### **WELCOME!**

Astrophysics IV:

# Stellar & Galactic Dynamics

Spring 2025

Dr. Yves Revaz
Laboratoire d'astrophysique
Observatoire de Sauverny
CH – 1290 Versoix



# **Mailing List**

• Use Moodle : moodle.epfl.ch

Anyone missing?

# **About me**

- MER at the Laboratory of Astrophysics
- Native from le Valais
- Former EPFL student
- Thesis in galactic dynamics (Prof. Pfenniger)
- Postdoc in Geneva, Paris and EPFL
- Faculty at EPFL since 2010

#### Research

- Formation and evolution of galaxies
- Galactic dynamics, galaxy clusters, dwarf galaxies
- Development of numerical tools (Gear, pNbody, Swift)
- Core Team Member of the Arrakihs Space mission
- Work package leader of WP2 of the Arrakihs Space mission
- Virtual reality
- VIRUP: The Virtual Reality Universe Project
- https://go.epfl.ch/virup

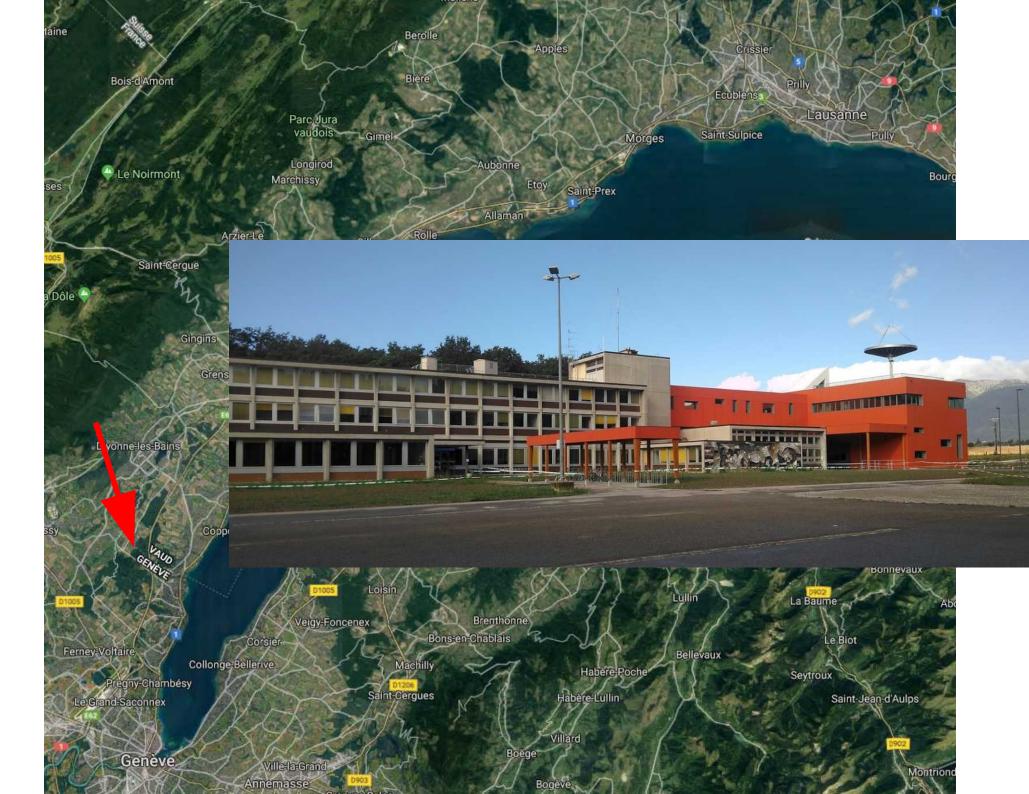
# **Contacts**

- Email: yves.revaz@epfl.ch
- Cubotron (BSP) 323
- Observatoire de Sauverny, 351









# Astrophysics @ EPFL Teaching

- Astro I: Introduction à l'astrophysique (Bachelor)
  - Jean-Paul Kneib
- Astro II: Bases physiques de l'astrophysique (Master)
  - Pascale Jablonka
- Astro III: Galaxy Formation and Evolution (Master)
  - Michaela Hirschmann
- Astro IV: Stellar and Galactic Dynamics (Master)
  - Yves Revaz
- Astro V: Observational Cosmology (Master)
  - Jean-Paul Kneib
- The Variable Universe (EDPY)
  - Richard Anderson
- MOOC:
  - The radio-sky I : Science and Observations
     Frédéric Courbin, Jean-Paul Kneib
  - Introduction à l'astrophysique

Frédéric Courbin

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  - Introduction à l'astrophysique
     Frédéric Courbin

#### In addition:

- TP4a
- TP4b
- Specialisation semester
- Master's project

# Astrophysics @ EPFL Research

Research group leaders: Jean-Paul Kneib

Michaela Hirschman Pascale Jabonka

Yves Revaz David Harvey

**Richard Anderson** 

Emma Tolley

Research fields:

Galaxy Formation & Evolution

Cosmological parameters

Epoch of reionization

Dark energy

Dark matter

# Astrophysics @ EPFL Research

Research group leaders: Jean-Paul Kneib

Michaela Hirschman

Pascale Jabonka

Yves Revaz David Harvey

**Richard Anderson** 

Emma Tolley

**Research Methods:** 

**Observations** 

Image processing

Numerical simulations

Machine learning





About Education Research Innovation Schools Campus Q

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#### **Research Themes**

Instruments & Consortia

Research Groups

Teaching

Student Research Projects

Members

News & Events

Public Outreach

#### **Research Themes**

### **Galaxy Formation & Evolution**



- Formation and evolution of galaxies: surveys and numerical simulations
  - [PJ Group, YR Group, GALSPEC]
- Galaxy clusters and cosmic filamentary structures.

# Outlines of the 14<sup>th</sup> lectures

# Goal of the course

Teach how a system (stellar or galactic) evolves under the forces of gravity that are generated by itself

Evolution of a self-gravitating system

# **Outlines**

#### Week 1:

#### **Introduction**

- The standard model in cosmology
- The formation of the large scale structure
- Which physics
- Our galaxy the Milky Way
- The Local Group and beyond

#### Week 2:

#### The gravity: a long distance force

- collision-less systems : the relaxation time

#### **Newton Mechanics (quick reminder)**

#### The Potential Theory I

- General results
  - Newton law, gravitational field force and potential

#### Week 3:

#### The Potential Theory I

- Spherical systems
  - Newton's theorems.
  - Circular speed, circular velocity, circular frequency, escape speed, potential energy
  - Useful relations for spherical systems

#### Week 4:

#### The Potential Theory II

- Examples of spherical models:
  - "Potential based" models
  - "Density based" models
- Axisymmetric models for disk galaxies
  - "Potential based" models
  - Potential of flattened systems
  - The potential of infinite thin (razor) disks (potential of a ring)
  - Potential of ellipsoidal systems
  - Potential of infinite thin disks and slabs

#### Week 5:

#### **Stellar Orbits I**

- Generalities: why studying stellar orbits?
- Lagrangian and Hamiltonian mechanics (quick reminder)
  - Euler-Lagrange equations
  - Hamilton's equations
- Orbits in spherical potentials
  - angular momentum conservation
  - equations of motion
  - radial orbits
  - non radial orbits
- Examples
  - Keplerian orbits
  - Orbits in an homogeneous sphere
  - Orbits in isochrone potentials

#### Week 6:

#### **Stellar Orbits II**

- Orbits in axisymmetric potentials
  - orbits in the equatorial plane
  - orbits outside the equatorial plane
  - equations of motion
  - orbits in the meridian plane
  - examples

#### Week 7:

#### **Stellar Orbits III**

- Nearly circular orbits
  - Epicycle frequences
  - The Oort constants
  - Probing the mass in the stellar disk
- Surface of section
  - Integral of motions
  - Poincaré maps

#### Week 8:

#### **Stellar Orbits IV**

- Orbits in planar non-axisymmetric potential
  - surface of sections
- Orbits in non-axisymmetric rotating potential
  - the Jacobi integral
  - Lagrange points
  - stability of orbits around Lagrange points
  - orbits not confined to Lagrange points
- Weak bars
  - the Lindblad resonances
  - orbit families in realistic bars

