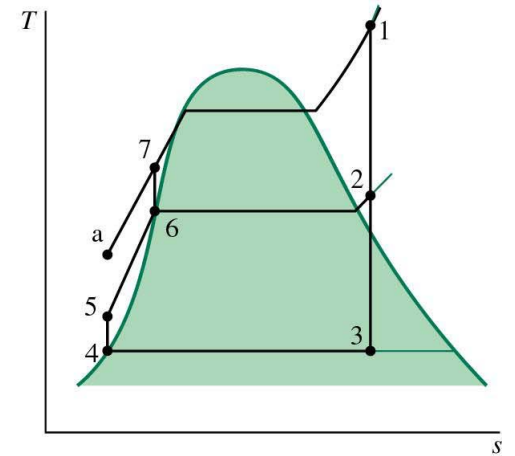
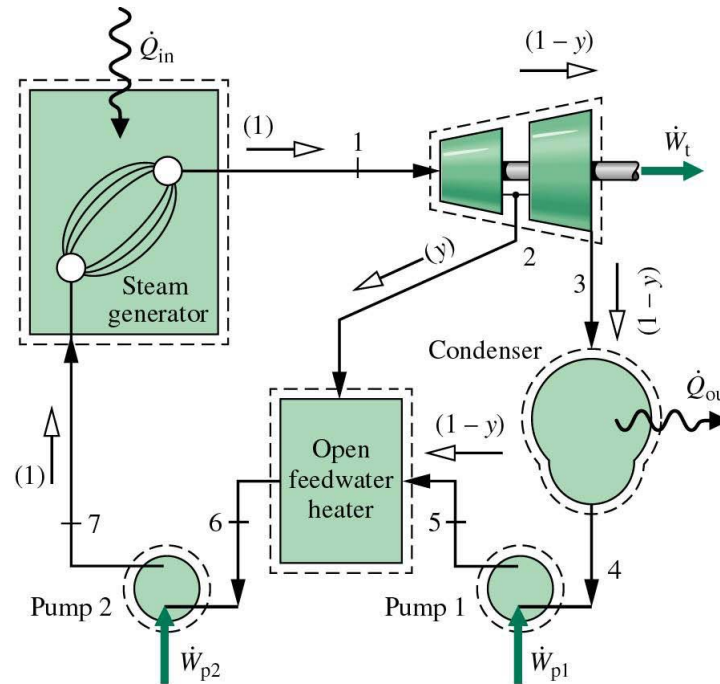
# Vapor power systems

- Rankine cycle: improving performance:
  - 2.Reheating

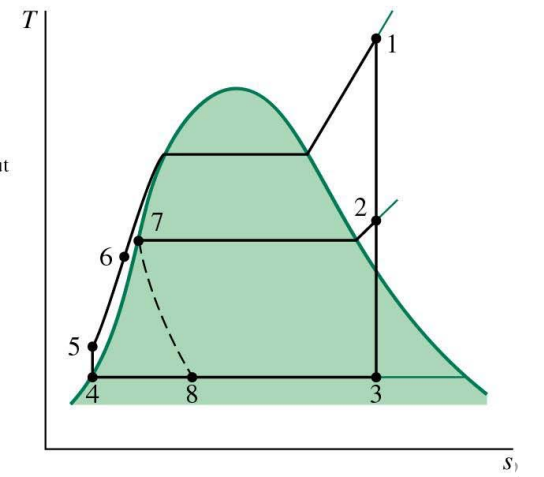
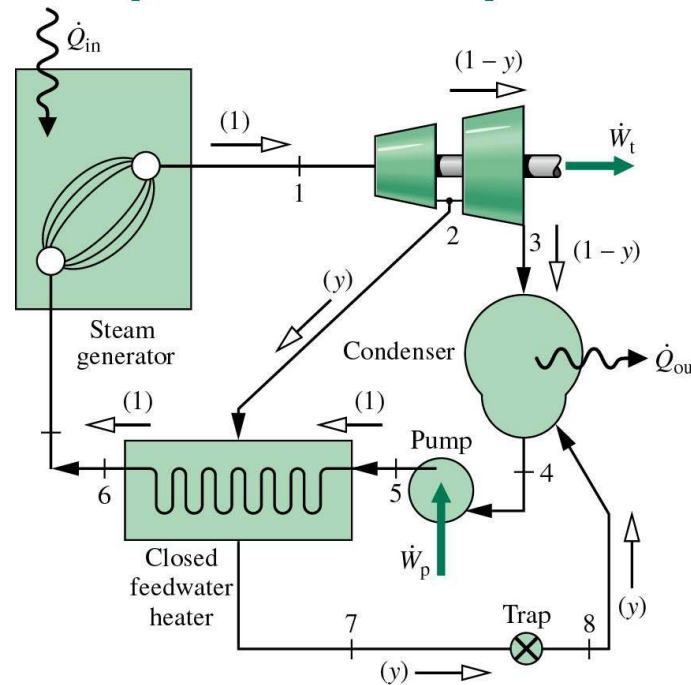


# Vapor power systems

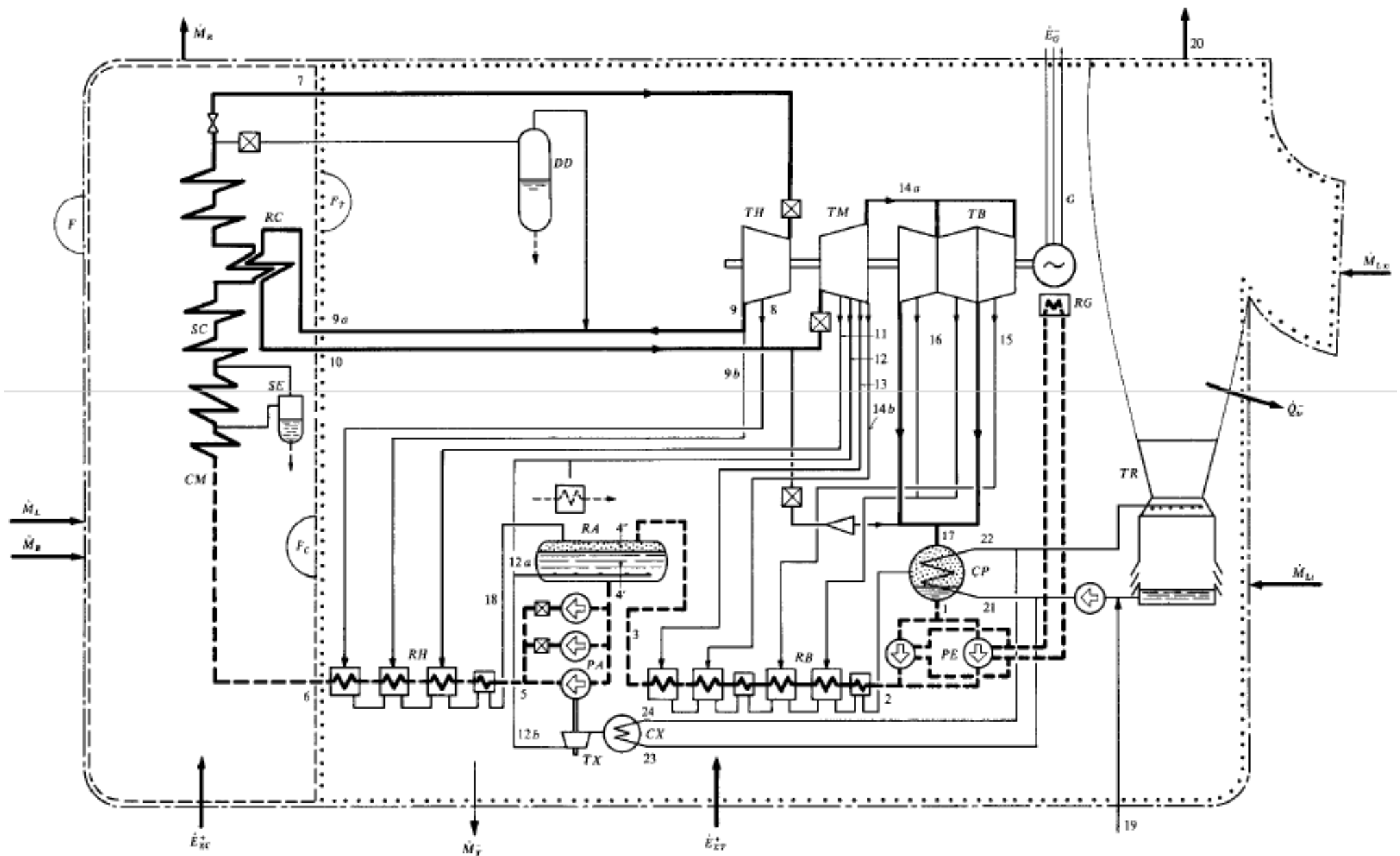
- Rankine cycle: improving performance:
  - **3.Regeneration** via open feedwater heater



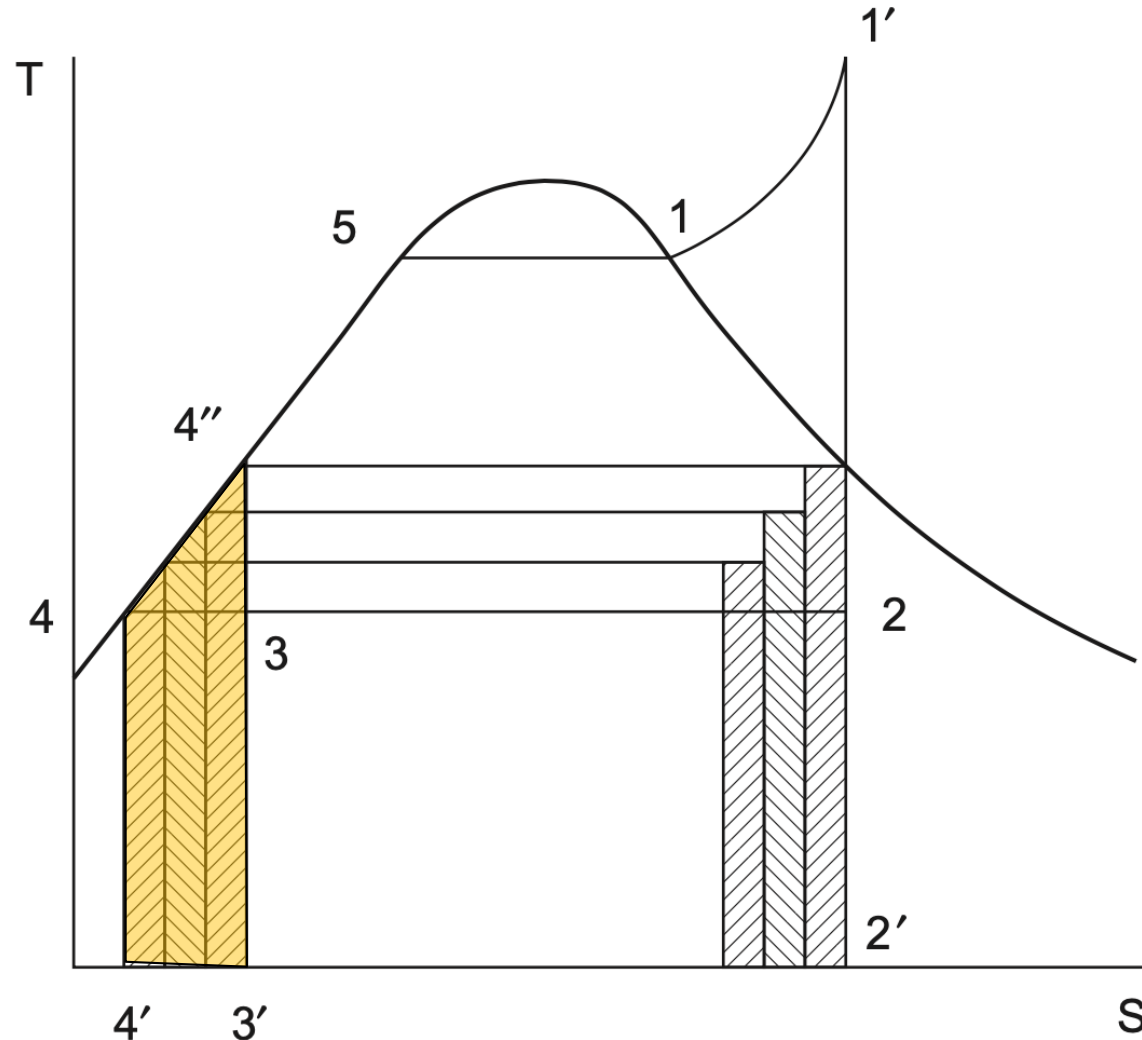
closed feedwater heater



# Real steam plant example:



# Multistage extraction



Heat addition to the cycle is reduced from the area bounded by  $4'-4-4''-5-1-1'-2-2'-4'$  to the area bounded by  $3'-3-4''-5-1-1'-2-2'-3'$ , hence the heat addition to the cycle is reduced by the area  $4'-4-4''-3-3'-4'$ , keeping the output unchanged, thereby reducing the cost of power generation.



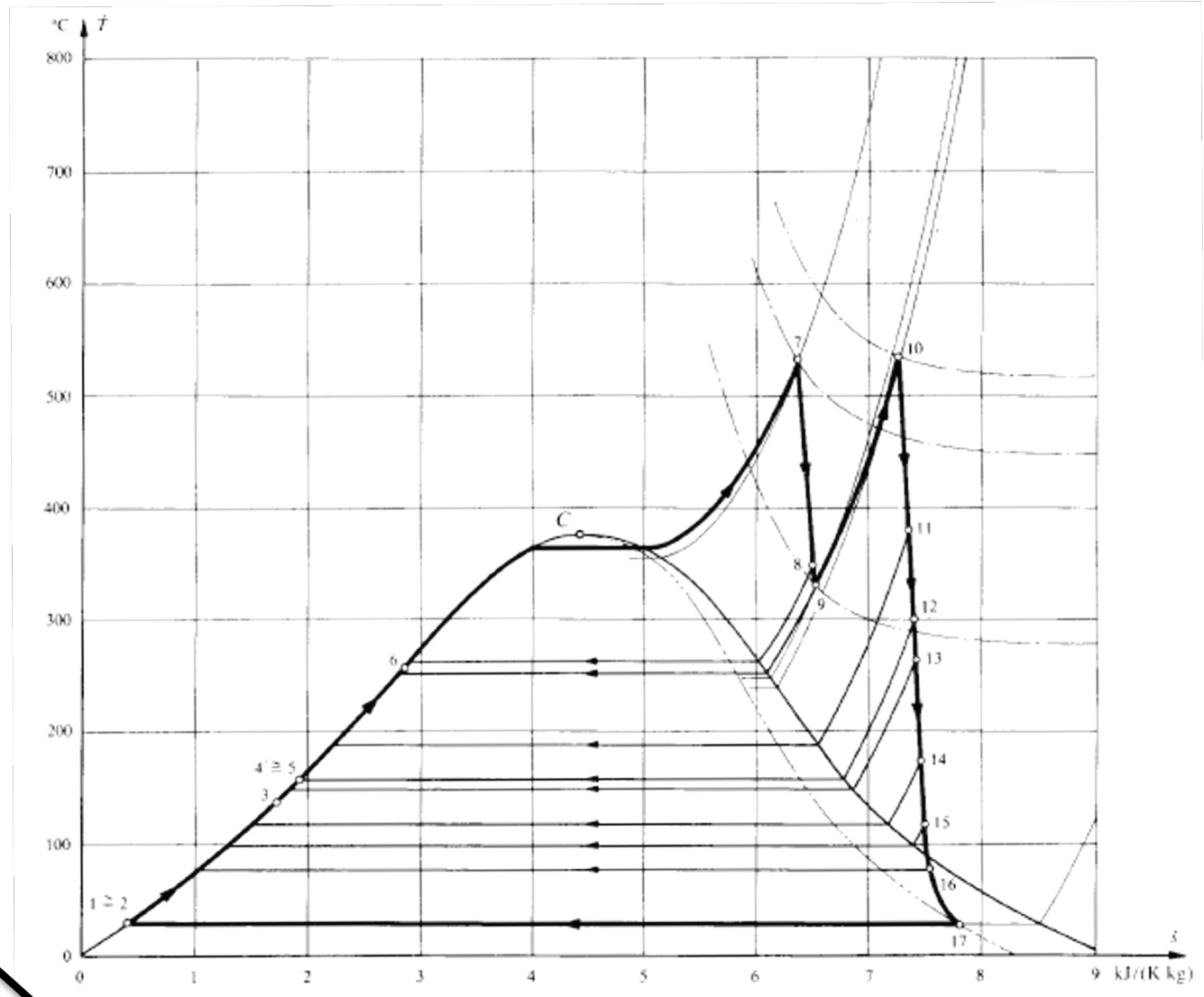
# Real steam plant example:

