

Information, Computation, Communication

Learning Python

Numbers and Booleans

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Next topic: if-elif-else



Numbers and Types

- Python has three **numeric types**:
 - `int`: integer
 - 1, 2, 3, ...
 - -1, -2, -3 ...
 - `float`: floating-point numbers
 - 0.123, 109.239292, ...
 - `complex`: complex numbers
 - $1j$
 - $3 + 5j$



◀ Arithmetic Operations

- Type below numbers and operations in the Python interpreter and observe the output (i.e., the response after pressing **Enter**)

```
3           # => 3 (an integer number)
3.0        # => 3.0 (a floating number)
1 + 1      # => addition, returns 2
8 - 1      # => subtraction, returns 7
(1+2j) * 2 # => multiplication with complex
           # numbers, returns 2 + 4j (complex)
```

◀ Arithmetic Operations

Division

- Python supports two division operators: true and integer division

```
5 / 2      # => true division, 2.5
```

```
13 / 4     # => true division, 3.25
```

```
9 / 3      # => true division, 3.0
```

```
7 / 1.4    # => true division, 5.0
```

```
5 // 2     # => floor (also called integer) division, 2
```

```
13 // 4    # => floor division, 3
```

```
7 // 1.4   # => floor division, 5.0
```

```
-10 // 3   # => -4
```

Arithmetic Operations

Integer division

To remember

- True division always returns a floating point number
- In integer division, the result type depends on the types of the operands:
 - `int // int => int`
 - `float // float => float`
 - **One integer and one float => float**
- To change the numeric type, we use built-in functions `int()`, `float()`
 - The type change operation is also called type **casting**
- Integer division rounds fractional remainders **down**
 - Regardless of type and sign
 - The result is always lower or equal to the result of the true division

◀ Arithmetic Operations

Exponentiation and modulus

`2 ** 4` # => exponentiation, $2^{**}4 = 2*2*2*2 = 16$

`5 % 2` # => integer remainder (modulus), returns 1

$5 \% 2 = 5 - 2 * (5//2) = 5 - 4 = 1$

`9 % 3` # => integer remainder (modulus), returns 0

`-10 % 3` # => modulus, returns **2 !!!**

$-10 \% 3 = -10 - 3 * (-10//3) = -10 - 3*(-4)$





Booleans

◀ Booleans

- Bool type (Boolean) is a subtype of integer
- True equals 1, and False equals 0
- Boolean types are common in control flow expressions (if-else, loop)

```
True           # => returns True
False          # => returns False
type(True)    # => <class 'bool'>
True + 4       # => returns 5
```

Note the capital first letter:

- True
-  true
- False
-  false

Boolean (Logical) Operations

$x \text{ or } y$ # => logical OR

Logical OR:
True or ??? => True
False or True => True
False or False => False

$x \text{ and } y$ # => logical AND

Logical AND:
True and True => True
True and False => False
False and ??? => False

$\text{not } x$ # => logical negation

Logical negation:
not True => False
not False => True



Comparisons

Also known as relational operators

◀ Comparisons

```
1 < 2           # => Evaluate if 1 is less than 2,  
                # returns True  
  
2.0 >= 1        # => Evaluate if 2.0 is greater than or  
                # equal to 1, returns True  
  
7 == 7          # => Evaluate if 7 equals 7,  
                # returns True  
  
True == 1       # => Evaluate if True equals 1,  
                # returns True  
  
2.0 != 2        # => Evaluate if 2.0 is different than  
                # 2, returns False  
                # (2.0) != type(2) would return True
```

◀ Comparisons: Chained

```
x = 2 # create integer variable x and assign 2 to it
y = 4 # create integer variable y and assign 4 to it
z = 6 # create integer variable z and assign 6 to it
# Use variables in expressions
x < y < z      # => x < y and y < z, returns True
x < y > z      # => x < y and y > z, returns False
x == y < z     # => x == y and y < z, returns False
```



Logical Operations with Types other than Boolean

◀ Boolean (Logical) Operations

In the context of Boolean operations (and, or, not), the following values are interpreted as False:

- False
- None (a value commonly used to signify 'empty', or 'no value')
- Numeric zero of all numeric types
- Empty strings
- Empty lists, tuples, dictionaries, sets, ...

All other values are interpreted as True

◀ Logical Operations with Nonboolean Types

```
x or y      # => logical OR  
# from left to right
```

Logical OR, x or y :
If x is (interpreted as) True $\Rightarrow x$
If x is (interpreted as) False $\Rightarrow y$

```
# Examples:
```

```
3 or 5      # => 3
```

```
5 or 'EPFL' # => 5
```

```
0 or 3      # => 3
```

```
False or 'EPFL' # => 'EPFL'
```


◀ Logical Operations with Nonboolean Types

x and y # => logical AND
from left to right

Logical AND, x and y:
If x is (interpreted as) True => y
If x is (interpreted as) False => x

Examples:

3 and 5 # => 5

5 and 'EPFL' # => 'EPFL'

0 and 3 # => 0

'EPFL' and False # => False

◀ Logical Operations with Nonboolean Types

not x # => logical negation

from right to left

Examples:

not 3 # => False

not 0 # => True

not False # => True

not 'EPFL' # => False

Logical negation, not x:
If x is (interpreted as) True => False
If x is (interpreted as) False => True

Logical Operations with Nonboolean Types

Examples

What is the value of the following expressions?