#### Week 9:

#### **Equilibria of collisionless systems I**

- The collisonless Boltzmann equation
  - The distribution function (DF) of stellar systems
  - The Collisionless Boltzmann equation
  - Limitations
- Relations between DFs and observables
  - Density, velocity distribution function, mean velocity, velocity dispersion
- The Jeans theorems
  - Solutions of the Collisionless Boltzmann equation
  - Symmetry and integrals of motion

#### **Week 10:**

#### **Equilibria of collisionless systems II**

- Self-consitent spherical models with Ergodic DF
  - DFs from mass distribution
    - The Eddington formula
    - Examples
  - Models defined from DFs
    - Polytropes and Plummer models
    - Parallel with hydrostatics polytropes
    - Isothermal models
    - Parallel with hydrostatics isothermal models

#### **Week 11:**

#### **Equilibria of collisionless systems III**

- Anisotropic distribution function in spherical systems
  - Motivations
  - General concepts
  - Example of an anisotropic DF
  - Application to the Hernquist model
- The Jeans Equations (moments equation)
  - Motivations
  - The Jeans Equations and conservation laws
  - The Jeans Equations in Spherical and Cylindrical coordinates

#### **Week 12:**

#### **Equilibria of collisionless systems IV**

- The Virial Equation and Virial Theorem
  - Theory
  - Applications

#### Stability of collisionless systems I

- Nbody- experiments
  - Are systems defined from a DF that solve the CB stable ?

#### **Week 13:**

#### Stability of collisionless systems II

- Linear response theory
  - in fluid systems
  - in stellar systems
- The Jeans instability
- The stability of uniformly rotating systems

#### **Week 14:**

#### Stability of collisionless systems III

- The stability of rotating disks : spiral stuctures
  - Spirals properties
  - The dispersion relation for a razor thin fluid disk
  - The WKB approximation
- The origin of spiral structures: another view
- Vertical instabilities
  - Nature is always more tricky...

# Polycop...? No.

- PDF manuscript notes ?
  - yes, on moodle.epfl.ch

- Recordings ?
  - No (except when I will be absent...)

- Additional material ?
  - yes, on moodle.epfl.ch

## Is it a difficult course?

Theoretical lecture (a lots of equations)

#### Physics:



- Newtonwian gravity
- Lagrangian/Hamiltonian formalism
- Distribution function
- A lots of paralell between different fields in physics:
   e.g. thermodynamics/statistical physics, hydrodynamics

#### **Mathematics**:

• Differencial equations, Fourrier transform, Abel integral, Elliptical coordinates

Integration over doisson

$$\frac{1}{g_{s,n}}(\bar{\kappa},t) = -\frac{4\bar{\kappa}G}{k^{2}} : \int d^{3}\bar{\nu} \; \bar{\kappa} \cdot \frac{\partial S}{\partial \bar{\nu}} \int_{-\infty}^{t} dt' \; e^{i\vec{k}\cdot\bar{\nu}(1'-t)} \left[ \bar{g}_{s,n}(\kappa,t') + \bar{g}_{e}(\kappa,t') \right]$$

In temporal Fourier space

His term way direge if Fe.V = W

$$\widehat{\widehat{g}}_{Sn}\left(\overline{k_{i}}u\right) = \left(-\frac{u_{i}G}{h^{2}} \left\{\frac{d^{3}\overline{v}}{\overline{k_{i}}\overline{v}} - u_{i}^{2}\overline{v}, \frac{dS_{0}}{\partial \overline{v}}\right\} \left(\widehat{\widehat{g}}_{Sn}(\overline{k_{i}}u) + \widehat{\widehat{f}}_{e}(\overline{k_{i}}u)\right)$$

In absence of perturbalian

ge = c

we must have :

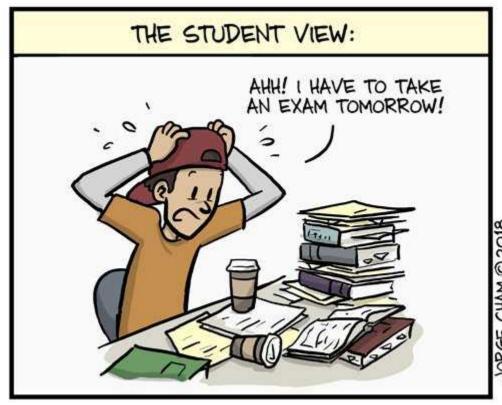
$$-\frac{u\bar{u}G}{h^2} \left\{ \frac{d^3\bar{v}}{\bar{k}.\bar{v}} - \omega \quad \bar{\kappa}. \quad \partial_{\bar{v}}^{\bar{v}} = 1 \right\}$$

In(w) > 0

(instead, we may ) home a divergence )

This is our dispertion relation

### **Exam**





WWW. PHDCOMICS. COM

### Oral Exam:

- Classical form : general questions on the lectures

# **Bibliography**

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  - Morphology and Dynamics of Galaxies, Saas-Fee Advanced Course #3

# Acknowledgements

- Daniel Pfenniger
- Pierre North
- George Meylan
- Jean-Paul Kneib

# The standard model in cosmology

a quick overview

• Einstein equations (1915)

$$R_{\mu\nu} - \frac{1}{2}Rg_{\mu\nu} = 8\pi G T_{\mu\nu}$$
 geometry of spacetime mass/energy content

• The cosmological principle:

The spatial distribution of matter in the universe is homogeneous and isotropic when viewed on a large enough scale.

 Under the cosmological principle, Einstein equations becomes quite simple:





Alexander Friedman (1888-1925)

Georges Lemaître (1894-1966)

The Friedman-Lemaître equations:

Mass/energy content of the Universe:

$$\Omega_{\rm M} + \Omega_{\rm K} + \Omega_{\Lambda} = 1$$

Fraction of matter Sensitive to the gravity curvature

cosmological constant dark energy

Time evolution of its size:

$$a(t) = a(\Omega_{\rm M}, \Omega_{\rm K}, \Omega_{\Lambda})$$

 Under the cosmological principle, Einstein equations become quite simple:

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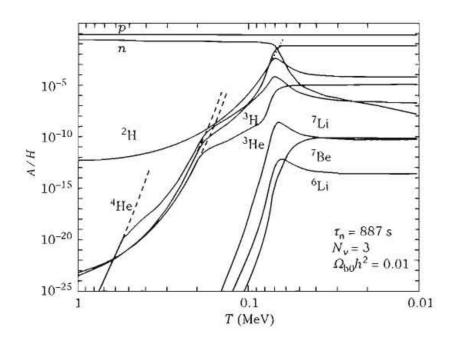
Time evolution of its size:

$$a(t) = a(\Omega_{\rm M}, \Omega_{\rm K}, \Omega_{\Lambda})$$

#### **Observational constraints:**

Big Bang nucleosynthesis (BBN)

Formation of lights atomic elements, (H, He, Li, Be) during 0.1 and 200s after the BB, when the Universe was hot and dense.



→ constraints on the fraction of atoms (baryons) in the Universe

$$\Omega_{\rm b} = 0.042$$







Ralph Alpher Hans Bethe 1948

George Gamow

#### Nobel Prize in Physics 1967

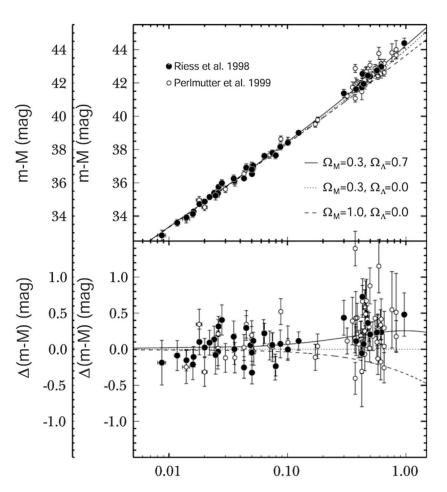


Photo from the Nobel Foundation archive.