- 2 \* 150 MW<sub>e</sub>
- 8 extractions
- 1 reheater;  
for feed-water at HP  
and LP
- 5 turbines  
(1 HP, 1 MP, 3 LP)
- 2 cooling towers

$$\epsilon_{\text{Turbogroup}} = 75\%$$

$$\epsilon_{\text{Boiler}} = 52\%$$

$$\epsilon_{\text{Plant}} = \epsilon_{\text{TG}} \cdot \epsilon_{\text{Boiler}} = 39\%$$

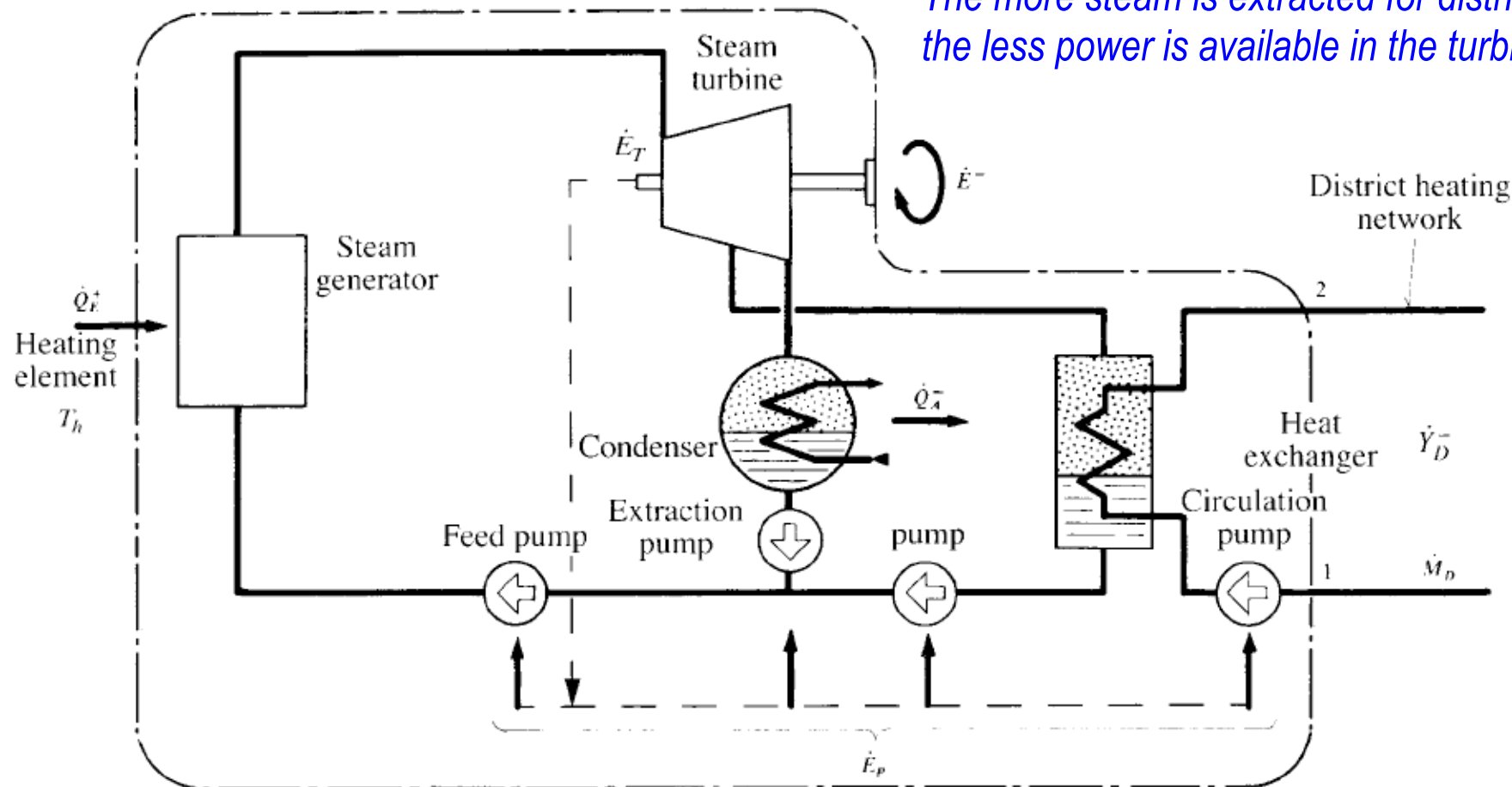


= the main exergy loss (large  $T$  drop)  $\leftrightarrow$  1<sup>st</sup> law : 94%

# Co-generation

- Power and heat:
  - steam extraction to HEX for district heating (70°C)
  - output service: power  $\dot{E}^-$  and enthalpy  $\dot{Y}_D^-$

*The more steam is extracted for district heating, the less power is available in the turbine*

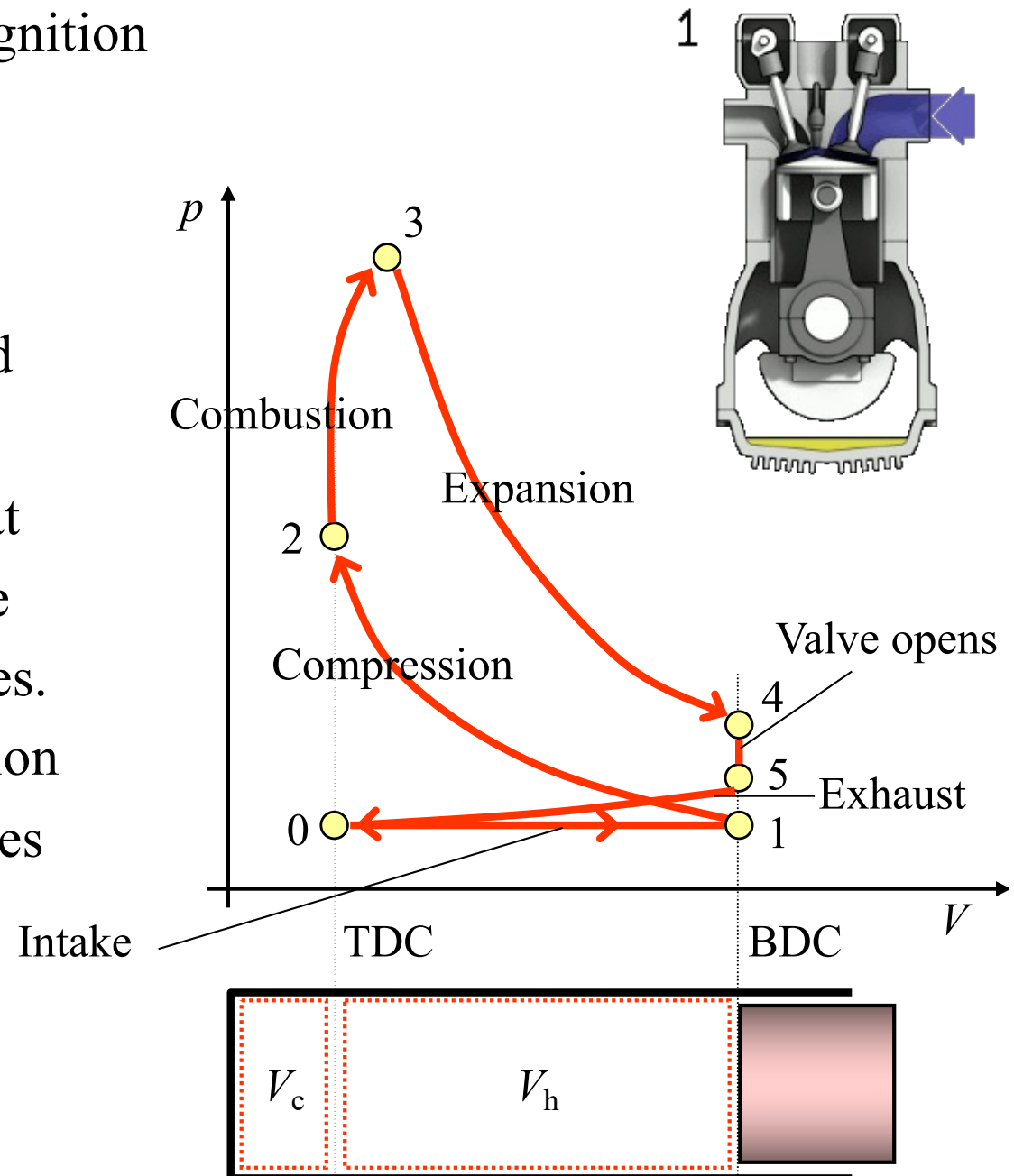


# Internal combustion engines

- Spark ignition or compression ignition

- *Air-standard analysis:*

- Fixed amount of air modeled as ideal gas
- Combustion modeled by heat transfer from external source
- No exhaust and intake strokes. Constant volume heat rejection
- Internally reversible processes



# Internal combustion engines

- Air-standard **Otto** cycle:

- 1-2: Isentropic compression

$$\frac{W_{12}}{m} = u_1 - u_2 \quad (<0)$$

- 2-3: Constant-volume heat transfer

$$\frac{Q_{23}}{m} = u_3 - u_2$$

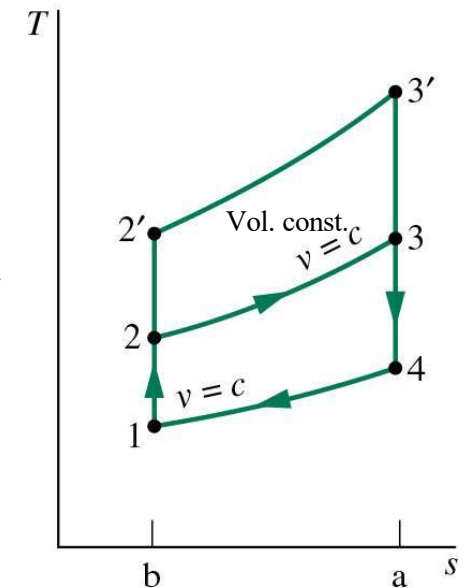
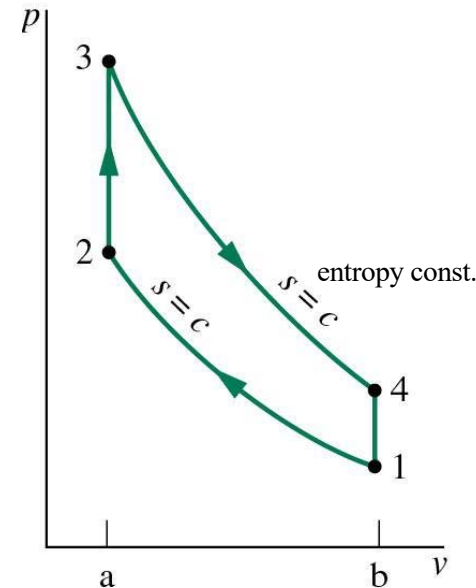
- 3-4: Isentropic expansion

$$\frac{W_{34}}{m} = u_3 - u_4$$

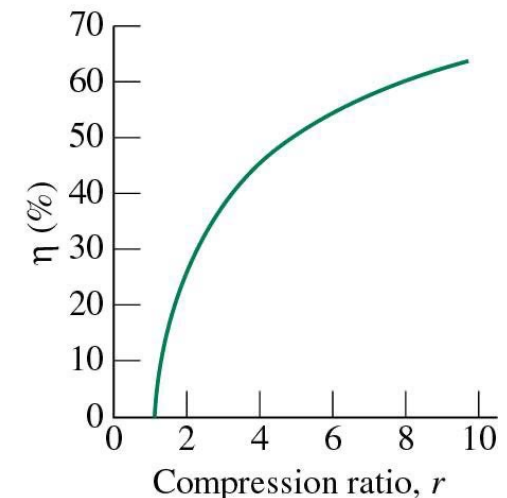
- 4-1: Constant-volume heat rejection

$$\frac{Q_{41}}{m} = u_1 - u_4 \quad (<0)$$

- Cycle efficiency:  $\eta = \frac{W_{\text{cycle}}}{Q_{23}} = \frac{u_3 - u_4 + u_1 - u_2}{u_3 - u_2}$



$$\text{Compression ratio: } r = \frac{V_1}{V_2} = \frac{V_4}{V_3}$$



# Internal combustion engines

- Air-standard **Diesel** cycle:
  - 1-2: Isentropic compression

$$\frac{W_{12}}{m} = u_1 - u_2$$

- 2-3: Constant-pressure heat transfer

$$\frac{W_{23}}{m} = p_2(v_3 - v_2) \quad \frac{Q_{23}}{m} = u_3 - u_2 + \frac{W_{23}}{m}$$

- 3-4: Isentropic expansion

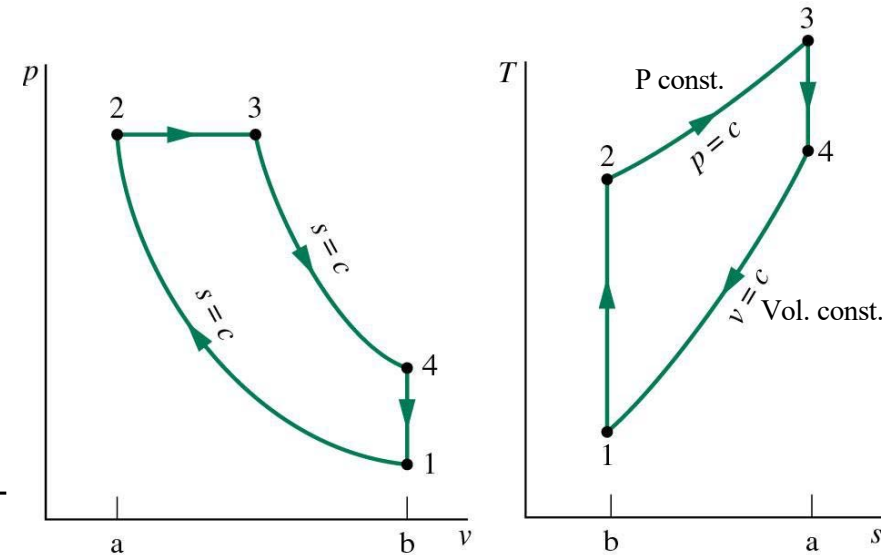
$$\frac{W_{34}}{m} = u_3 - u_4$$

- 4-1: Constant-volume heat rejection

$$\frac{Q_{41}}{m} = u_1 - u_4$$

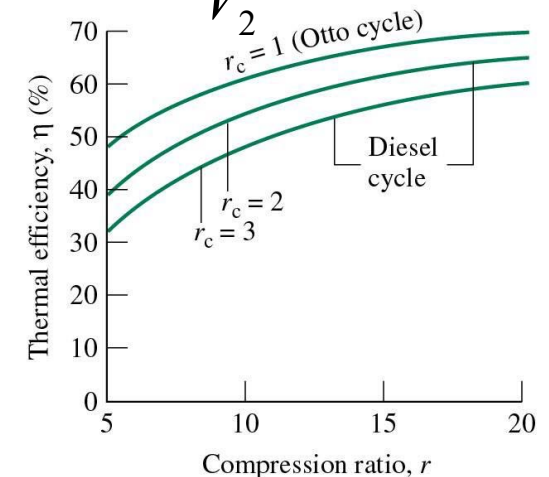
- Cycle efficiency:

$$\eta = \frac{W_{\text{cycle}}}{Q_{23}} = \frac{h_3 - h_2 - u_4 + u_1}{h_3 - h_2}$$



