Table 6.5: Statistical models in R. Lower case letters denote continuous numeric variables and uppercase letters denote factors. Note that the error term is always implicit.

| Effects model | R Model formular | Description |
| :---: | :---: | :---: |
| $y_{i}=\beta_{0}+\beta_{1} x_{i}$ | $y \underset{y}{\sim} \sim 1+x$ | Simple linear regression model of y on x with intercept term included |
| $y_{i}=\beta_{1} x_{i}$ | $\begin{aligned} & y \sim 0+x \\ & y \sim-1+x \\ & y \sim x-1 \end{aligned}$ | Simple linear regression model of $y$ on $x$ with intercept term excluded |
| $y_{i}=\beta_{0}$ | $\begin{aligned} & y \sim 1 \\ & y \\ & \sim \end{aligned}$ | Simple linear regression model of y against the intercept term |
| $y_{i}=\beta_{0}+\beta_{1} x_{i 1}+\beta_{2} x_{i 2}$ | y ~ $\mathrm{x} 1+\mathrm{x} 2$ | Multiple linear regression model of y on x 1 and x 2 with the intercept term included implicitly |
| $y_{i}=\beta_{0}+\beta_{1} x_{i 1}+\beta_{2} x_{i 1}^{2}$ | $\begin{aligned} & y \sim 1+x+I\left(x^{\wedge} 2\right) \\ & y \sim \operatorname{poly}(x, 2) \end{aligned}$ | Second order polynomial regression of $y$ on $x$ <br> As above, but using orthogonal polynomials |
| $y_{i j}=\mu+\alpha_{i}$ | y ~ A | Analysis of variance of $y$ against a single factor $A$ |
| $y_{i j k}=\mu+\alpha_{i}+\beta_{j}+\alpha \beta_{i j}$ | $\begin{aligned} & y \underset{\sim}{\sim} \underset{y}{\sim}+B+B \\ & \sim A: B \end{aligned}$ | Fully factorial analysis of variance of $y$ against $A$ and $B$ |
| $y_{i j k}=\mu+\alpha_{i}+\beta_{j}$ | $\mathrm{Y} \sim \mathrm{A} * \mathrm{~B}-\mathrm{A}: B$ | Fully factorial analysis of variance of $y$ against $A$ and $B$ without the interaction term (equivalent to $\mathrm{A}+\mathrm{B})$ |
| $y_{i j k}=\mu+\alpha_{i}+\beta_{j(i)}$ | $\begin{aligned} & y \sim B \text { \%in\% } A \\ & y \sim A / B \end{aligned}$ | Nested analysis of variance of $y$ against $A$ and $B$ nested within $A$ |
| $y_{i j}=\mu+\alpha_{i}+\beta\left(x_{i j}-\bar{x}\right)$ | $\begin{aligned} & y \sim A * x \\ & y \sim A / x \end{aligned}$ | Analysis of covariance of $y$ on $x$ at each level of A |
| $\begin{gathered} y_{i j k l}=\mu+\alpha_{i}+\beta_{j(i)}+\gamma_{k}+ \\ \alpha \gamma_{i k}+\beta \gamma_{j(i) k} \end{gathered}$ | $\begin{aligned} & y \sim A+\operatorname{Error}(B)+ \\ & C+A: C+B: C \end{aligned}$ | Partly nested ANOVA of y against a single between block factor (A), a single within block factor (C) and a single random blocking factor (B). |