Hans Albrecht Bethe

#### **Observational constraints:**

The standard candels (Type Ia supernovae)



#### The Nobel Prize in Physics 2011



© The Nobel Foundation. Photo: U Montan Saul Perlmutter Prize share: 1/2



© The Nobel Foundation. Photo: U. Montan
Brian P. Schmidt
Prize share: 1/4



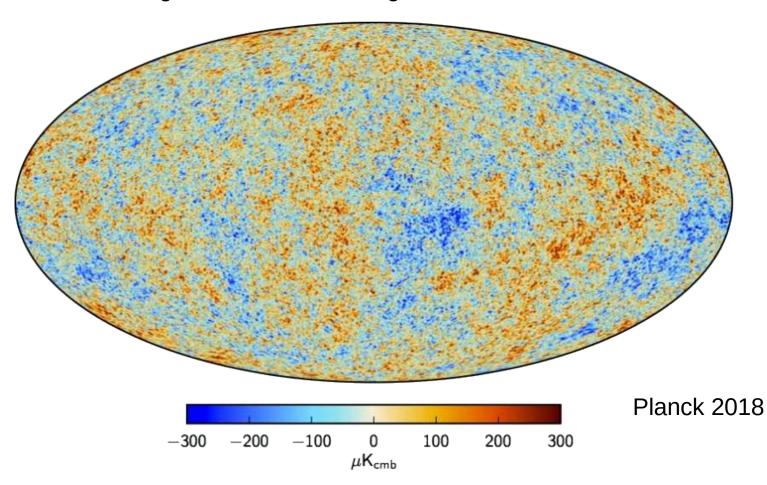
© The Nobel Foundation. Photo: U. Montan
Adam G. Riess
Prize share: 1/4