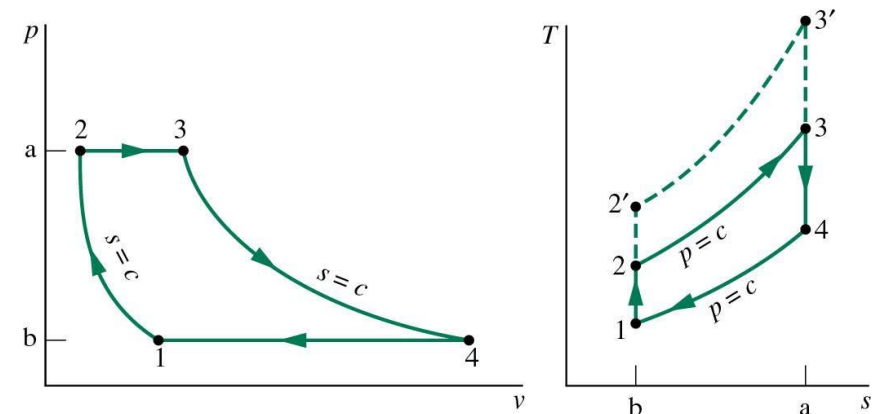
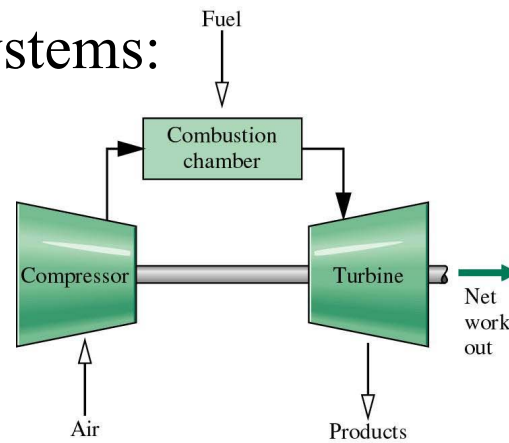
Compression ratio:  $r = \frac{V_1}{V_2} = \frac{V_4}{V_3}$

Cut-off ratio:  $r_c = \frac{V_3}{V_2}$



# Gas turbine power plants

- Gas turbine systems:



- Air-standard Brayton cycle (ideal):

- 1-2: Isentropic compression  $\frac{\dot{W}_{12}}{\dot{m}} = h_1 - h_2$

- 2-3: Isobaric heat transfer  $\frac{Q_{23}}{\dot{m}} = h_3 - h_2$

- 3-4: Isentropic expansion  $\frac{\dot{W}_{34}}{\dot{m}} = h_3 - h_4$

- 4-1: Isobaric heat transfer  $\frac{Q_{41}}{\dot{m}} = h_1 - h_4$

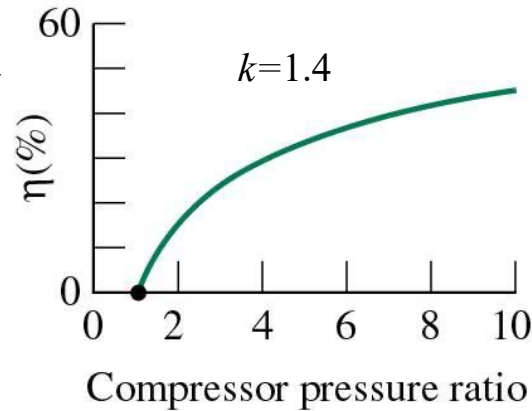
Cycle efficiency:

$$\eta = \frac{W_{\text{cycle}}}{Q_{23}} = \frac{h_3 - h_4 + h_1 - h_2}{h_3 - h_2}$$

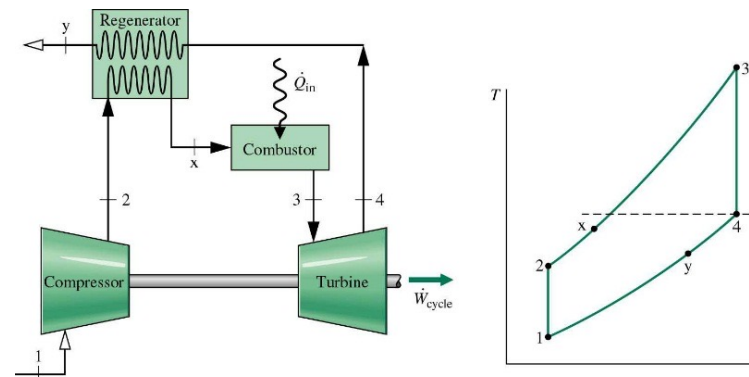
# Gas turbine power plants

- Air-standard Brayton cycle: pressure ratio effect on performance

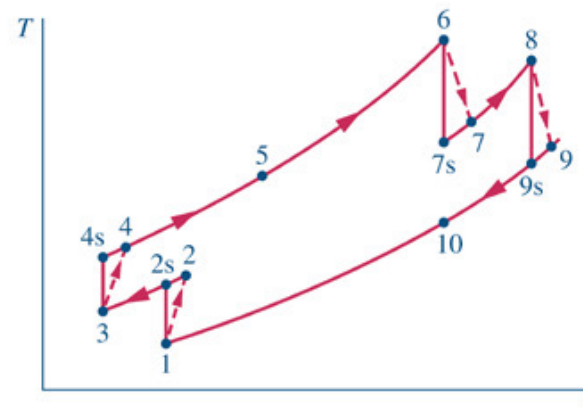
- Efficiency increases with increasing pressure ratio



- Regeneration:



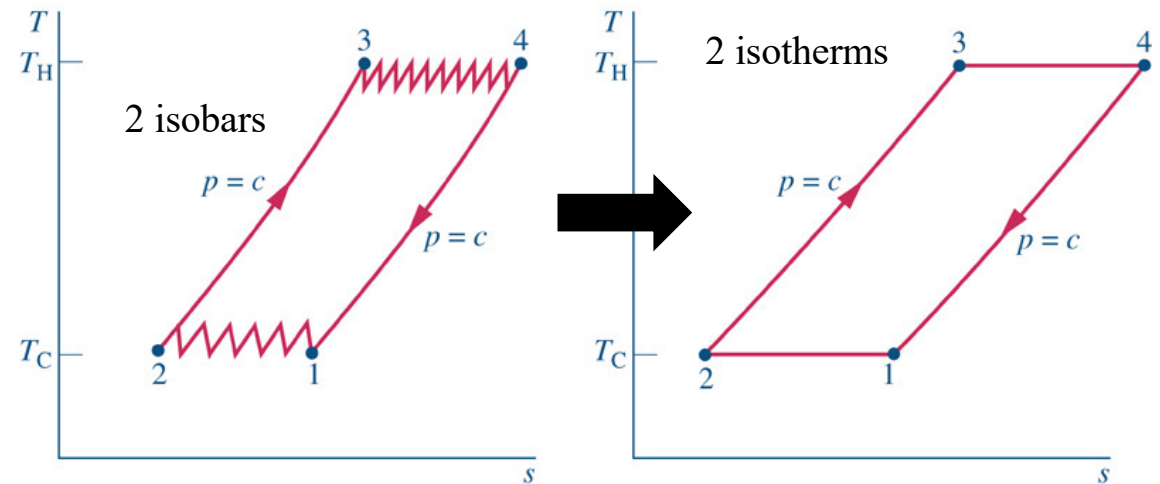
- Reheating and intercooling:



# External combustion engines

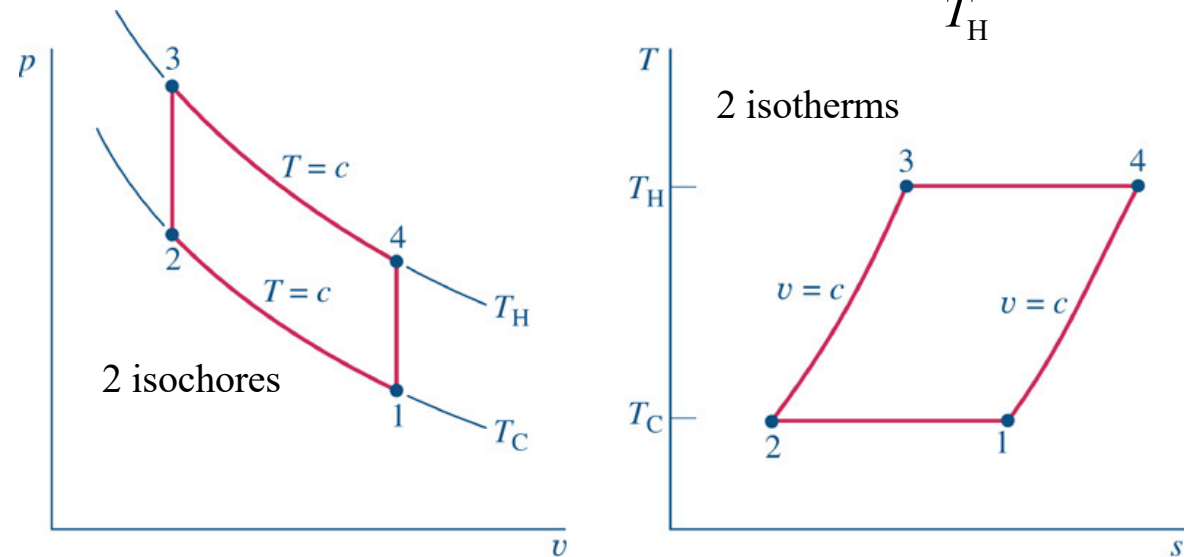
- Ericsson and Stirling cycle (both with same features as Carnot):

- In the limit of large number of multi-stage compression with inter-cooling, and multi-stage expansion with re-heating, with ideal regeneration



$$\eta_{\text{th}} = 1 - \frac{T_C}{T_H}$$

- Cycle with regeneration, internally reversible, internal heat transfer processes → Stirling cycle





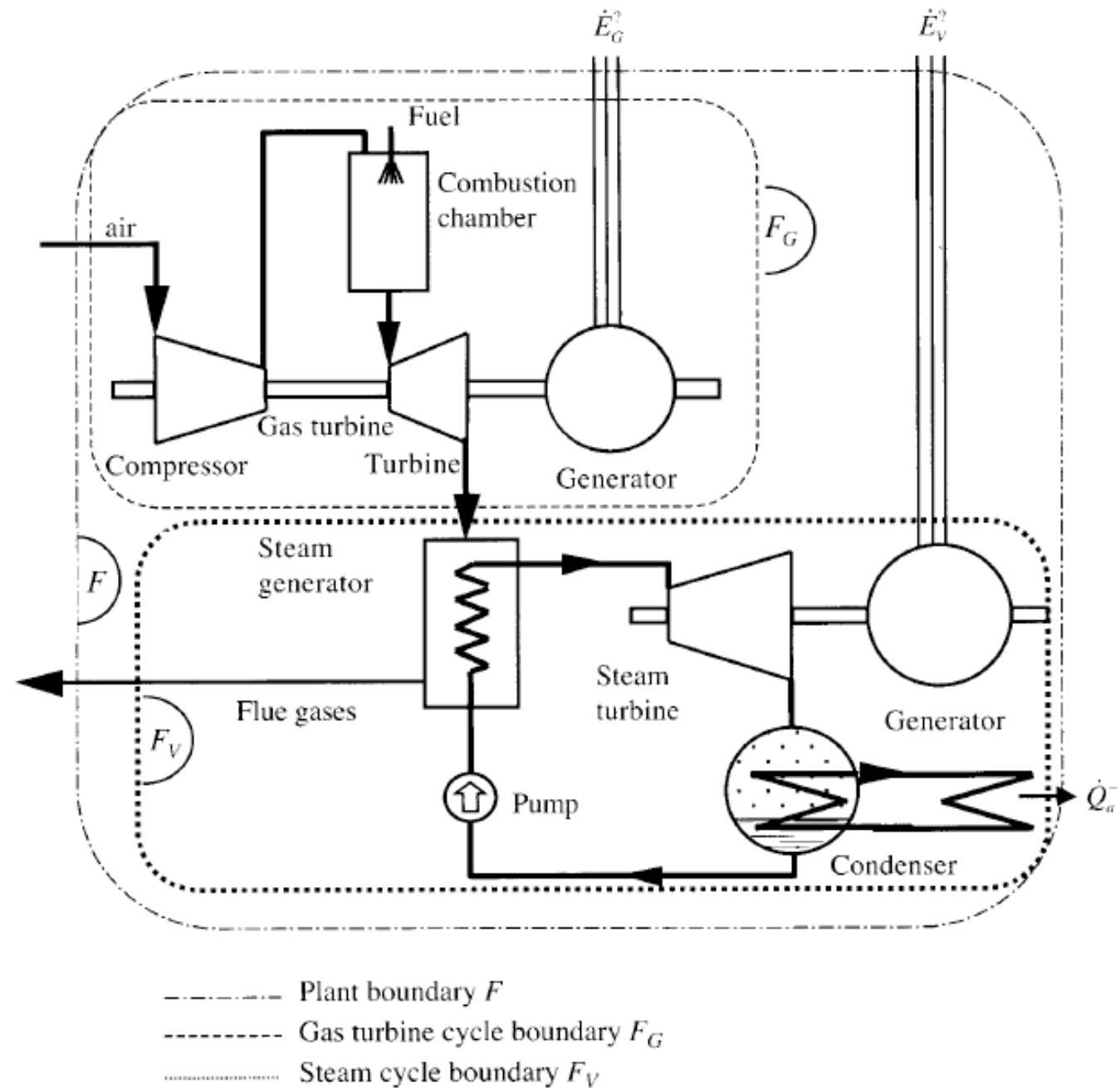
# Combined cycle (CC)

