Chapter 6: The Edges Library
Why is $a_i$ a condition for $a_j$?

$E = \{ e_{ij} \mid e_{ij}: (a_i, a_j, \{\text{operators}\}, \text{label}, \text{weight}) \}$

How much is $a_i$ a condition for $a_j$?
### Library of Edge Labels

Why is $a_i$ a condition for $a_j$?

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<th>Preparation</th>
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Why is \( a_i \) a condition for \( a_j \) ?

The preparation edges connect two activities when the learner has a higher probability of succeeding at \( a_j \) if he carried out \( a_i \) before \( a_i \).

The set edges connect two activities when the skills or contents addressed in \( a_i \) and \( a_j \) are in relationship with each other; for example, subset/superset, whole/part, and siblings. (UP / DOWN)

The translation edges connect two activities in which the same content is addressed under different formats, representations, notations, or viewpoints. Learners therefore have to translate the representation used in \( a_i \) into the representation used in \( a_j \).

The generalization edges introduce variations of the content or skills across the space of generalization, namely introducing the student to more general, less general, or analogical contexts from \( a_i \) to \( a_j \). (UP / DOWN)
Pre-requisites are common sense: You need to be able to do $5+7 \ (a_i)$, before trying $25+37 \ (a_j)$.

Nonetheless, a high portion of failure is explained the accumulation of small gaps in pre-requisites.

Mastery learning focused especially on this sequencing.
Preparation Edges

- Prerequisite
- Zone of Proximal Development
- Adv. Organizer
- Motivation
- Anticipation
- Logistics
- Data collection

What I do \( (a_i) \)

in interaction with a more knowledgeable peer

What I can do alone \( (a_i) \)

CHAPTER 6
In the first activity, students solve equations individually. The teacher analyzes their work and identifies those who concentrate on algebraic manipulations compared to those able to think in terms of problem-solving strategy. In the second activity, a student from the first category is asked to work with a student from the second category. The latter is expected to convey his strategies by arguing about the choice of equation manipulations proposed by the former.
An advance organizer is information presented by an instructor that helps the student organize new incoming information (D. Ausubel):

- Reactivate previous knowledge
- Preactivate knowledge structures
Preparation Edges

- Prerequisite
- ZPD
- Adv. Organizer
- Motivation
- Anticipation
- Logistics
- Data collection

“What you will learn today”

Class

“Advance organizer and extrinsic motivation”

Team

Teach the Cartesian coordinate system

Individual

Play naval battle
Preparation Edges

- Prerequisite
- ZPD
- Adv. Organizer
- Motivation
- Anticipation
- Logistics
- Data collection

Students may try to get the reward without learning anythings.

It is sometimes hard to demonstrate why some skills are useful.
The teacher reminds students of the model taught the previous week and asks students to install a new simulation tool (logistics edge). He gives them a phenomenon for which the previous model produces incorrect results, which will justify a revision of the previous model.
Preparation Edges

- Prerequisite
- ZPD
- Adv. Organizer
- Motivation
- Anticipation
- Logistics
- Data collection
Set Edges

(S+) Aggregation
(S+) Expansion
(S-) Decomposition
(S-) Selection
(S=) Juxtaposition
(S=) Contrast
(S=) Identity

Knowledge space or « Class-Structure » of the domain to be taught.

Bringing the learner up/down and left/right in this knowledge space.
After an introduction, the teacher splits the class into two subclasses, those who have already studied how to form questions and negative sentences in English, and those who have not. The novices do individual exercises on each skill (first questions and then negative sentences), and finally these two skills are aggregated during pair dialogue exercises that include negative questions. The more experienced subclass starts directly with the pair dialogue exercises, but the students who encounter difficulties are then redirected towards individual exercises on each skill.
After an introductory video, the participants in this MOOC, "Introduction to statistics," are split into 2 subclasses for individual activities. In the first subclass, students acquire procedural knowledge—how to manually calculate the standard deviation for a set of 20 data points. In the second subclass, students acquire declarative knowledge—the concepts of dispersion, heterogeneity and variance, and illustrated graphical representations. Then, each student from a subclass is paired with a student from the other subclass, and collaboratively they first have to do a quiz that measures declarative knowledge and then a task that requires procedural knowledge. To be able to collaborate with their peer, those who acquired declarative knowledge individually have to proceduralize it with the help of their peer, and those who acquired procedural knowledge individually have to elicit it (next edge label).
Translation Edges

- Proceduralization
- Elicitation
- Alternate
- Reframe
- Reverse
- Repair
- Teach

http://www.nctm.org/classroom-resources/lessons/Graphical-Representations-for-the-Number-of-Hits/
Translation Edges

- Proceduralization
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- Multiple types (procedural, declarative)
- Multiple levels of abstraction (concrete, abstract)
- Multiple representations
- Multiple viewpoints
- Multiple scales
- Multiple methods
- .....
A **splountz** is a triangle with 3 smaller shapes placed on different sides, one in the same color as the triangle and the two others in a different color.
A **splountz** is a triangle with 3 smaller shapes placed on different sides, one in the same color as the triangle and the two others in a different color.

Is this a Splountz?

- ☑ Yes
- ❌ No
Label \((A_1, A_2)\) = deduction

From the general to the particular
A_1

**SPUCs**

- Positive instances
- Near-Miss instances
- Negative instances

*Diagram depicting different instances and near-miss instances.*
$A_2$

What is a SPUC?
Label \((A_1,A_2)\) = induction

From the particular to the general
Generalisation Edges

(G+) Induction
(G+) Deduction
(G+) Extraction
(G+) Synthesis
(G=) Analogy
(G=) Transfer
(G–) Restriction

Concept

Example

Example

induction

analogy

deduction
The problem of transfer

“If 1 bottle of milk costs 5 francs, how many can I buy for 35 francs”

“If a car travels a distance of one kilometer in 5 minutes, how many kilometers will the car travel if it continues at the same speed for 35 minutes.”

“If 2 books 10 francs, how many can I buy for 50 francs”

Humans are not very good at transfer because knowledge structures are very much anchored into a specific context.
The problem of transfer

- PCA for online learning analytics
- Near transfer
- PCA in online shopping analytics
- Far transfer
- PCA for computer vision
The learners become better in transfer if, during the learning scenario, the teacher paid attention to vary systematically the context of the examples/exercises presented.
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### Edge Labels

- **Concrete**: Represented by a solid square.
- **Procedural**: Represented by a hollow square.
- **Symbolic**: Represented by a diagonal line through a square.

### Arrow Types

- **S+**: Solid arrow.
- **S-**: Solid arrow with a bar.
- **S=**: Solid arrow with a bar and another bar.

### Level Indicators

- **G+**: Red arrow with a plus sign.
- **G-**: Red arrow with a minus sign.
- **G=**: Red arrow with a equals sign.
A learning scenario must explore the knowledge mesh in multiple ways, creating multiple pathways between various formats of knowledge.

You don’t know a forest if you walk around it or across it but only if you have crossed it in many ways, many directions, etc.
The orchestration graph translates this multidimensional exploration into a linear path, because time is linear.