 $\Omega_{\Lambda} \neq 0$ 

Perlmutter 1998

#### **Observational constraints:**

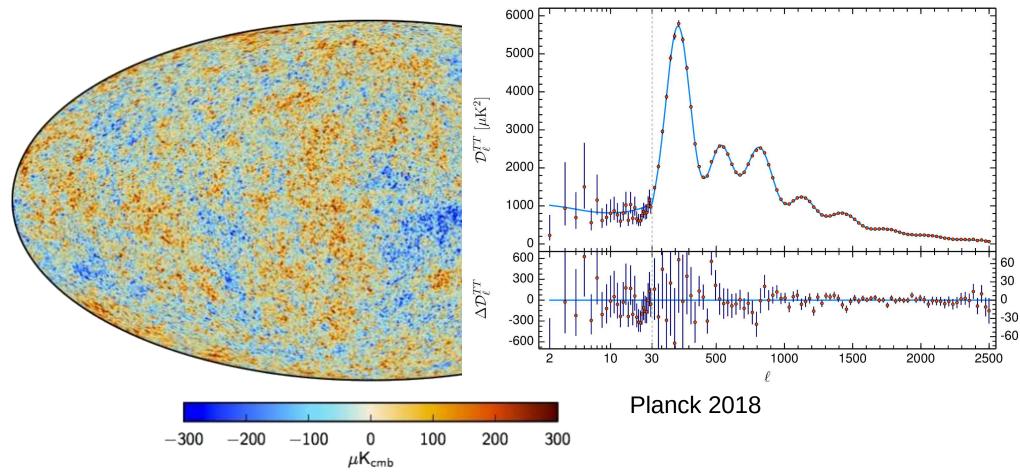
The cosmological microwave background



$$\Omega_{\rm K} = 0 \quad \Omega_{\rm M} + \Omega_{\Lambda} = 1$$

#### **Observational constraints:**

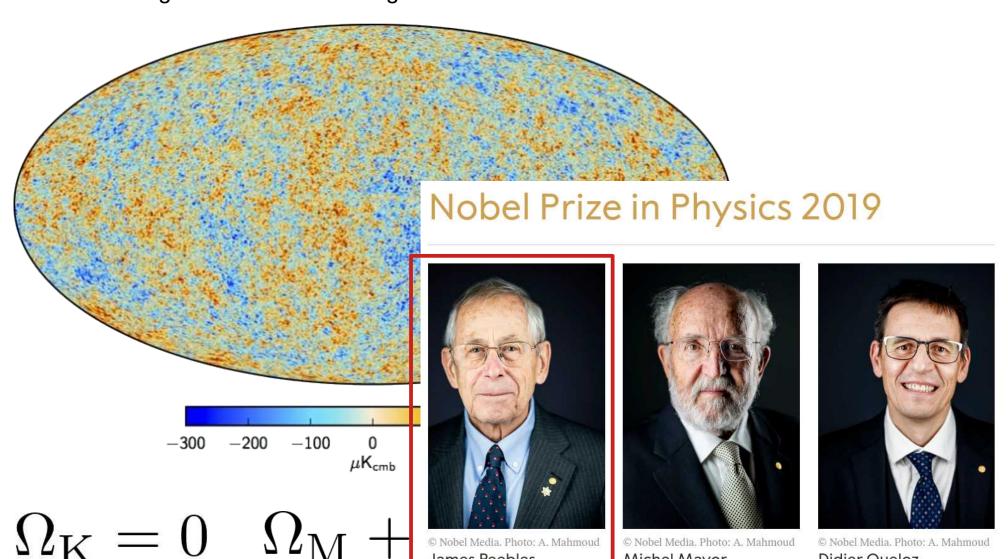
The cosmological microwave background



$$\Omega_{\rm K} = 0 \quad \Omega_{\rm M} + \Omega_{\Lambda} = 1$$

#### **Observational constraints:**

The cosmological microwave background

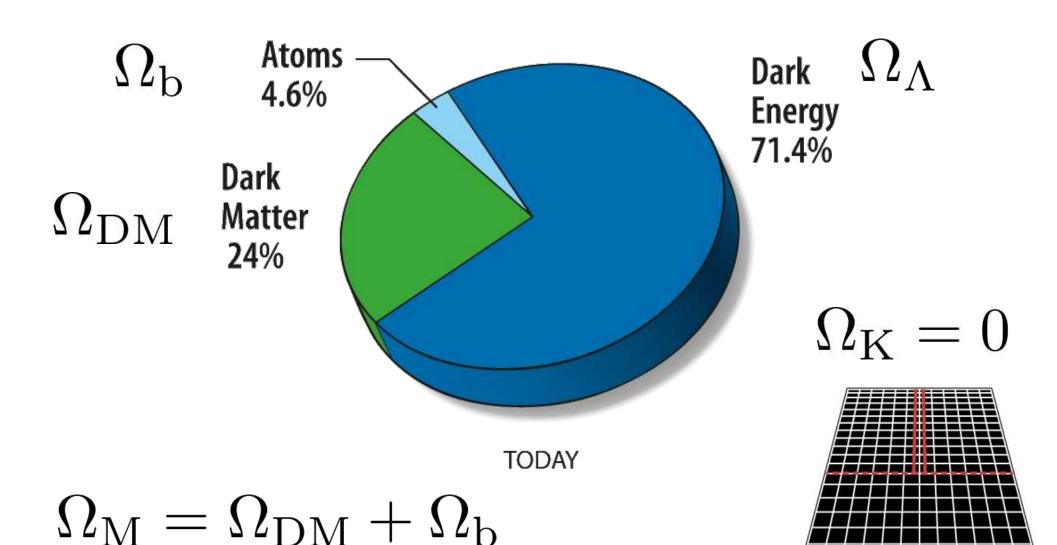


James Peebles

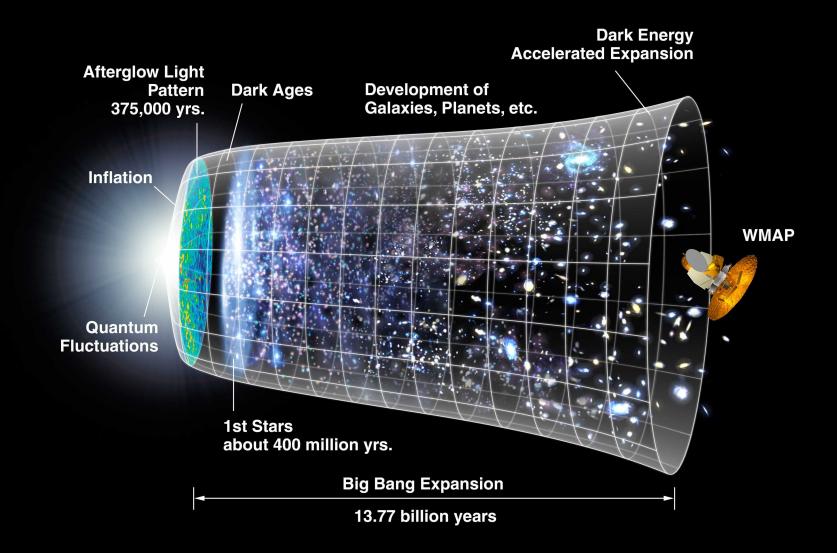
Michel Mayor

Didier Queloz

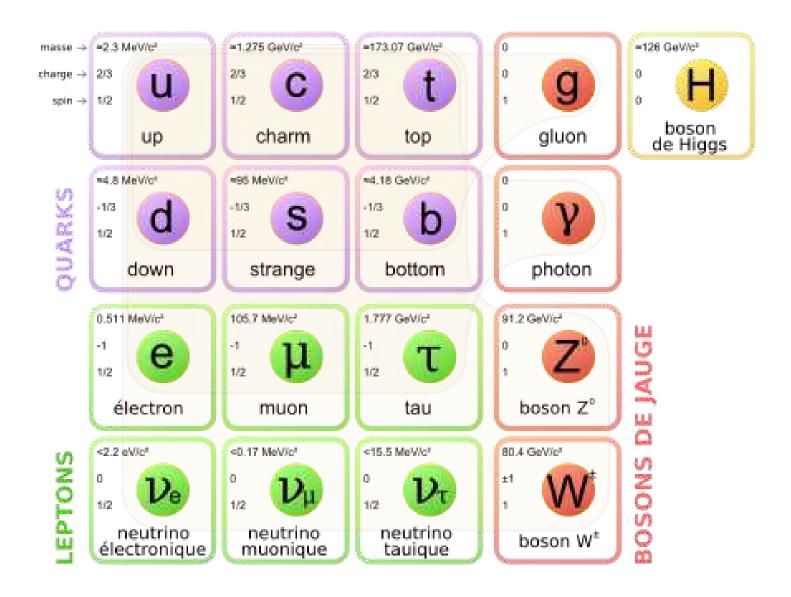




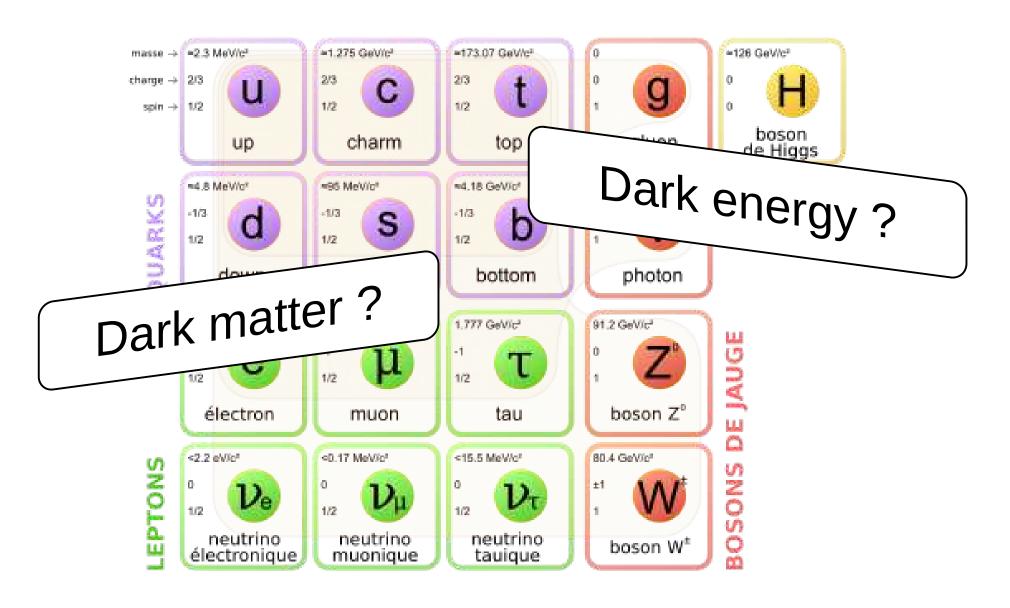
#### $a(t) = a(t, \Omega_{M}, \Omega_{K}, \Omega_{\Lambda})$



#### The standard model particle physics



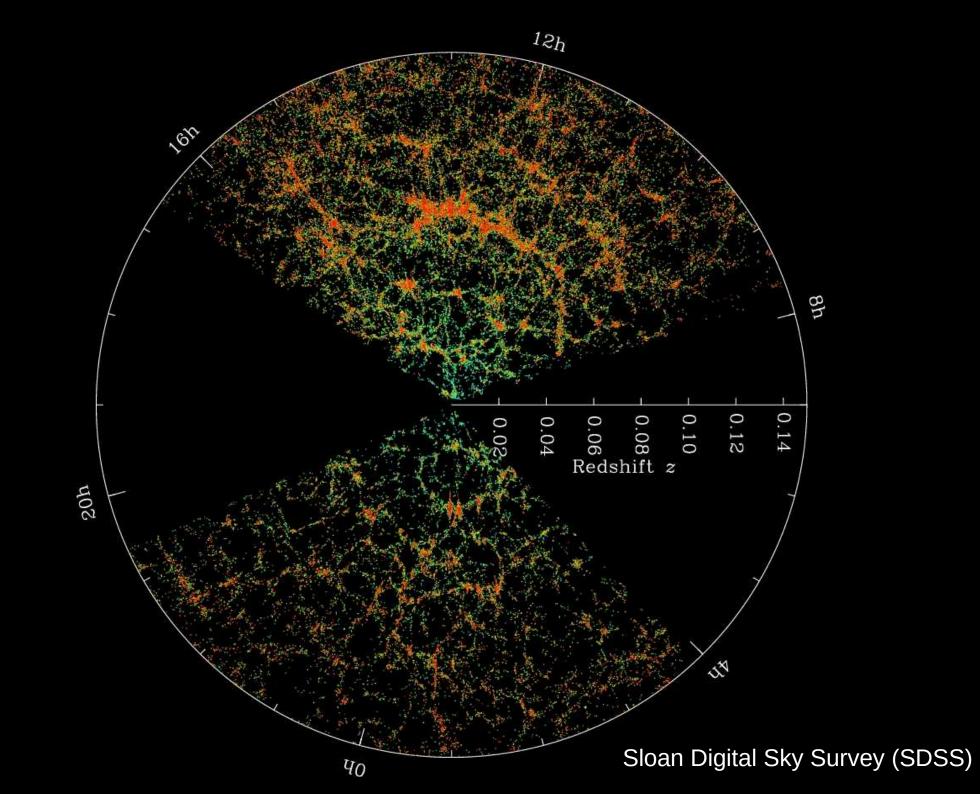
#### The standard model particle physics