---

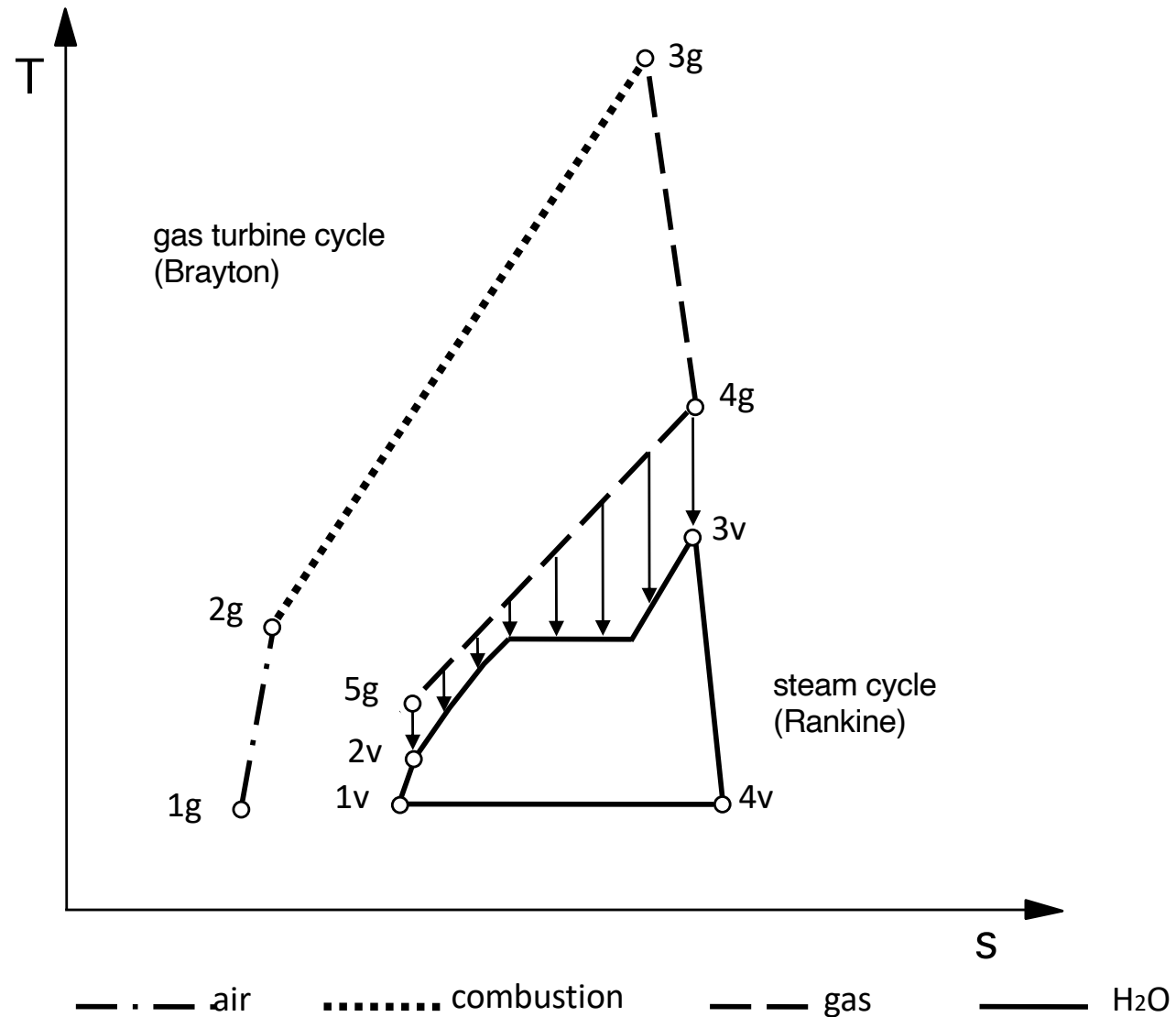
- Gas cycle + steam cycle
  - Fuels: oil, natural gas, gasified coal fuels
  - GT on top of ST (*'topping cycle'*) **reduces exergy heat transfer loss** between fuel combustion gases and steam
  - ST below the GT (*'bottoming cycle'*) **reduces heat exergy loss** of the hot GT exhaust gas (450-650°C)
- *'win' – 'win'* combination between both cycles
- the individual cycles in a CC configuration find themselves simplified with respect to their stand-alone configurations:
- for the GT: no regenerator (it becomes the steam heater)
  - for the ST: almost no steam extraction

# Layout

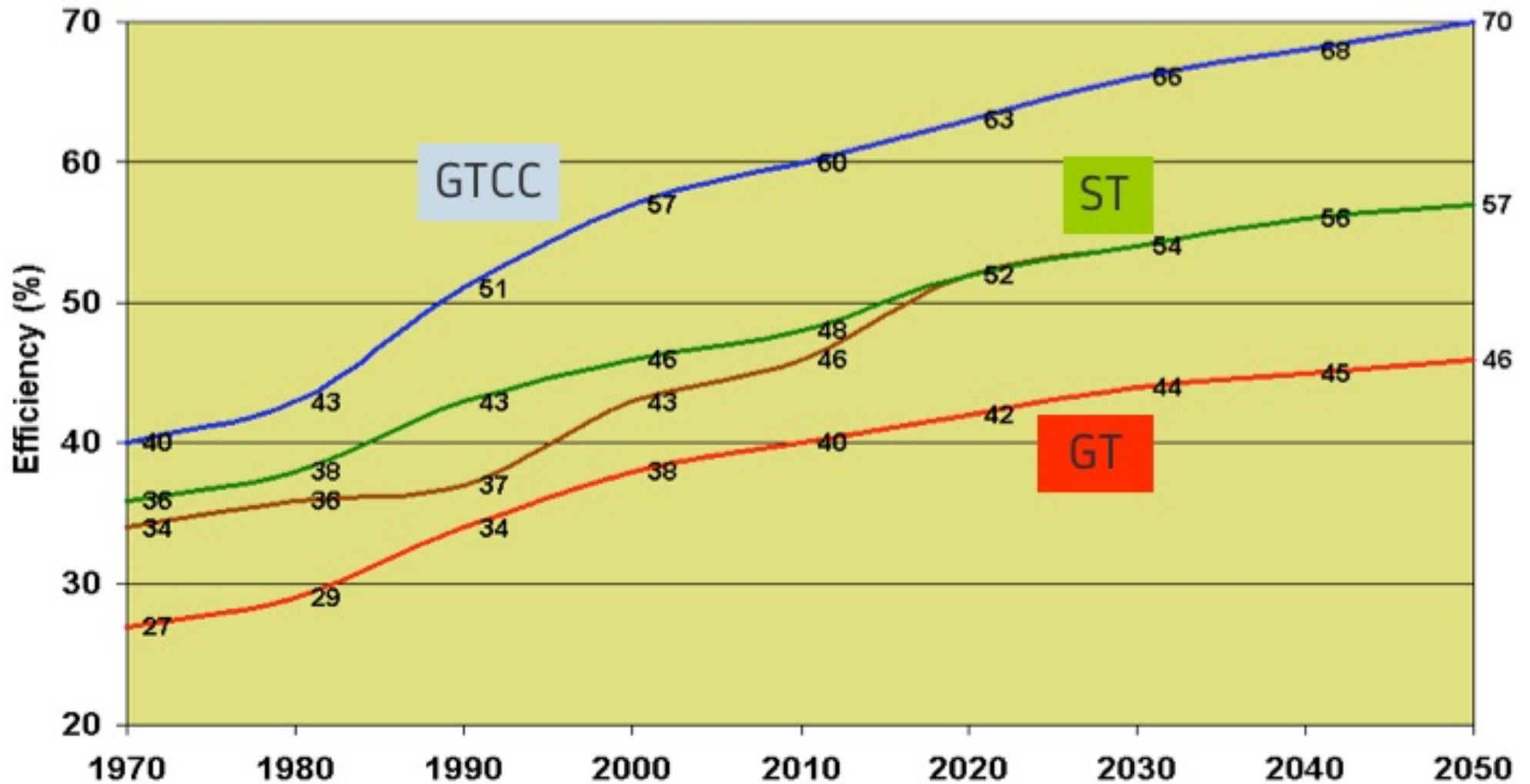
(no cogen.)



# Combined gas-steam cycle in $T-s$ diagram

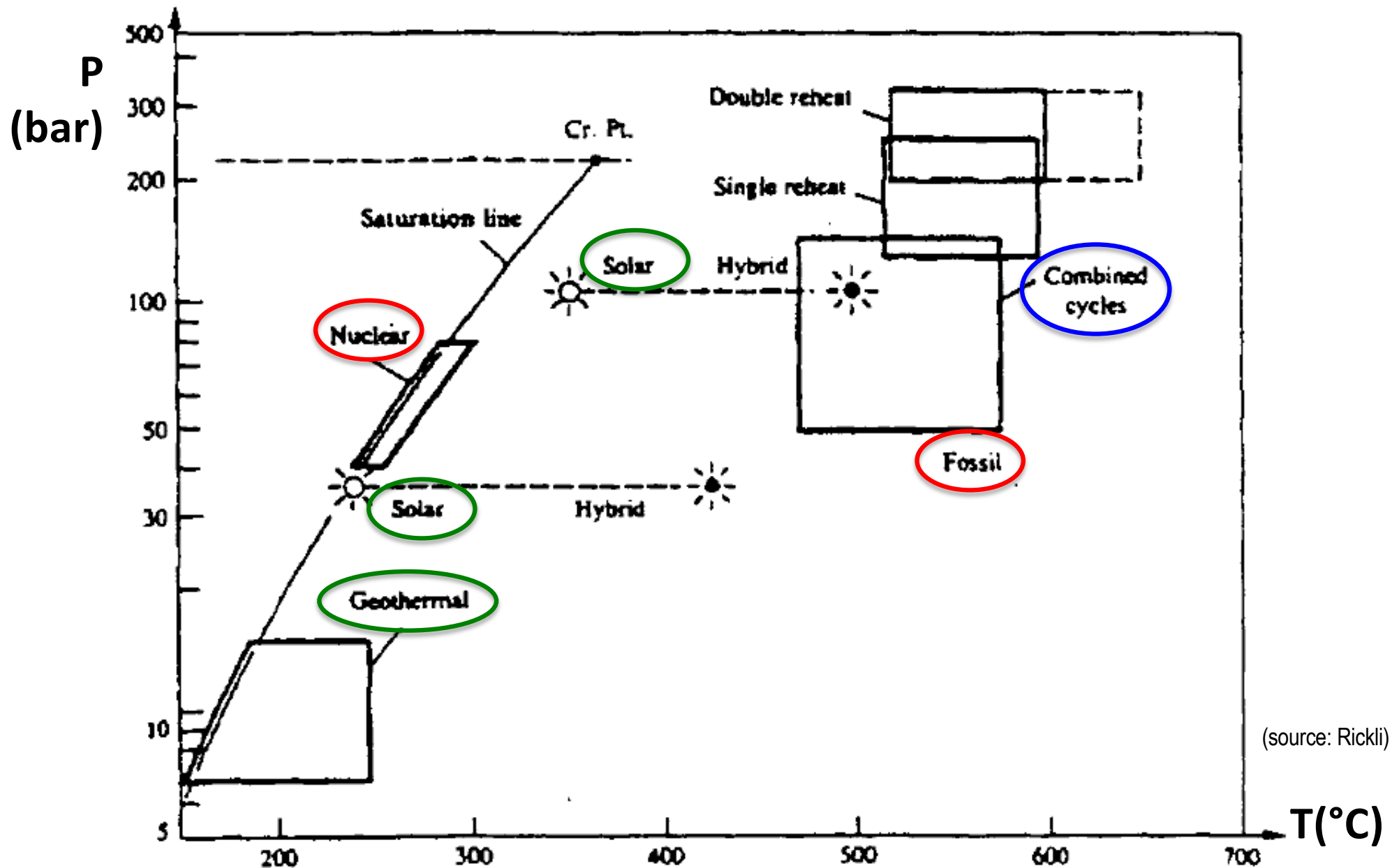


# Efficiency evolution and perspectives



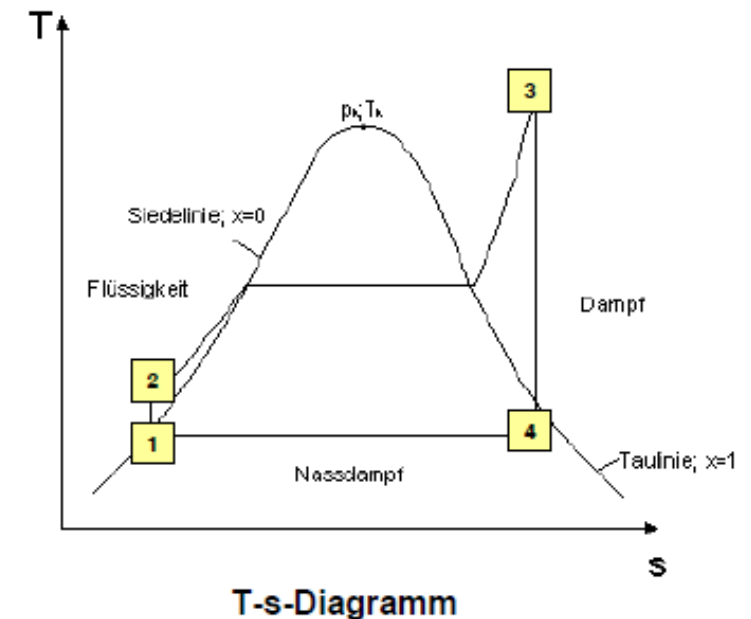
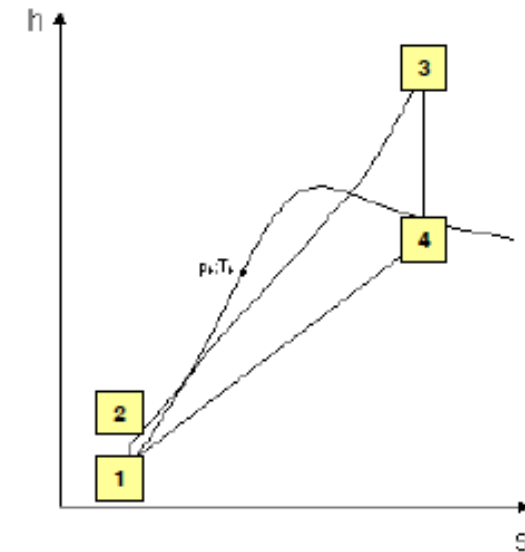
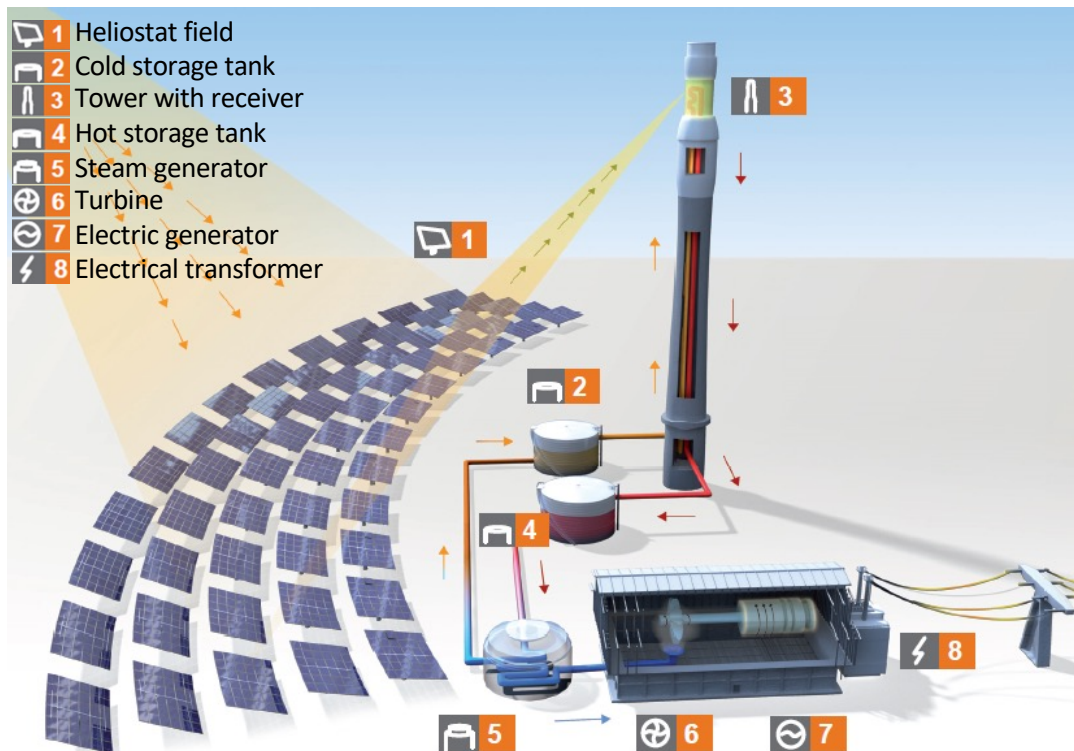
(T. Kaiser, Alstom)