Example 1

```
temp = 17
```

```
result = ((temp > 15) and 'black dress') or 'jeans'
```

Example 2

```
temp = 10
```

```
result = ((temp > 15) and 'black dress') or 'jeans'
```

Logical Operations with Nonboolean Types

Examples

What is the value of the following expressions?

Example 1

```
temp = 17
```

```
result = ((temp > 15) and 'black dress') or 'jeans'
```

```
# answer: 'black dress'; # steps:
```

```
# (1) temp > 15 returns True
```

```
# (2) True and 'black dress' returns 'black dress'
```

```
# (3) 'black dress' or 'jeans' returns 'black dress'
```

Example 2

```
temp = 10
```

```
result = ((temp > 15) and 'black dress') or 'jeans'
```

```
# answer: 'jeans'
```



Assignments

Assignment

Operator	Syntax	Meaning
=	$x = y + z$	Assign $x = y + z$
+=	$x += y$	Add and assign $x = x + y$
-=	$x -= y$	Subtract and assign $x = x - y$
*=	$x *= y$	Multiply and assign $x = x * y$
/=	$x /= y$	Divide (true) and assign $x = x / y$
%=	$x %= y$	Compute modulo and assign $x = x \% y$
//=	$x //= y$	Divide (integer) and assign $x = x // y$
**=	$x **= y$	Calculate exponent and assign $x = x ** y$

- Assignment operator computes the value of the expression on the right and assigns it to the operand on the left
- Assignment operator can be combined with arithmetic operators

Assignment Operators

Examples

What is the value of the following expressions?

Example 1

a = 5

x = 3

y = 0

a *= x - (y <= x)

Assignment Operators

Examples

What is the value of the following expressions?

Example 1

a = 5

x = 3

y = 0

a *= x - (y <= x)

answer: a = 10

steps:

(1) y <= x returns True

(2) x - True returns 2

(3) a *= 2 returns a*2 which equals 10



Operator Precedence

Precedence of Operators

- Python will always evaluate the arithmetic operators first
 - `**` is highest, then multiplication/division, then addition/subtraction
- Next come the relational operators
- The logical operators are done last

Priority level	Category	Operators	Associativity
7 (highest)	Exponent	<code>**</code>	right to left
6	Multiplication, etc.	<code>*</code> , <code>/</code> , <code>//</code> , <code>%</code>	left to right
5	Addition and subtraction	<code>+</code> , <code>-</code>	left to right
4	Relational	<code><=</code> , <code>>=</code> , <code>></code> , <code><</code> , <code>==</code> , <code>!=</code>	left to right
3	Logical	<code>not</code>	right to left
2	Logical	<code>and</code>	left to right
1 (lowest)	Logical	<code>or</code>	left to right

Precedence of Operators

The acronym **PEMDAS** is a convenient way to remember the rules

- **P**arentheses have the **highest** precedence and can be used to force an expression to evaluate in the order you want
- **E**xponentiation has the next highest precedence
- **M**ultiplication and **D**ivision have the same precedence, which is **higher** than **A**ddition and **S**ubtraction, which also have the same precedence



Precedence of Operators

Examples - PEMDAS

What is the value of the following expressions?

Example 1

```
result = True or False and False
```

Precedence of Operators

Examples - PEMDAS

What is the value of the following expressions?

Example 1

```
result = True or False and False
```

answer: True

Steps:

and has a higher precedence over *or*

result = True or (False and False)

False and False => False

True or False => True

Precedence of Operators

Examples - PEMDAS

What is the value of the following expressions?

Example 2

```
result = 2 ** 3 ** 2
```

Precedence of Operators

Examples - PEMDAS

What is the value of the following expressions?

Example 2

```
result = 2 ** 3 ** 2
```

answer: 512

Steps:

associativity: right to left

```
# result = 2 ** (3 ** 2)
```

```
# 3 ** 2 = 9
```

```
# result = 2 ** 9 = 512
```

Precedence of Operators

Examples - PEMDAS

What is the value of the following expressions?

Example 3

`a = b = 0`

`result = a < b + 5`

Precedence of Operators

Examples - PEMDAS

What is the value of the following expressions?

```
# Example 3
```

```
a = b = 0
```

```
result = a < b + 5
```

```
# answer: True
```

```
# Steps:
```

```
#   addition has a higher precedence over <
```

```
#   result = 0 < (b + 5)
```

```
#   b + 5 = 5
```

```
#   0 < 5 => True
```



Next topic: **If-elif-else**