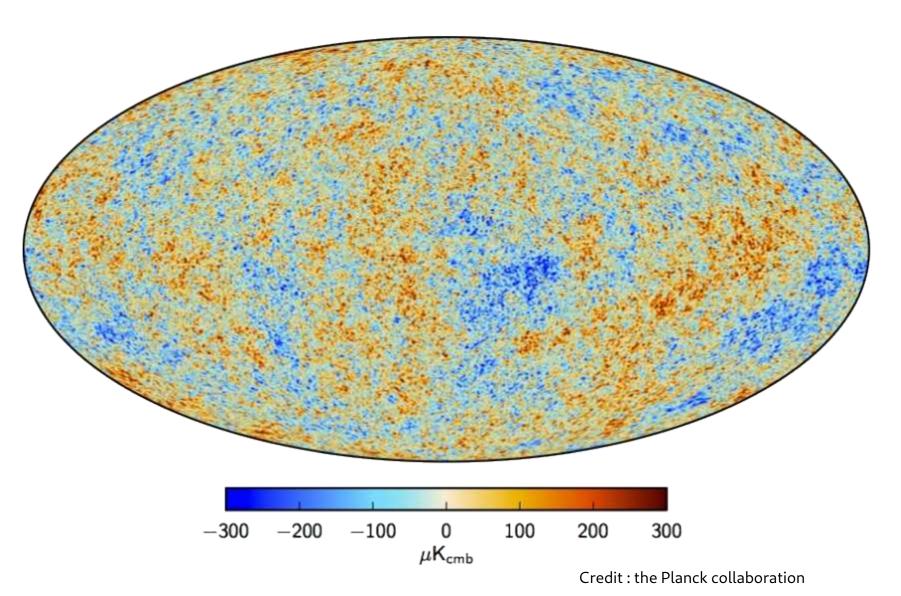
#### Introduction

# The formation of the large scale structures

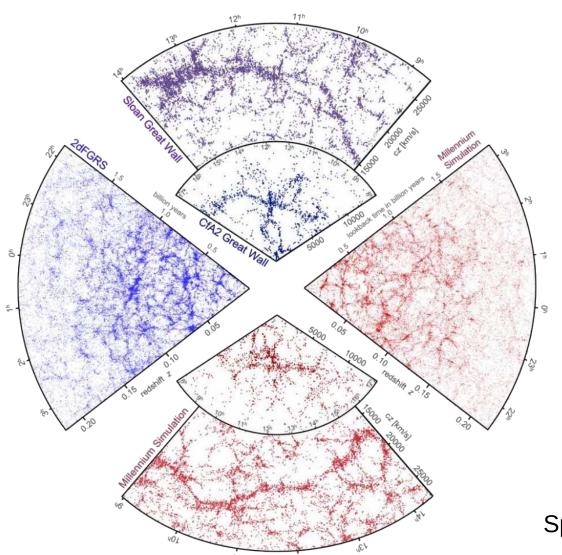
a quick overview



## Temperature/Density fluctuations of the universe (CMB) at the recombination epoch, when it was only 380'000 years old



# ACDM is successful at reproducing the large scale structure of our Universe



Springel et al. 2006

# Reproducing and understanding the Universe at small scale, at the scale of galaxies, is much more challenging...



#### Introduction

# Galaxy formation: Which physics?

# Galaxy formation Which physics?

- Gravity
- Gas hydrodynamics
- Gas radiative cooling, gas heating
- Star formation
- Stellar feedback (Supernovae Ia/II, AGB, etc.)
- Chemical evolution, gas mixing, diffusion
- Active Galactic Nuclei (AGN) feedback
- Cosmic rays
- Magnetic fields
- Thermal conductivity
- Dust
- ...

# Galaxy formation Which physics?

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- Thermal conductivity
- Dust
- ...

#### **Units**

Parsec (pc) = 3.2616 light year  $= 3.085 \times 10^{16}$  meter Distances:

Solar Mass (M<sub>o</sub>)  $= 2x10^{30} \text{ kg}$ Masses:

Solar Luminosity ( $L_{\odot}$ ) =  $3x10^{26}$  Watt Luminosities:

Time:

Giga Year (Gyr)  $= 10^9 \text{ yr}$ Mega Year (Myr)  $= 10^6 \text{ yr}$ 

Speed: km/s = km/s

Densities atom/cm<sup>3</sup>  $= 1.7x10^{-21} \text{ kg/m}^3 \text{ (air density)}$ 

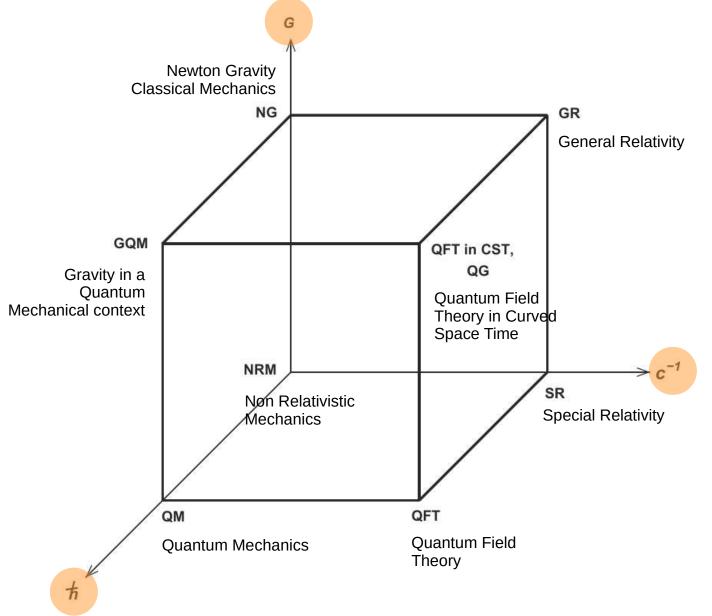
> $M_{\odot}$  /  $pc^3$  $= 6.7 \times 10^{-20} \text{ kg/m}^3 \text{ (air density)}$

lua

Credit: wikipedia

The cube of theoretical physics

Sleeping Beauties in Theoretical Physics (T. Padmanabhan)



**Fig. 1.1:** The landscape of theoretical physics can be concisely described by a cube — The Cube of Theoretical Physics — whose axes represents the three fundamental constants  $G,\hbar$  and  $c^{-1}$ . The vertices and linkages describe different structural properties of the physical theories. See text for detailed description.

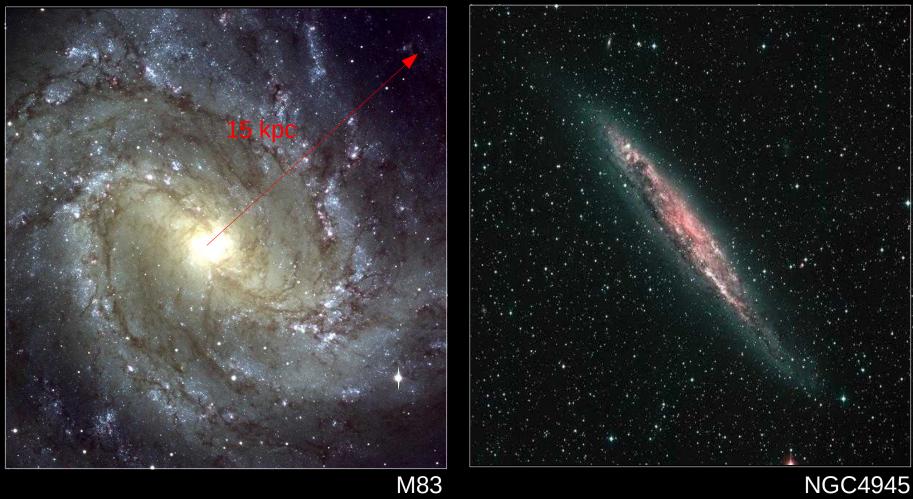
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#### Introduction