# Steam $P$ - $T$ diagram for various cycle applications



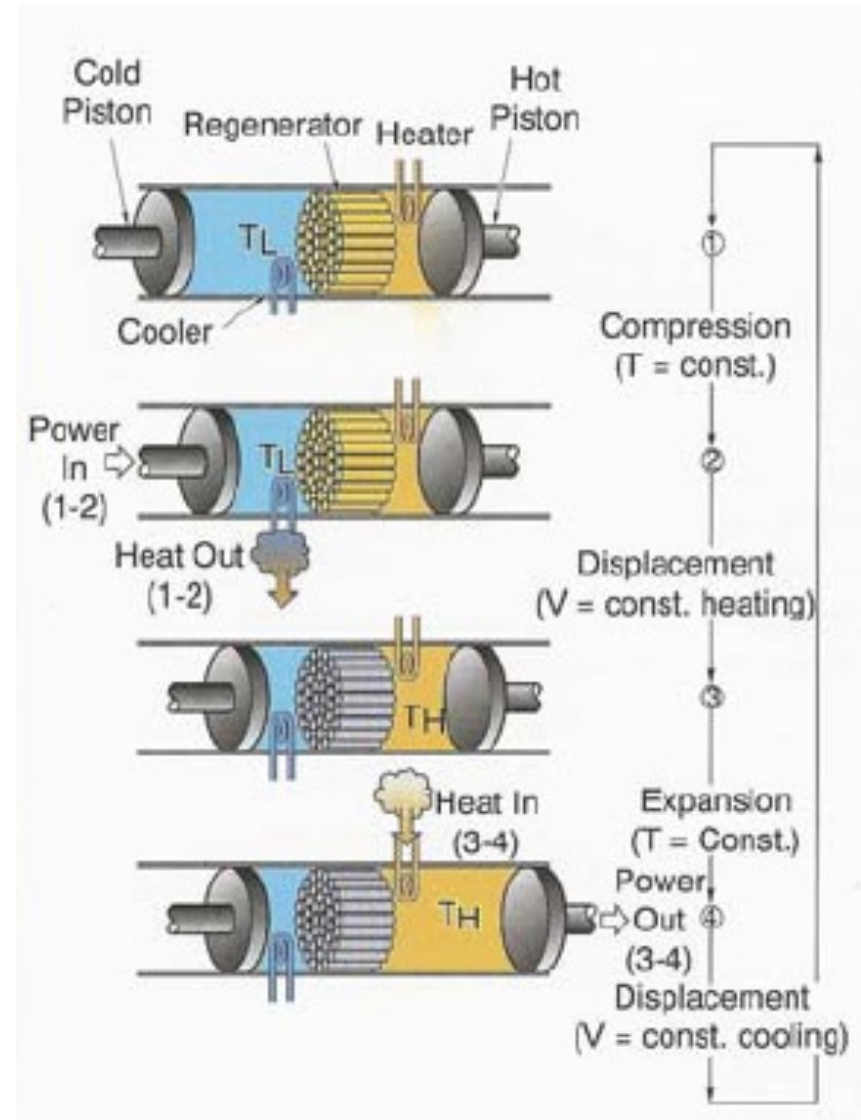
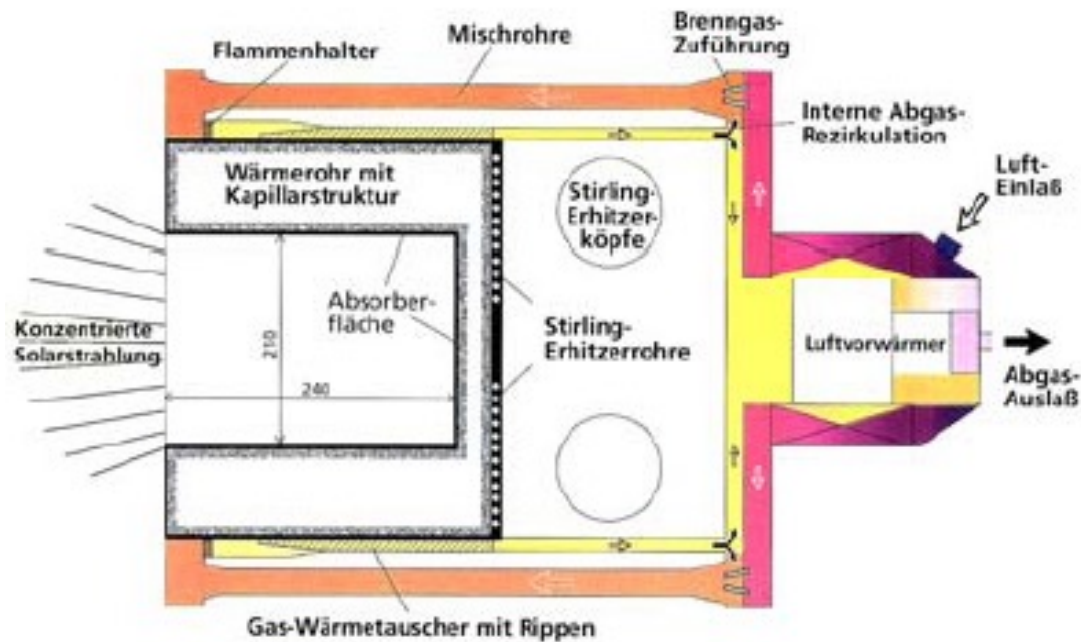
# Concentrated Solar Power - Centralized

- Traditional Rankine cycle:



# Concentrated Solar Power - Decentralized

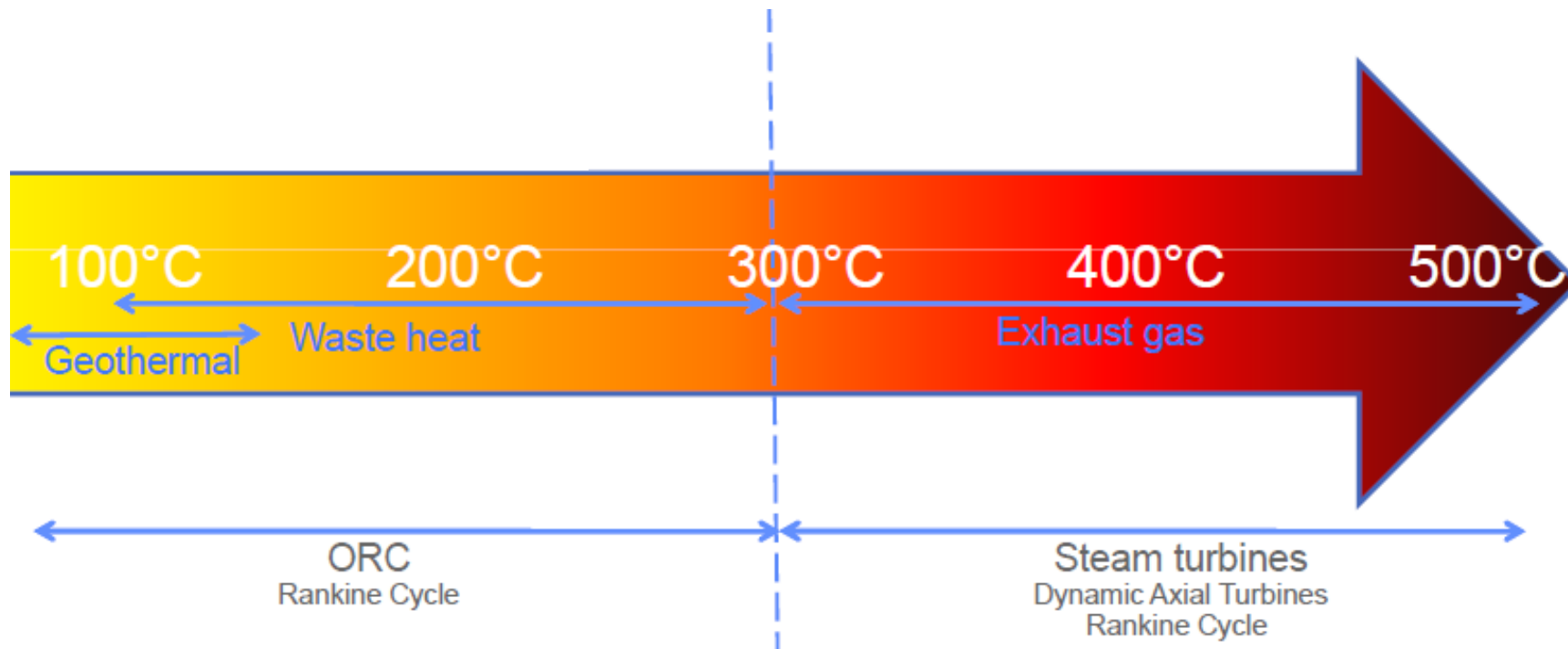
- Stirling cycle:





# Low temperature heat sources

- For **geothermal, waste heat**, non- / low-concentrated solar:
  - temperatures too low for water as HTF (heat transfer fluid)
  - instead using (organic) fluid with different critical parameters

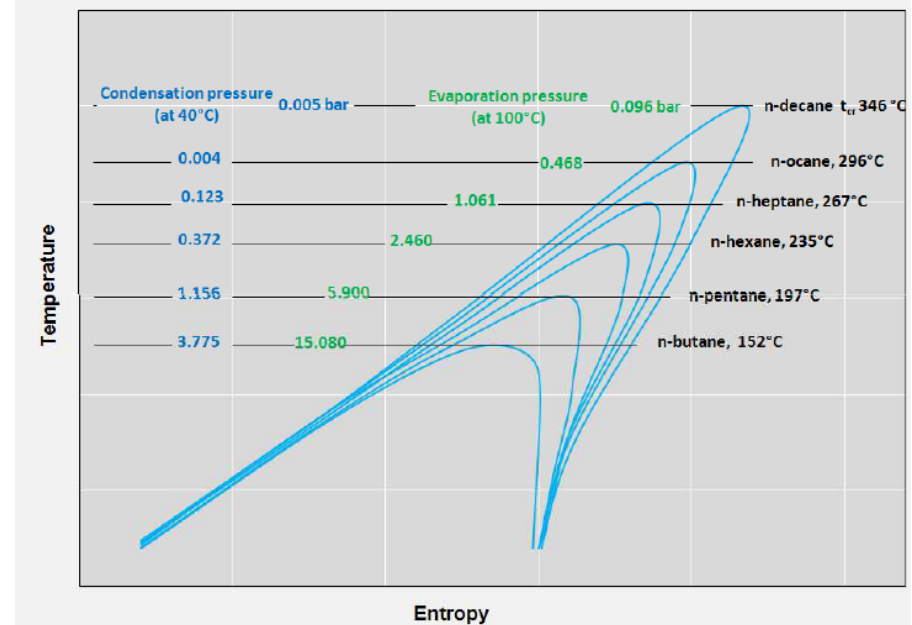




# HTF for ORC

- Choice depends on:
  - Flammability and toxicity depending on security of the site
  - ODP for the environment
  - Stability
  - Authorization for the fluid

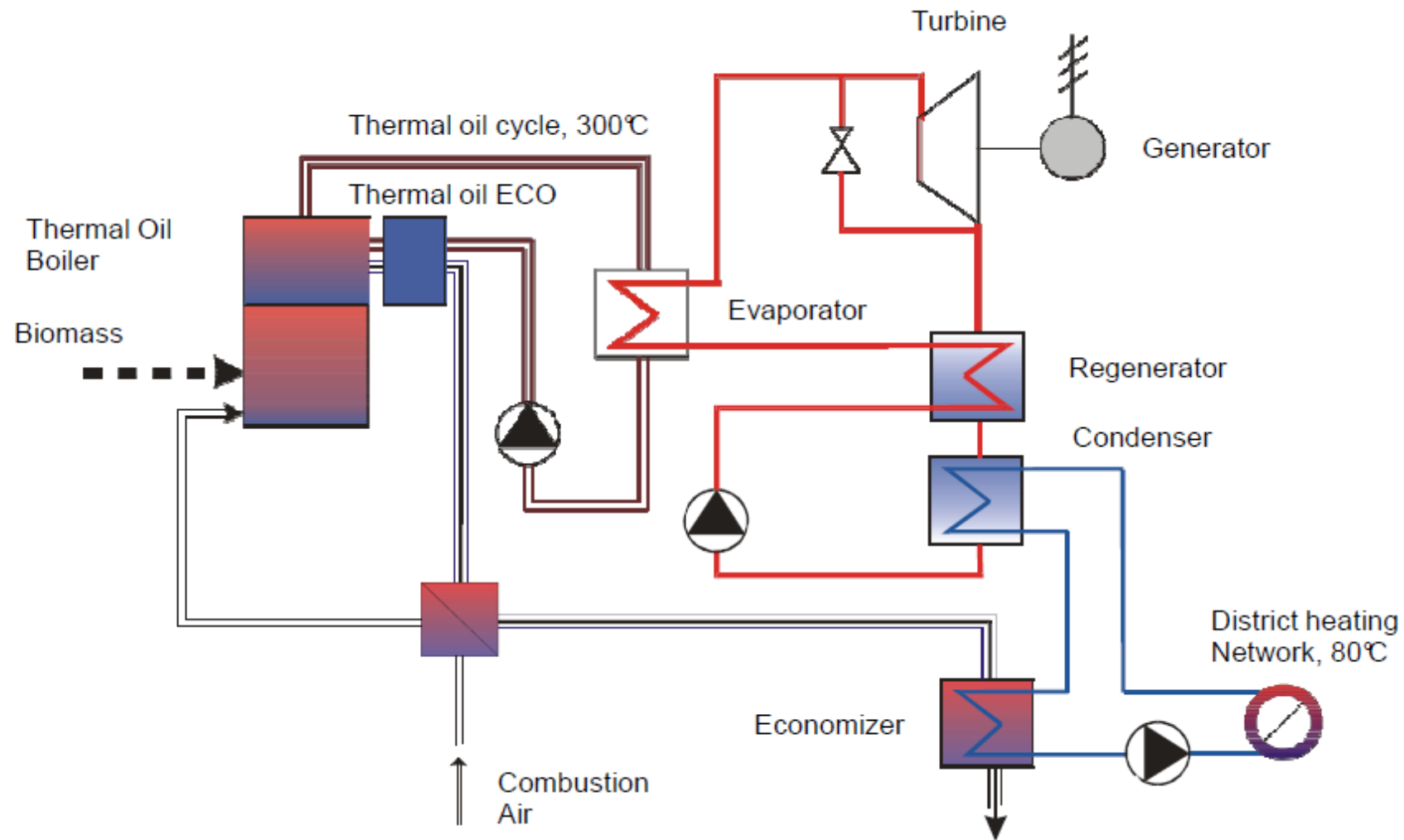
(ODP ozone depletion potential)



	R245 fa	R152A	R32	Pen-tane	Iso-Butane	Toluene
Saturated pressure at 120°C (bar)	19.2	42	58	9	28	1.3
Service temperature (°C)	140	140	140	140	140	140
Saturated pressure at 50°C (bar)	3.5	11	31	1.6	6.8	0.1
Expander pressure ratio	5.6	3.6	1.8	5.7	4.1	10.7
Ozone Depletion Potential	0	0	0	0	0	0
Global Warming Potential	950	140	675	7	3	3
ASHRAE Safety group	B1	A2	A2L	A3	A3	A3
Power density [kW/Exp]	16	26	16	8	21	1.4

# ORC example

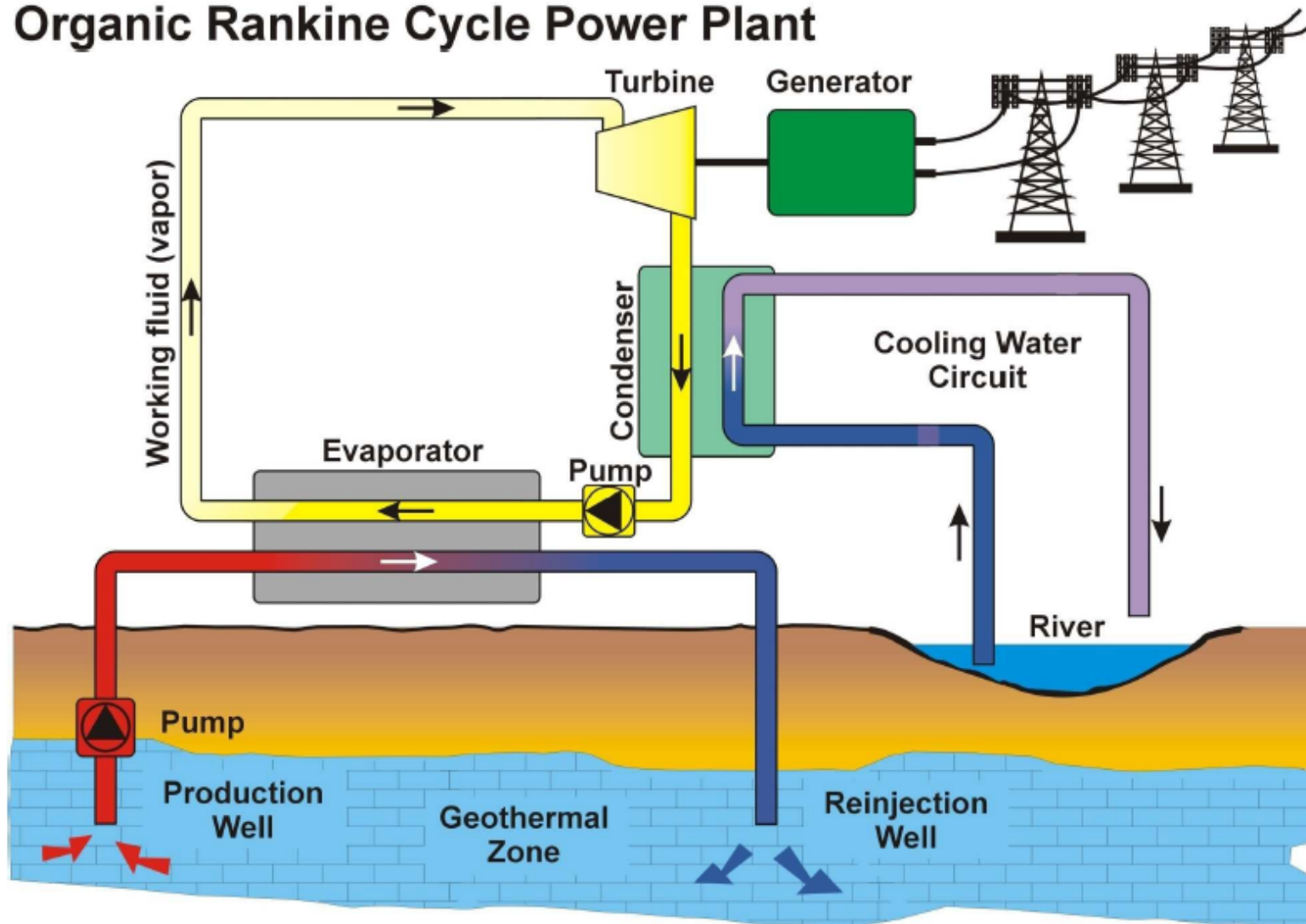
- Biomass: working fluid silicone oil



# ORC example

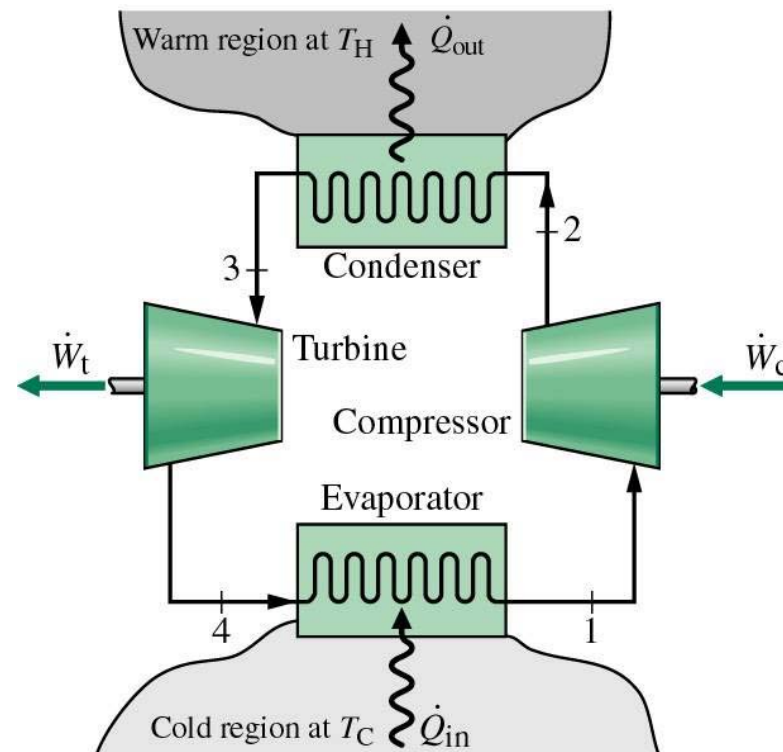
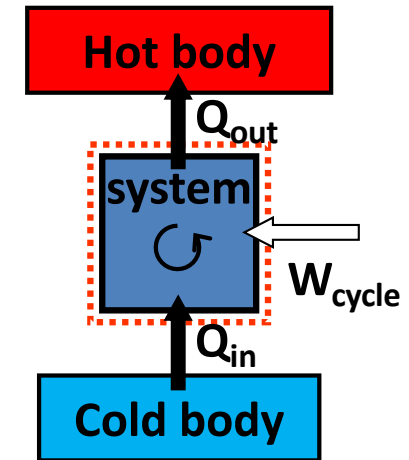
- Geothermal

## Organic Rankine Cycle Power Plant



# Refrigeration and heat pump systems

- Refrigeration and heat pump
  - Maintain colder temperature below temperature of surrounding
  - Maintain higher temperature above temperature of surrounding



# Vapor-compression refrigeration system

- Practical refrigeration/heat pump cycle, ideal:

- 1-2: Isentropic compression

$$\frac{\dot{W}_c}{\dot{m}} = h_1 - h_2$$

- 2-3: Isobaric heat rejection  
(incl. condensing step)

$$\frac{\dot{Q}_{\text{out}}}{\dot{m}} = h_3 - h_2$$

- 3-4: throttling process

$$h_3 = h_4$$

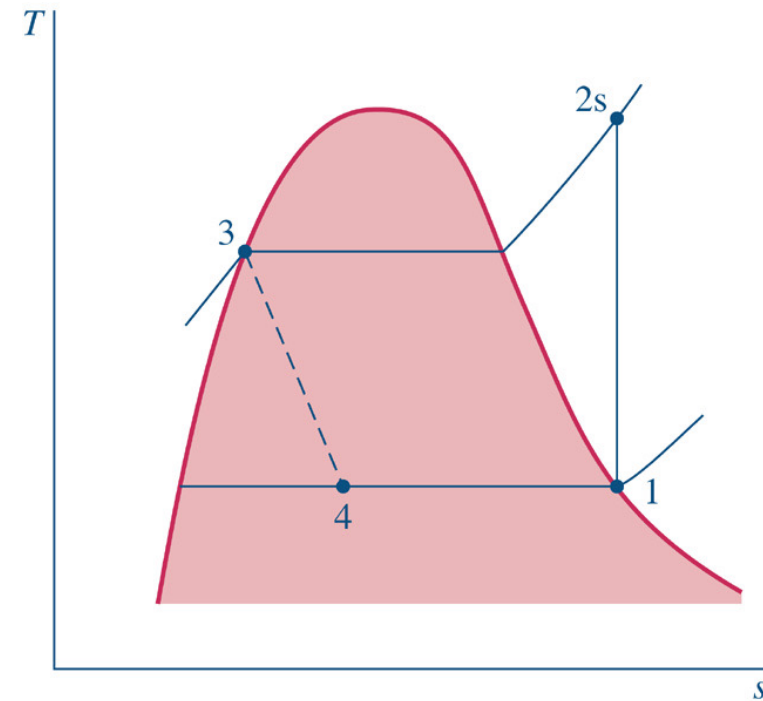
- 4-1: Isobaric heat addition (evaporation step)

$$\frac{\dot{Q}_{\text{in}}}{\dot{m}} = h_1 - h_4$$

- Coefficient of performance:

$$\text{COP}_{\text{cm}} = \frac{h_1 - h_4}{h_2 - h_1} < \text{COP}_{\text{cm,max}}$$

$$\text{COP}_{\text{hm}} = \frac{h_2 - h_3}{h_2 - h_1} < \text{COP}_{\text{hm,max}}$$



# Gas refrigeration systems

- Gas refrigeration systems, Brayton refrigeration cycle

- 1-2(s): (Isentropic) compression

$$\frac{\dot{W}_c}{\dot{m}} = h_2 - h_1$$

- 2-3: Isobaric cooling

$$\frac{\dot{Q}_{\text{out}}}{\dot{m}} = h_3 - h_2$$

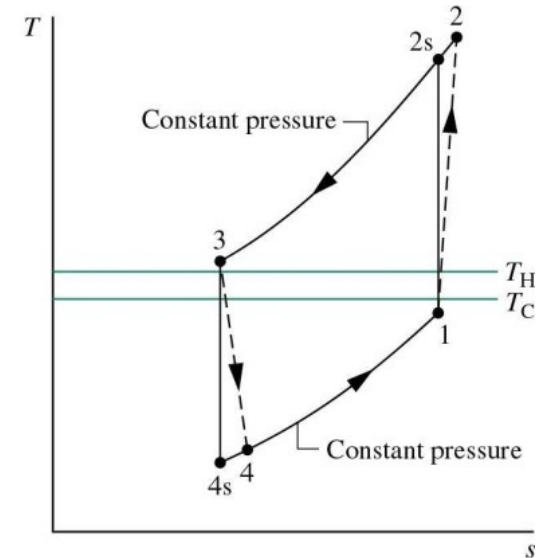
- 3-4(s): (Isentropic) expansion

$$\frac{\dot{W}_t}{\dot{m}} = h_3 - h_4$$

- 4-1: Isobaric evaporation/heating

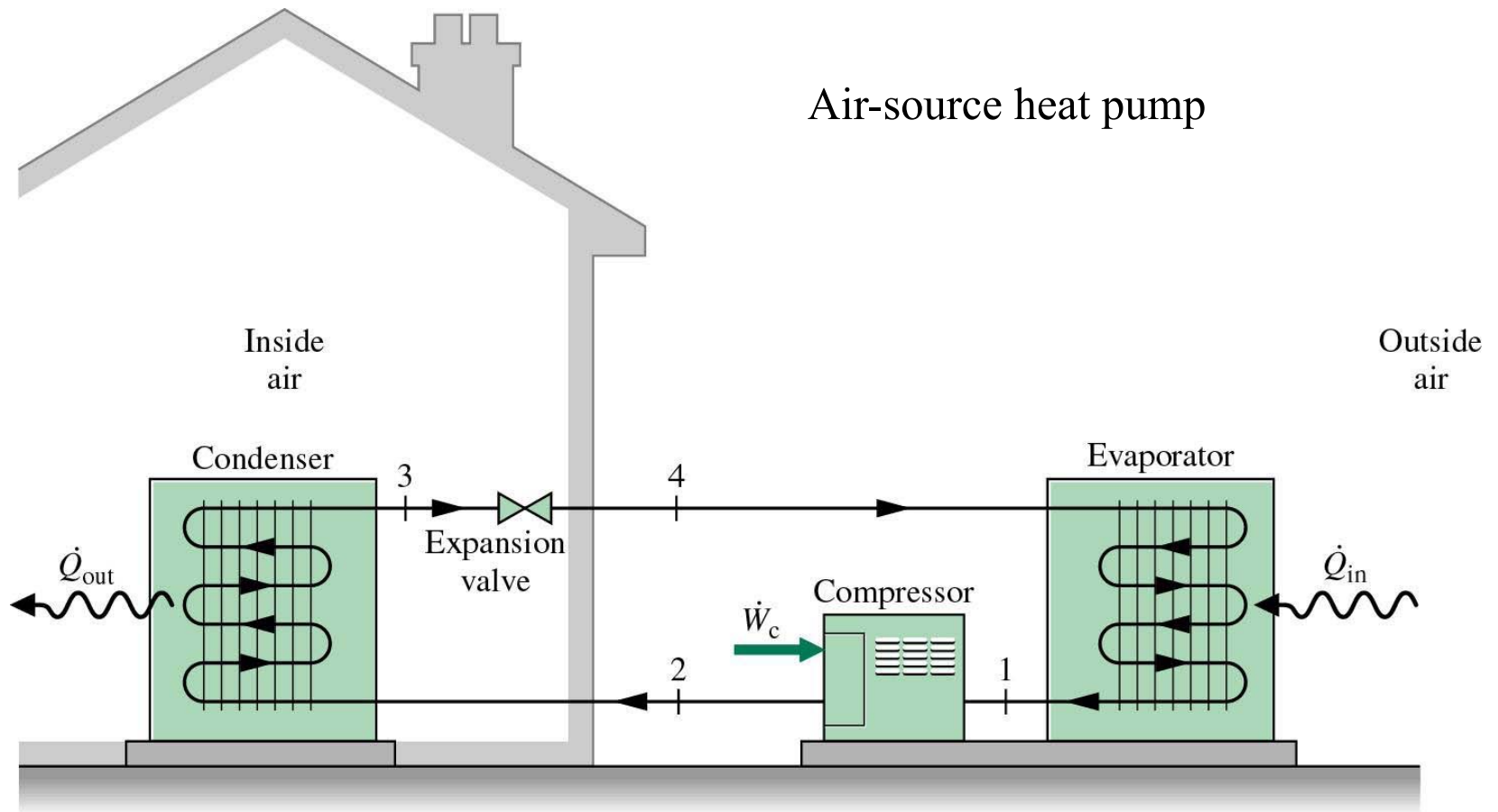
$$\frac{\dot{Q}_{\text{in}}}{\dot{m}} = h_1 - h_4$$

- Coefficient of performance:  $\text{COP}_{\text{cm}} = \frac{h_1 - h_4}{|h_1 - h_2 - (h_3 - h_4)|}$