# Our galaxy The Milky Way

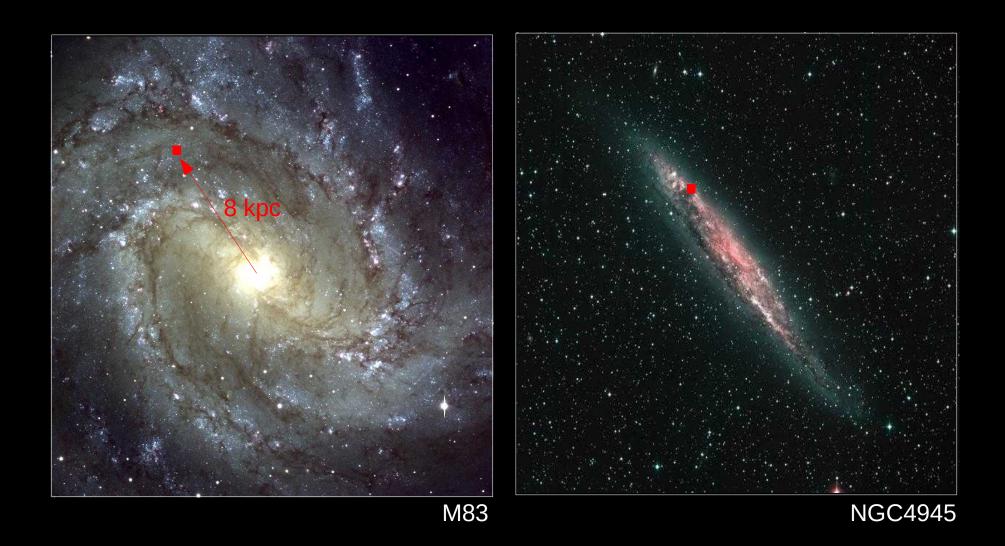


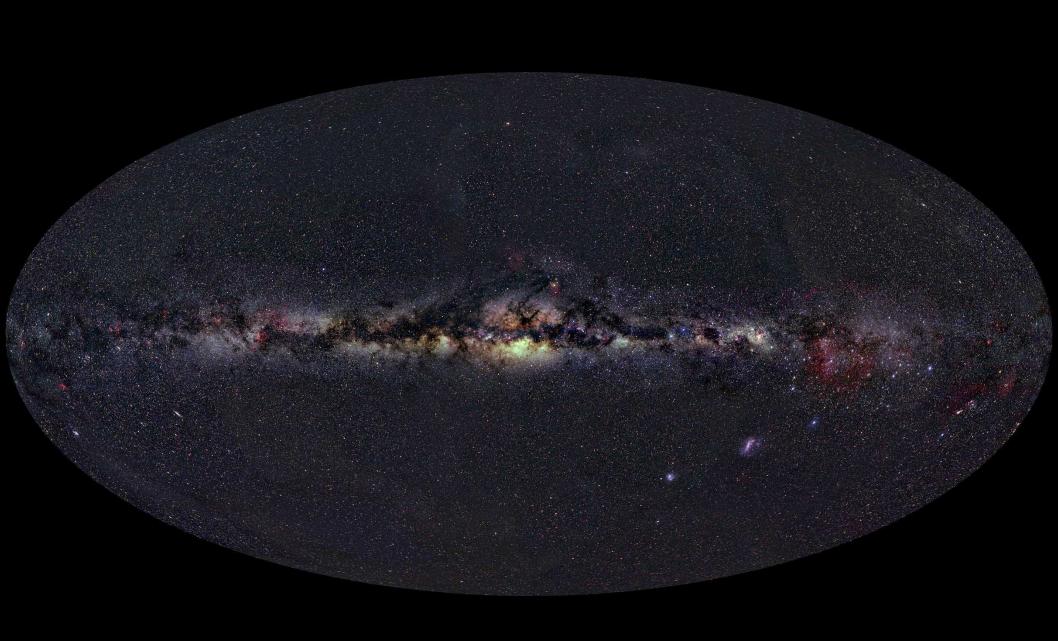
#### The Milky Way : a disky galaxy



NGC4945

#### Position of the Sun





#### **The Galactic Centre**



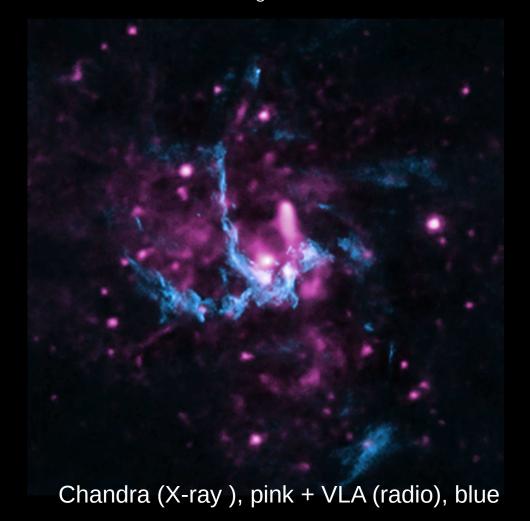
#### **The Galactic Centre**

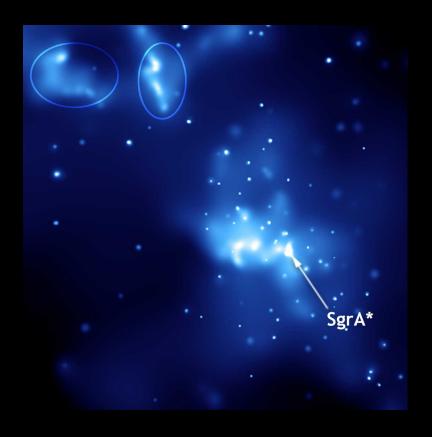
Very well determined via radio observations of the radio-source Sagittarius A\* (Galactic Black Hole)

Location: 17h45m 40.0409s (RA), -29°0'28.118" (DEC)

Distance: 25.900±1.400 light years (7.940±420 pc)

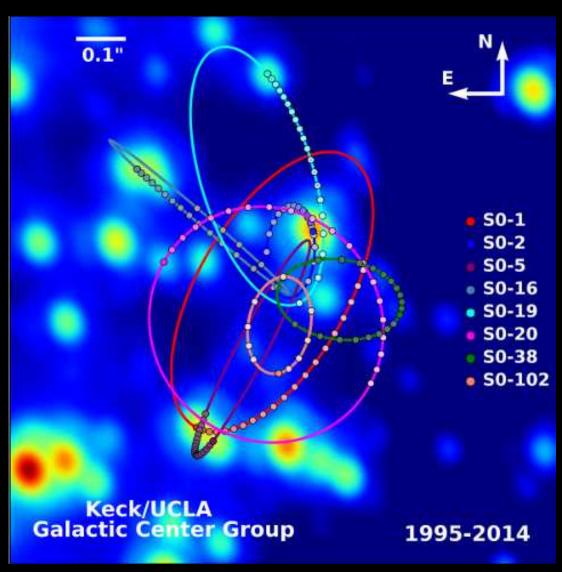
Mass: 4.31±0.38 10<sup>6</sup> M<sub>o</sub>





Chandra (X-ray)

### **The Galactic Centre BH**



http://www.astro.ucla.edu/~ghezgroup/gc/blackhole.html

https://youtu.be/xHMZOaQttqw

https://youtu.be/if2opecmev8

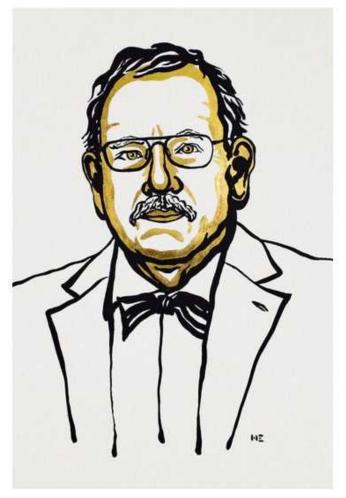
### The Nobel Prize in Physics 2020



III. Niklas Elmehed. © Nobel Media.

Roger Penrose

Prize share: 1/2



III. Niklas Elmehed. © Nobel Media.

Reinhard Genzel

Prize share: 1/4



III. Niklas Elmehed. © Nobel Media.

Andrea Ghez

Prize share: 1/4

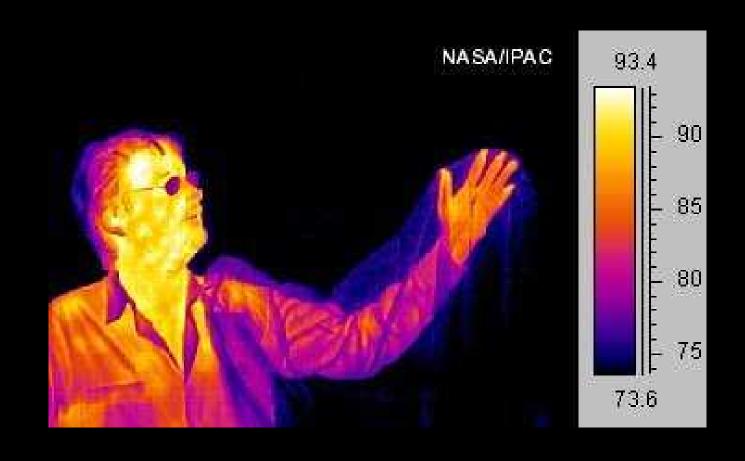
### Event Horizon Telescope (EHT) 2019

The accretion disk of the Milky Way black hole, seen in radio

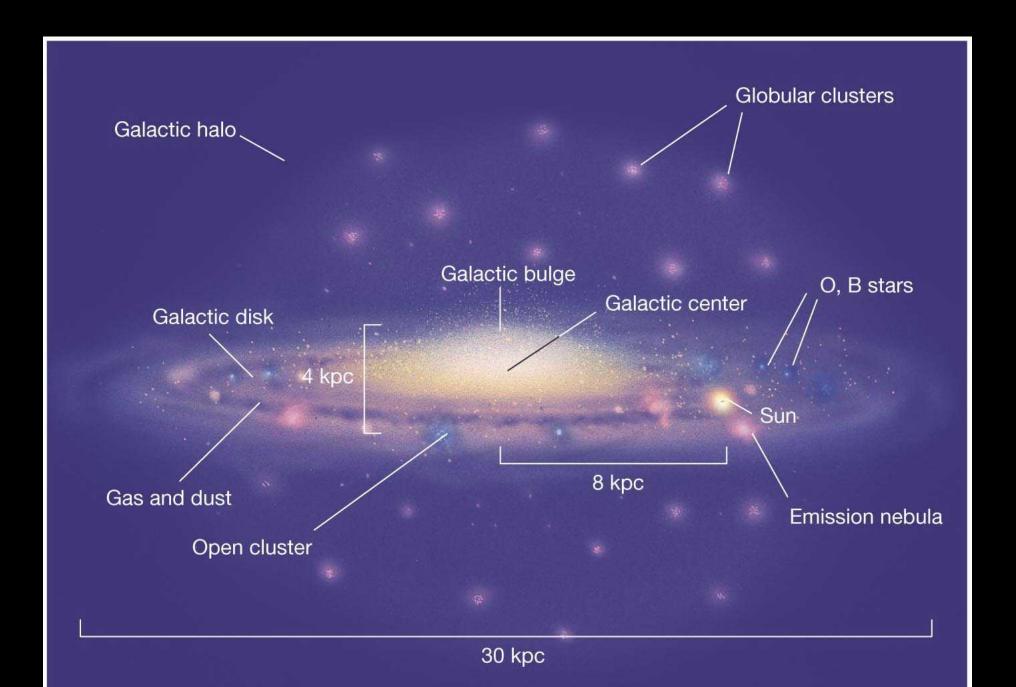
## The Milky Way in different wavelength