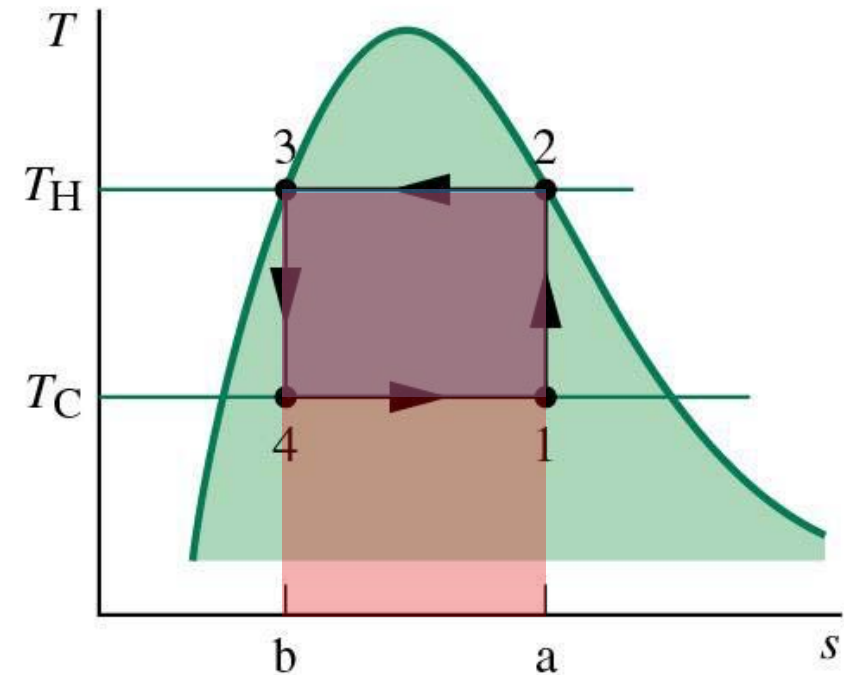
# Heat pump systems

- Heat pump system:
  - Common application: space heating
  - Vapor-compression as well as absorption heat pumps



# Heat pump systems

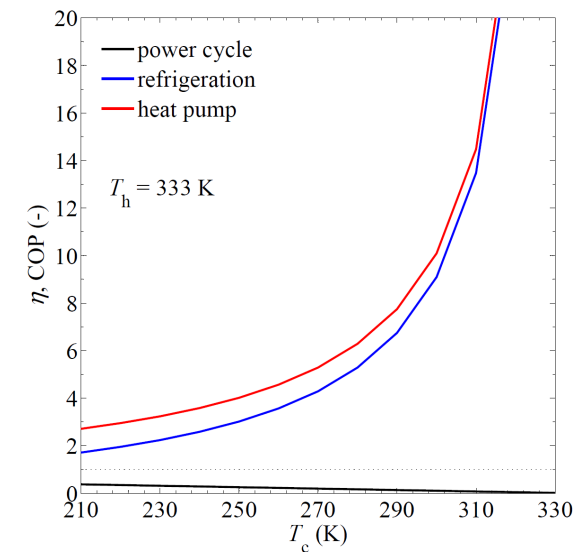
- Carnot heat pump cycle:



– Performance:

$$\text{COP}_{\text{hm,max}} = \frac{\dot{Q}_{\text{out}} / \dot{m}}{\left| \dot{W}_{\text{c}} / \dot{m} - \dot{W}_{\text{t}} / \dot{m} \right|} = \frac{T_{\text{H}} (s_{\text{a}} - s_{\text{b}})}{(T_{\text{H}} - T_{\text{C}})(s_{\text{a}} - s_{\text{b}})}$$

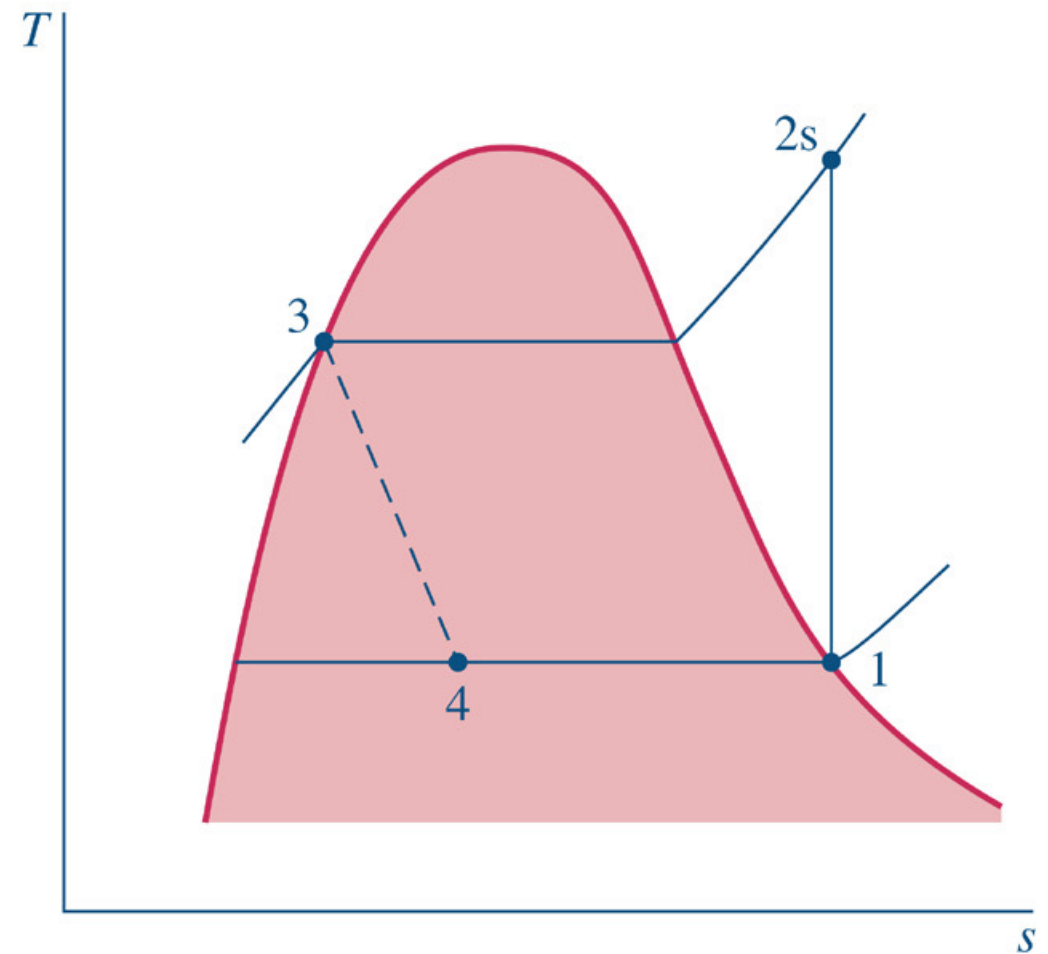
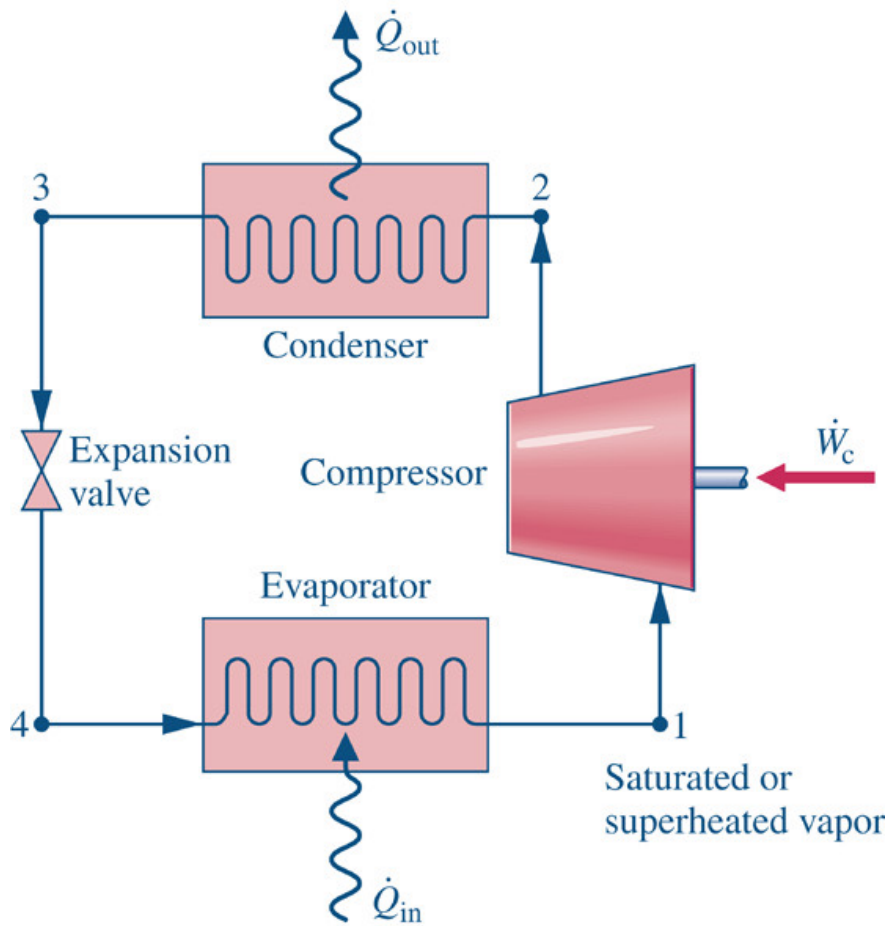
$$= \frac{T_{\text{H}}}{T_{\text{H}} - T_{\text{C}}}$$





# Heat pump systems

- Vapor-compression heat pumps:



# Heat pump systems

- Vapor-compression heat pumps:

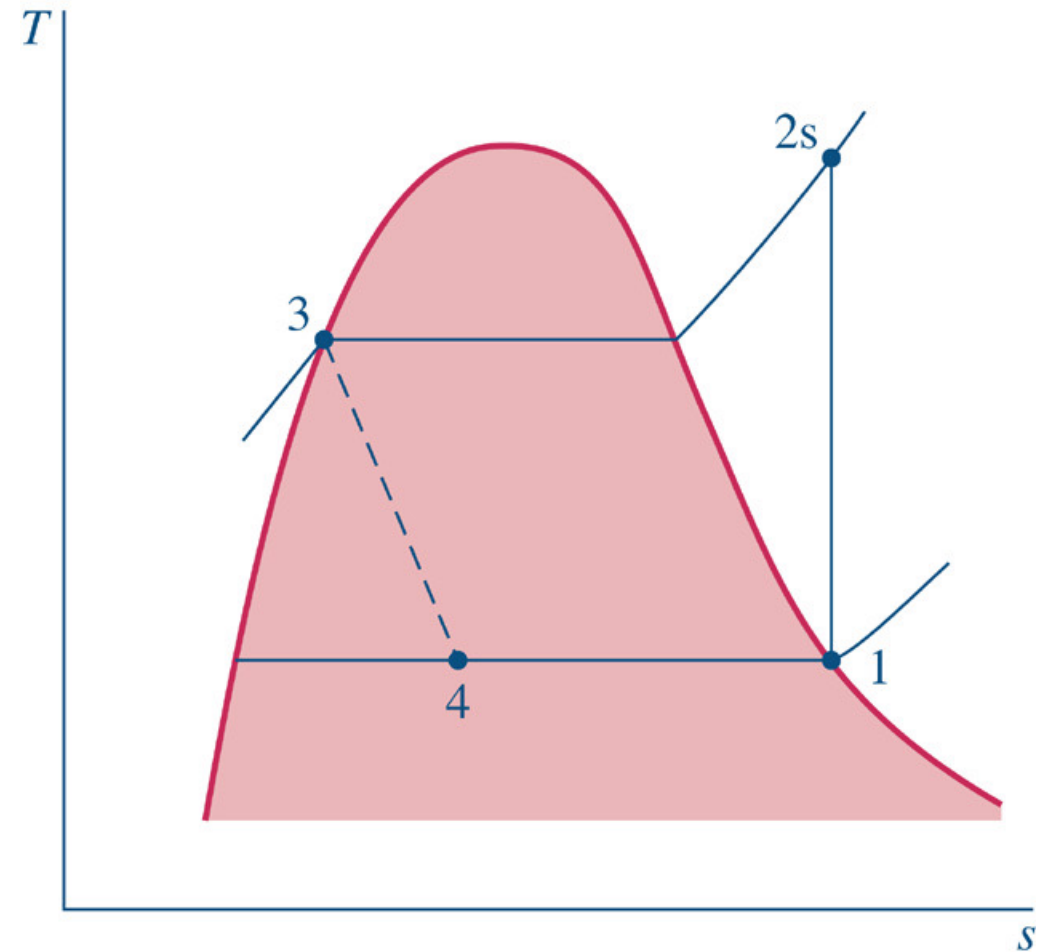
- 1-2:  $\frac{\dot{W}_c}{\dot{m}} = h_1 - h_2$

- 2-3:  $\frac{\dot{Q}_{\text{out}}}{\dot{m}} = h_3 - h_2$

- 3-4:  $h_3 = h_4$

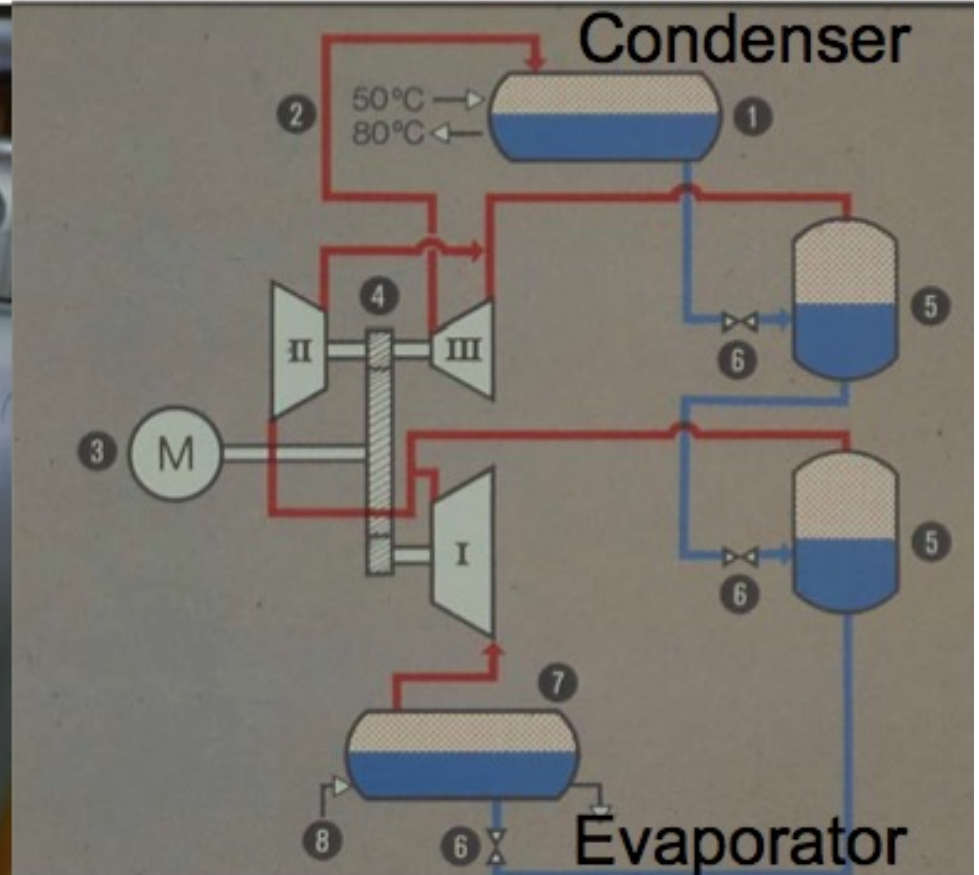
- 4-1:  $\frac{\dot{Q}_{\text{in}}}{\dot{m}} = h_1 - h_4$

- Performance:  $\text{COP}_{\text{hm}} = \frac{\dot{Q}_{\text{out}} / \dot{m}}{\dot{W}_c / \dot{m}} = \frac{h_2 - h_3}{h_2 - h_1}$



# Heat pump

## The largest heat pump (for District heating): 3 compression stages



Goteborg:  $45 \text{ MW}_{\text{th}}$

# Absorption heat pump

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- Principle: achieve the pressure raise from low (BP) → high (HP) not by *mechanical compression*, but by **desorption** (using a *heat source*) of a working fluid from its solvent, in which this working fluid had previously been absorbed (=rejecting heat during **absorption**)
  - e.g. working fluid **NH<sub>3</sub>** with **water** as solvent
  - e.g. working fluid **water** with **LiBr** as solvent

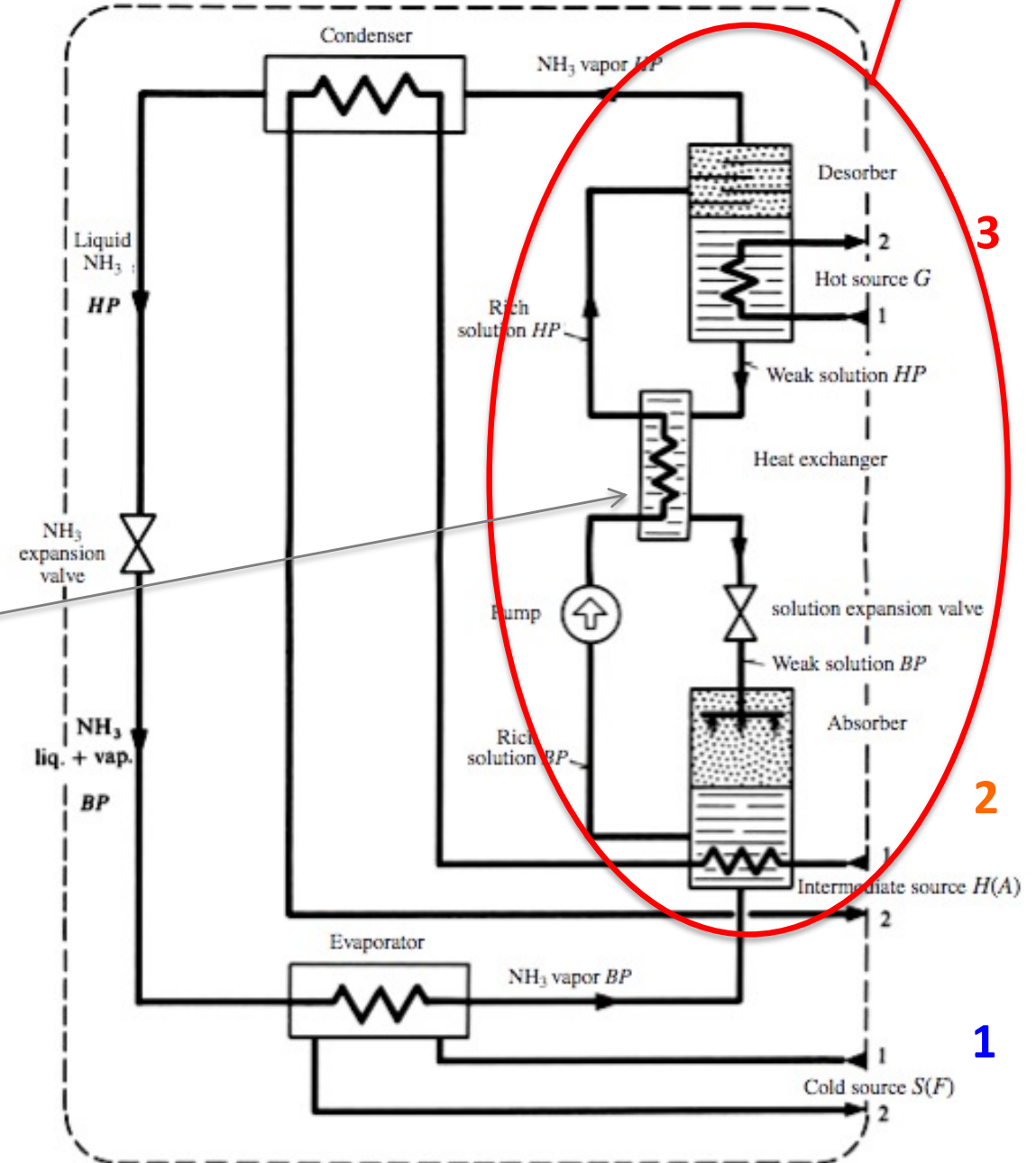
often low temperature (~100°C),  
ideal for many renewables

# Absorption heat pump

replaces a compressor

- **absorber** (water):  
receives low p NH<sub>3</sub> vapor (BP)  
⇒ liberates absorption heat (H)
- **liquid pump** BP → HP
- **boiler**: delivers the absorption heat (G) to desorb the NH<sub>3</sub> vapor → HP
- expander (liq.) HP → BP
- internal heat exchanger between the rich and poor solutions (in NH<sub>3</sub>)
- tubing

$$\dot{E}_P^+$$



TRITHERMAL CYCLE 1, 2, 3

# Learning outcomes

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- Introduction into thermodynamics:
  - 1<sup>st</sup> law for closed and open systems
  - 2<sup>nd</sup> law for closed and open systems, entropy definition
  - Exergy
  - State functions
- Exemplary thermodynamic power systems:
  - Power systems:
    - Vapor power systems
    - Gas power systems:
      - Internal combustion engines
      - Gas turbine power plants
- Examples of relevant power cycles for renewable sources
- Examples thermodynamic cooling and heating systems:
  - Refrigeration and heat pump systems

**Addendum :**  
**derivation of exergy balance from 1st + 2<sup>nd</sup> Laws**

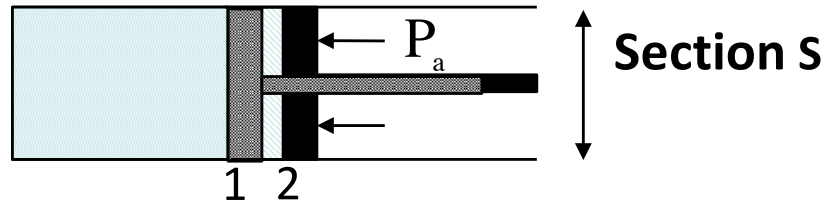


# 1<sup>st</sup> Law

Mechanical work transfer + Heat transfer + Enthalpy flow balance (linked to mass flow) = Rate of variation of internal energy (accumulation or diminution)

$$\sum_k (\dot{E}_k^+) + \dot{E}_a^+ + \sum_i (\dot{Q}_i^+) + \dot{Q}_a^+ + \sum_j (h_{cz,j} \dot{M}_j^+) = dU_{cz} / dt$$

Effective work  
(via crankshaft or  
connecting rod)



$$\dot{E}_a^+ = -P_a dV / dt = \text{mechanical work related to the atmosphere}$$



(separating atmosphere terms)

$$\sum_k [\dot{E}_k^+] - P_a \frac{dV}{dt} + \sum_i [\dot{Q}_i^+] + \dot{Q}_a^+ + \sum_j [h_{czj} \dot{M}_j^+] = \frac{dU_{cz}}{dt}$$

$$\sum_k [\dot{E}_k^+] + \sum_i [\dot{Q}_i^+] + \dot{Q}_a^+ + \sum_j [h_{czj} \dot{M}_j^+] = \frac{d(U_{cz} + P_a dV)}{dt}$$

For 1 network:

$$\sum_k [\dot{E}_k^+] + \sum_i [\dot{Q}_i^+] + \dot{Q}_a^+ + \sum_j [h_{czj} \dot{M}_j^+] - \frac{d(U_{cz} + P_a V)}{dt} = 0$$

For n networks:

$$\sum_k [\dot{E}_k^+] + \sum_i [\dot{Q}_i^+] + \dot{Q}_a^+ + \sum_n \left( \sum_j [h_{czj} \dot{M}_j^+] - \frac{d(U_{cz} + P_a V)}{dt} \right) = 0$$

# 2<sup>nd</sup> Law (separating heat transfer with atmosphere)

Entropy transferred by **heat** transfer

+

Entropy flow balance (linked to mass flow)

+

Internal entropy creation rate

=

Rate of variation of system entropy

$$\sum_i \dot{Q}_i^+ / T_i + \boxed{\dot{Q}_a^+ / T_a} + \sum_j (s_j \dot{M}_j^+) + \boxed{\delta S^i / dt} = dS / dt$$

$$\geq 0$$

1<sup>st</sup> law:

$$\sum_k (\dot{E}_k^+) + \sum_i \dot{Q}_i^+ + \boxed{\dot{Q}_a^+} + \sum_j (h_{czj} \dot{M}_j^+) = d(U_{cz} + P_a V) / dt$$

$$\sum_i \dot{Q}_i^+ / T_i + \dot{Q}_a^+ / T_a + \sum_j (s_j \dot{M}_j^+) - dS / dt + \delta S^i / dt = 0$$

$$\boxed{T_a \sum_i \dot{Q}_i^+ / T_i + \dot{Q}_a^+} + T_a \sum_j (s_j \dot{M}_j^+) - T_a dS / dt = -T_a \delta S^i / dt$$

# EXERGY BALANCE (1<sup>st</sup> Law *minus* 2<sup>nd</sup> Law):

1<sup>st</sup> Law

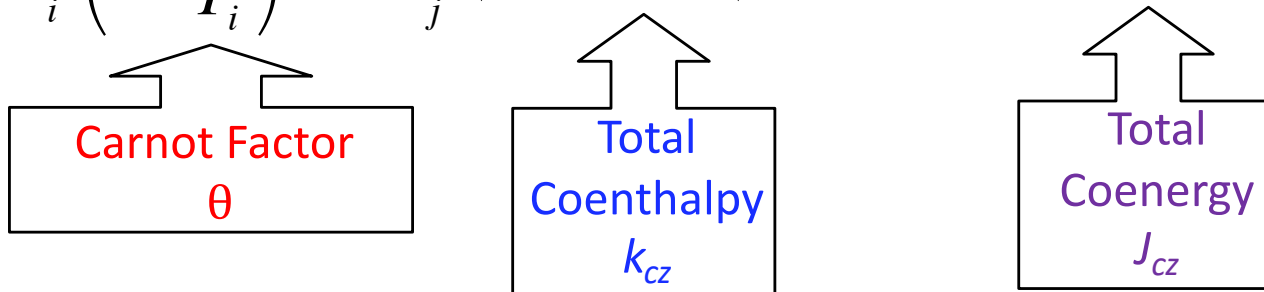
$$\sum_k (\dot{E}_k^+) + \sum_i \dot{Q}_i^+ + \cancel{\dot{Q}_a^+} + \sum_j (h_{cz,j} \dot{M}_j^+) - d(U_{cz} + P_a V) / dt = 0$$

minus the 2<sup>nd</sup> Law

$$-T_a \sum_i \dot{Q}_i^+ / T_i - \cancel{\dot{Q}_a^+} - T_a \sum_j (s_j \dot{M}_j^+) + T_a dS / dt = T_a \delta S^i / dt$$

---


$$\sum_k (\dot{E}_k^+) + \sum_i \left(1 - \frac{T_a}{T_i}\right) \dot{Q}_i^+ + \sum_j (h_{cz,j} - T_a s_j) \dot{M}_j^+ - d(U_{cz} + P_a V - T_a S) / dt = T_a \delta S^i / dt$$



(grouped as 'transformation-exergy' on next slide)

# EXERGY BALANCE

1<sup>st</sup> Law

$$\sum_k (\dot{E}_k^+) + \sum_i \dot{Q}_i^+ + \dot{Q}_a^+ + \sum_j (h_{czj} \dot{M}_j^+) - d(U_{cz} + P_a V) / dt = 0$$

minus the 2<sup>nd</sup> Law

$$-T_a \sum_i \dot{Q}_i^+ / T_i - \dot{Q}_a^+ - T_a \sum_j (s_j \dot{M}_j^+) + T_a dS / dt = T_a \delta S^i / dt$$

$$\sum_k (\dot{E}_k^+) + \sum_i \left(1 - \frac{T_a}{T_i}\right) \dot{Q}_i^+ + \sum_j (h_{czj} - T_a s_j) \dot{M}_j^+ - d(U_{cz} + P_a V - T_a S) / dt = T_a \delta S^i / dt$$

Mech.work-exergy     Heat-exergy     Transformation-exergy (1 per network n)     Exergy loss

$$\sum_k \dot{E}_k^+ + \sum_i \dot{E}_{qi}^+ + \sum_n \dot{E}_{yn}^+ = \dot{L}$$

In this formulation, every term is either positive or negative

# Summary of formulations (with + = entering the system)

Energy balance (1<sup>st</sup> law)

$$\sum_k (\dot{E}_k^+) + \sum_i \dot{Q}_i^+ + \dot{Q}_a^+ + \left[ \sum_j (h_{cz,j} \dot{M}_j^+) - d(U_{cz} + P_a V) / dt \right] = 0$$

$$\sum_k \dot{E}_k^+ + \sum_i \dot{Q}_i^+ + \sum_n \dot{Y}_n^+ - \dot{Q}_a^- = 0$$

*Every received energy quantity not kept in the system eventually is heat loss to the atmosphere*

Exergy balance (1<sup>st</sup> + 2<sup>nd</sup> laws)

$$\sum_k (\dot{E}_k^+) + \sum_i \left(1 - \frac{T_a}{T_i}\right) \dot{Q}_i^+ + \left[ \sum_j (h_{cz,j} - T_a s_j) \dot{M}_j^+ - d(U_{cz} + P_a V - T_a S) / dt \right] - T_a \delta S^i / dt = 0$$

$$\sum_k \dot{E}_k^+ + \sum_i \dot{E}_{qi}^+ + \sum_n \dot{E}_{yn}^+ - \dot{L} = 0$$

*Every received work quantity not exported as work from the system is internal entropy creation*

# Formulations with only positive terms

**Energy** balance (1<sup>st</sup> law)

$$\sum_k \dot{E}_k^+ + \sum_i \dot{Q}_i^+ + \sum_n \dot{Y}_n^+ - \dot{Q}_a^- = \sum_k \dot{E}_k^- + \sum_i \dot{Q}_i^- + \sum_n \dot{Y}_n^-$$

*All received energy in a system equals the energy output services plus the heat loss to the atmosphere*

**Exergy** balance (1<sup>st</sup> + 2<sup>nd</sup> laws)

$$\sum_k \dot{E}_k^+ + \sum_i \dot{E}_{qi}^+ + \sum_n \dot{E}_{yn}^+ - \dot{L} = \sum_k \dot{E}_k^- + \sum_i \dot{E}_{qi}^- + \sum_n \dot{E}_{yn}^-$$

*Real equivalent work output of a system equals the maximal equivalent work received by the system minus the irreversibility losses due to internal entropy creation*

# Effectiveness and exergy efficiency

## Effectiveness (1<sup>st</sup> law)

$$\varepsilon = \frac{\sum[\dot{E}^-] + \sum[\dot{Q}^-] + \sum[\dot{Y}^-]}{\sum[\dot{E}^+] + \sum[\dot{Q}^+] + \sum[\dot{Y}^+]}$$

Examples:

Heat pump

$$\varepsilon_h = \frac{\dot{Q}_{cond}^-}{\dot{E}_{elec}^+}$$

Refrigeration pump

$$\varepsilon_f = \frac{\dot{Q}_{evap}^+}{\dot{E}_{elec}^+}$$



## Exergy efficiency (1<sup>st</sup> and 2<sup>nd</sup> laws)

$$\eta = \frac{\sum[\dot{E}^-] + \sum[\dot{E}_q^-] + \sum[\dot{E}_y^-]}{\sum[\dot{E}^+] + \sum[\dot{E}_q^+] + \sum[\dot{E}_y^+]}$$

General and always applicable

$$\eta = \frac{\dot{E}_q^-}{\dot{E}^+}$$

$$\eta = \frac{\dot{Q}_{cond}^- \left(1 - \frac{T_a}{T_{cond}}\right)}{\dot{E}^+}$$

$$\eta = \frac{\dot{Q}_{evap}^+ \left(\frac{T_a}{T_{evap}} - 1\right)}{\dot{E}^+}$$