### The Milky Way in different wavelength



# Components of the WM



# Components of the WM



Diameter :

30 kpc

Total mass:

10<sup>12</sup> M<sub>o</sub>

**Rotation:** 

200 Myr (sun) 500 Myr (ext.)

# Stellar component : bulge/bar

 $0.5 \times 10^{10} \, \text{M}_{\odot}$ 



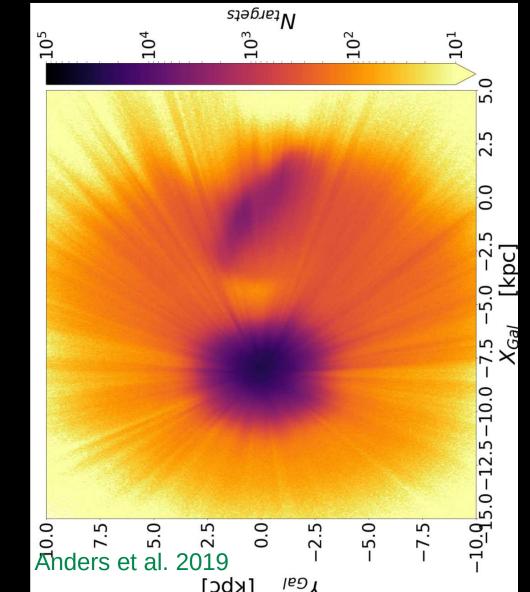
- old stars
- RMS vel ~150 km/s

### Stellar component : bulge/bar



265 millions of stars!





https://sci.esa.int/j/61461

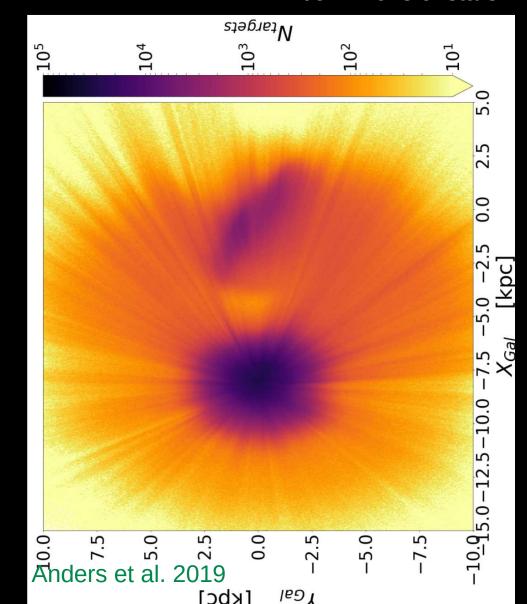
### Stellar component : bulge/bar



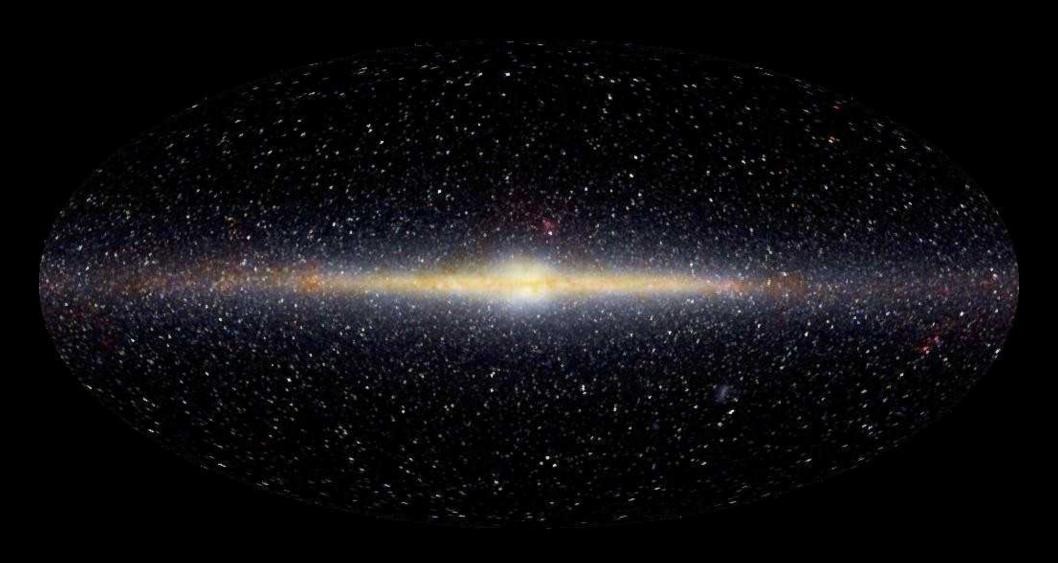
0.5x10<sup>10</sup> M<sub>e</sub>

265 millions of stars!





# COBE satellite view of the MW in infrared light



### Stellar component : disk

5x10<sup>10</sup> M<sub>o</sub> (10 % of total)

#### thin disk:

- 90% of the stellar disk
- scale height : ~300 pc
- RMS vel ~50 km/s



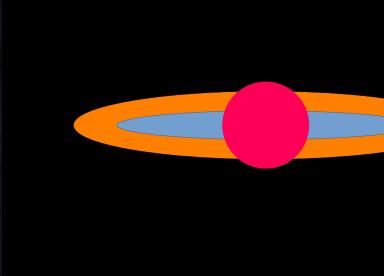


### Stellar component : disk

5x10<sup>10</sup> M<sub>o</sub> (10 % of total)

#### thick disk:

- 10% of the stellar disk
- scale height :  $\sim$ 1 kpc
- RMS vel >~50 km/s



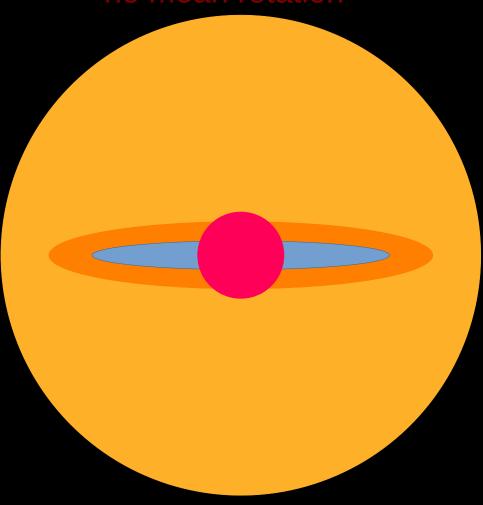


# Stellar component : halo

5x108 M<sub>o</sub> (1 % of stars)

- old stars
- no mean rotation





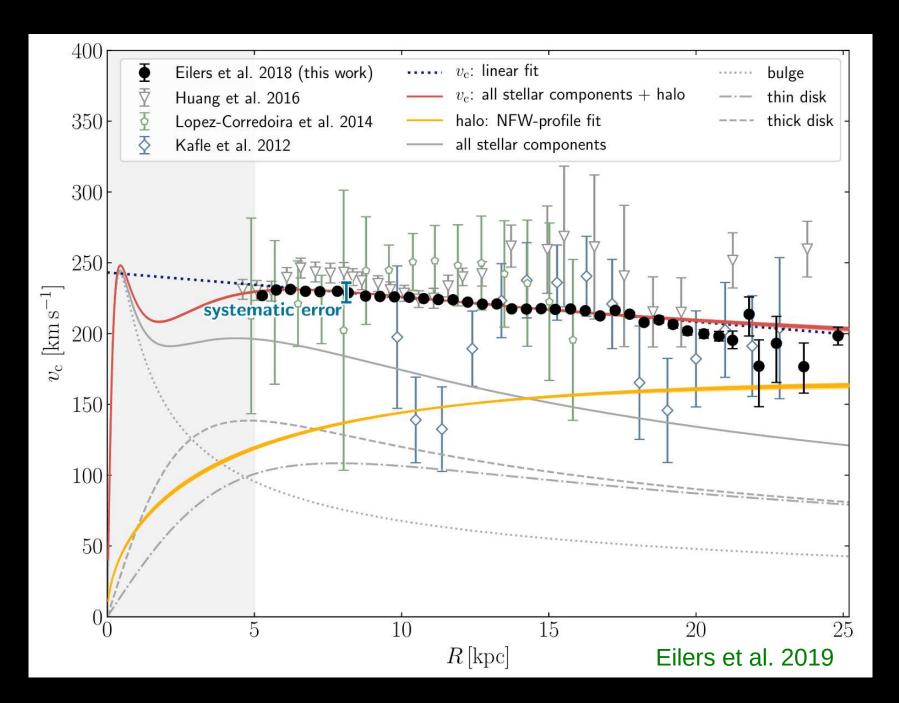
# Gaseous component : disk, HVC



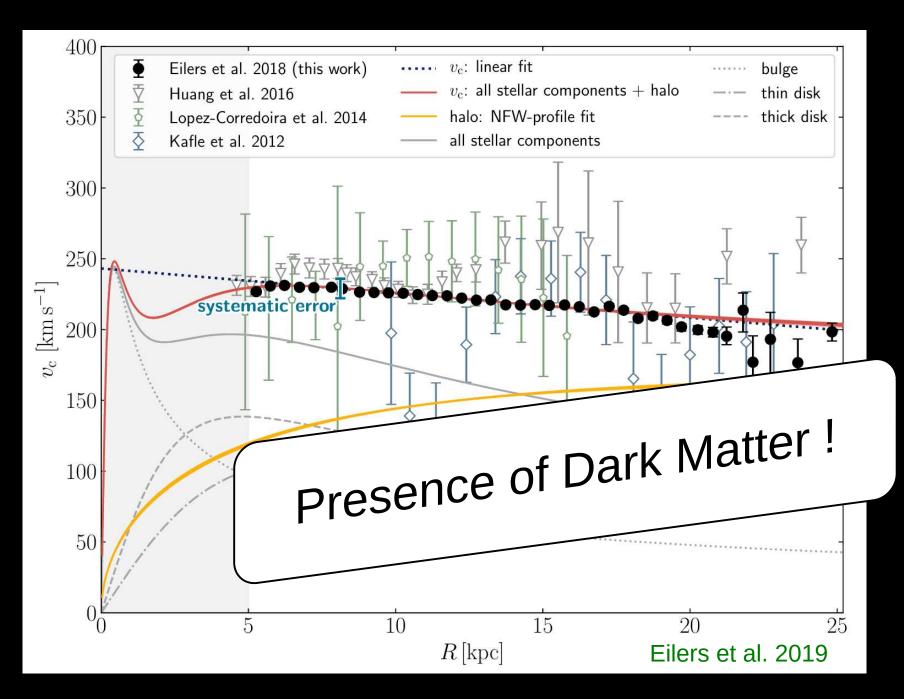
10° M<sub>®</sub> (0.1 %)



### The circular rotation curve of the MW

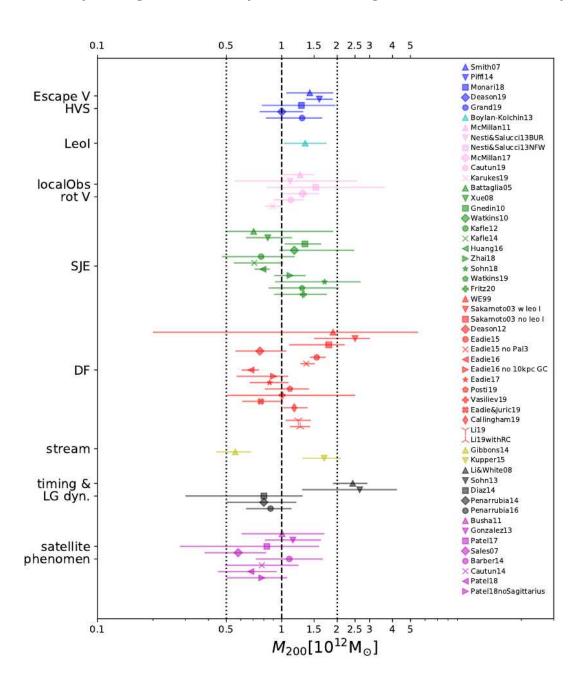


### The circular rotation curve of the MW



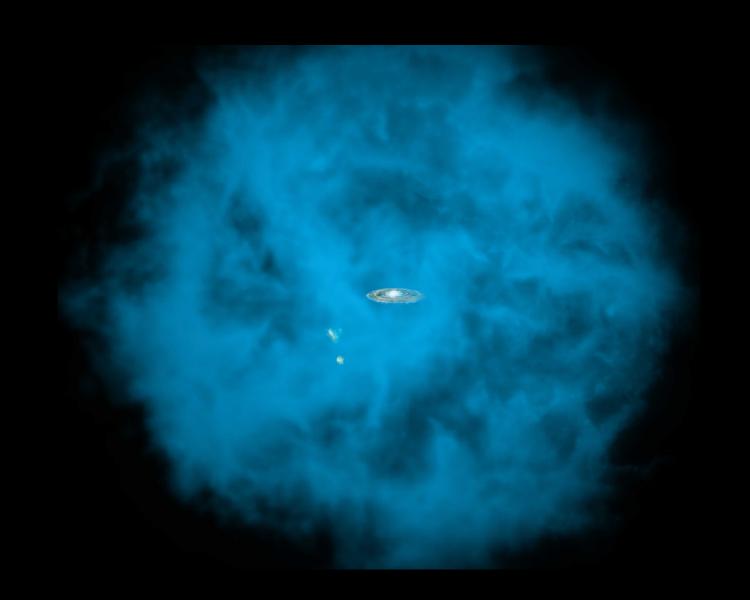
### The Milky Way total (gravitational) mass

(Wang 2019, https://arxiv.org/abs/1912.02599)



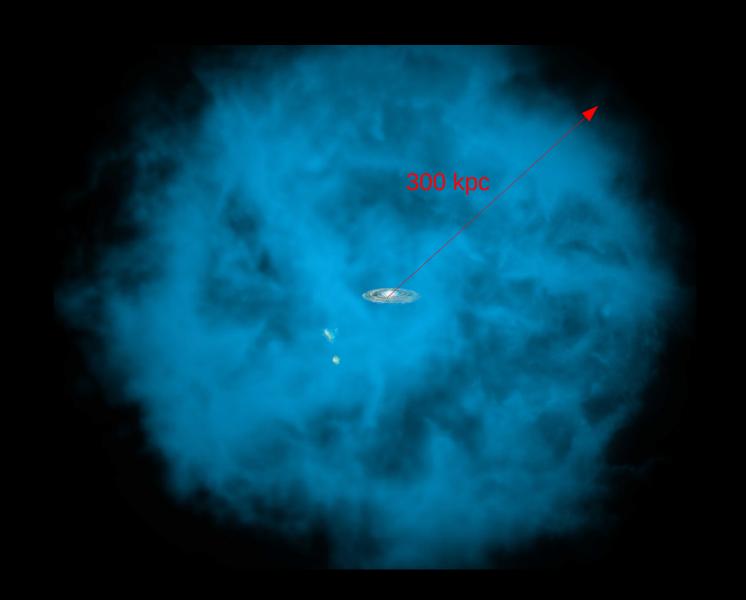
# dark component : dark matter halo

about 90% of the total mass,  $10^{12} \, M_{\odot}$ 



# dark component : dark matter halo

about 90% of the total mass,  $10^{12} \, M_{\odot}$ 



### The End